

Introduction à l'informatique CM9

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aeporreca.org/introinfo

Interface pour les arbres binaire

```
def nouveau_nœud(valeur, gauche, droite):
```

```
    ...
```

```
def est_vide(arbre):
```

```
    ...
```

```
def valeur(nœud):
```

```
    ...
```

```
def gauche(nœud):
```

```
    ...
```

```
def droite(nœud):
```

```
    ...
```

Implémentation avec des tableaux

Implémentation avec des tableaux

```
def nouveau_nœud(valeur, gauche, droite):  
    return [valeur, gauche, droite]
```

Implémentation avec des tableaux

```
def nouveau_nœud(valeur, gauche, droite):  
    return [valeur, gauche, droite]  
  
def est_vide(arbre):  
    return arbre is None
```

Implémentation avec des tableaux

```
def nouveau_nœud(valeur, gauche, droite):  
    return [valeur, gauche, droite]
```

```
def est_vide(arbre):  
    return arbre is None
```

```
def valeur(nœud):  
    return nœud[0]
```

Implémentation avec des tableaux

```
def nouveau_nœud(valeur, gauche, droite):  
    return [valeur, gauche, droite]
```

```
def est_vide(arbre):  
    return arbre is None
```

```
def valeur(nœud):  
    return nœud[0]
```

```
def gauche(nœud):  
    return nœud[1]
```

Implémentation avec des tableaux

```
def nouveau_nœud(valeur, gauche, droite):  
    return [valeur, gauche, droite]
```

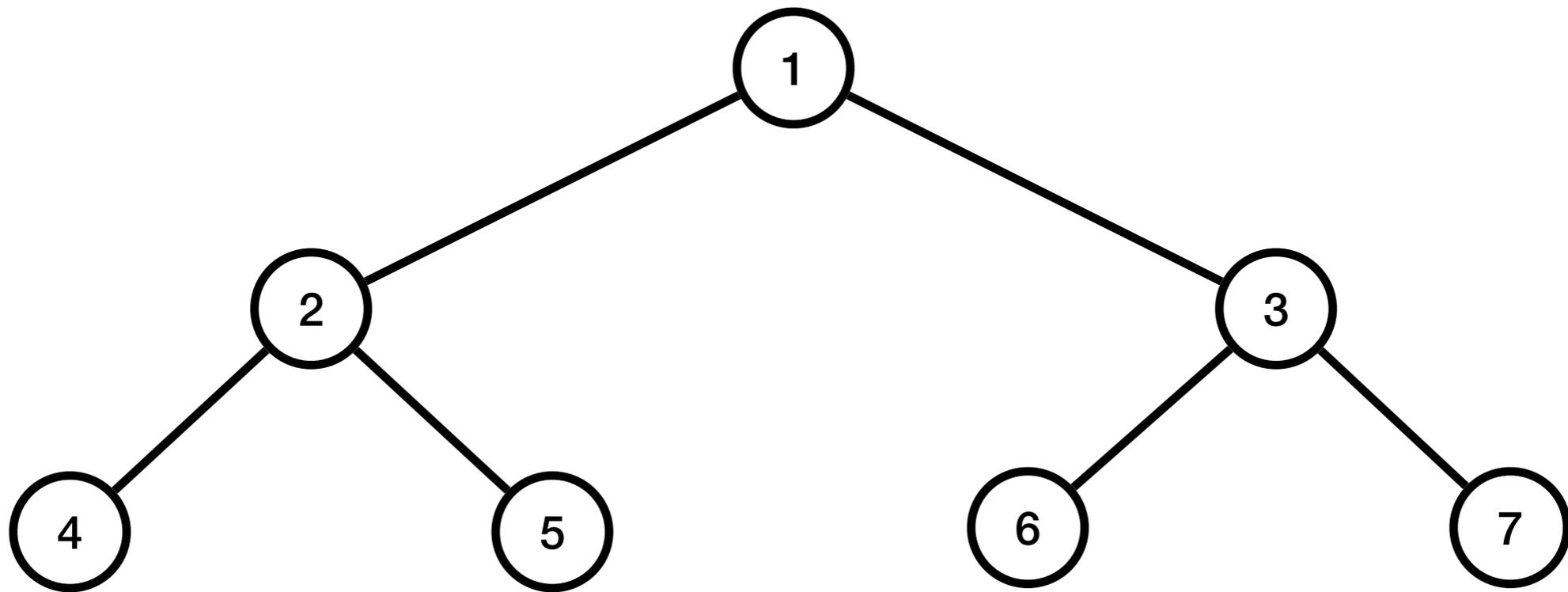
```
def est_vide(arbre):  
    return arbre is None
```

```
def valeur(nœud):  
    return nœud[0]
```

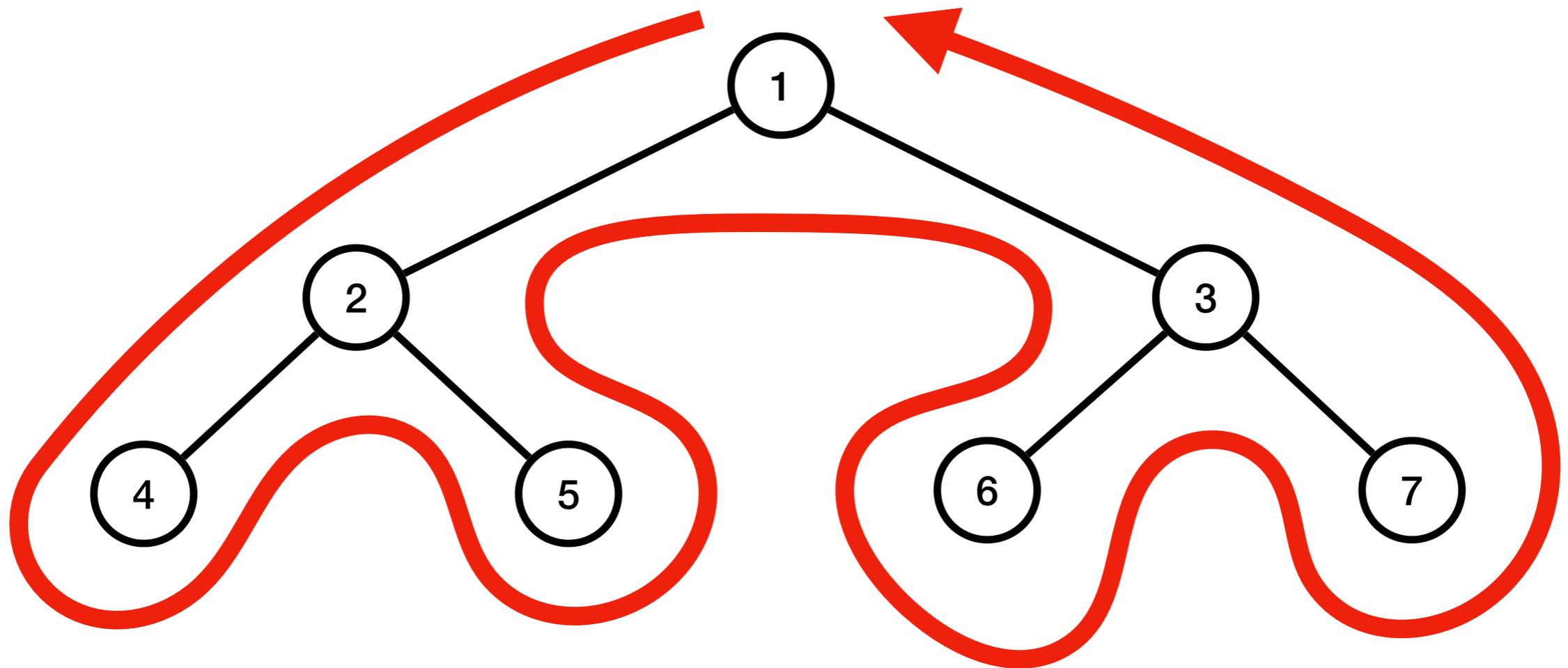
```
def gauche(nœud):  
    return nœud[1]
```

```
def droite(nœud):  
    return nœud[2]
```

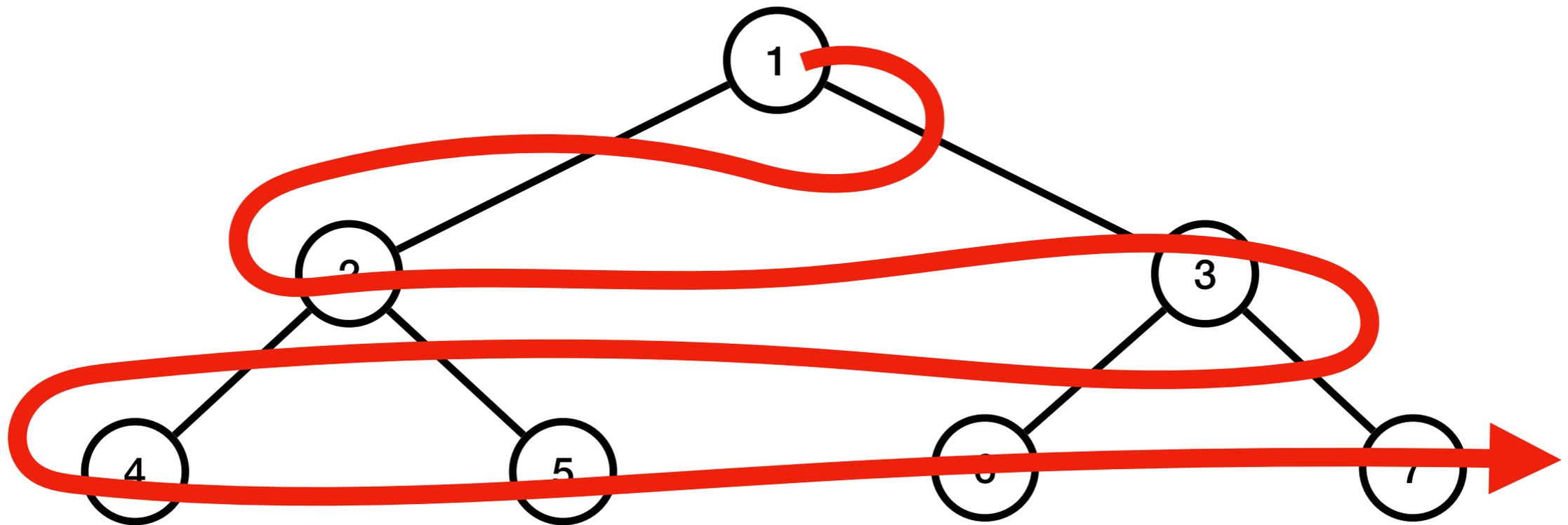
Parcours d'arbres binaires



Parcours d'arbres binaires



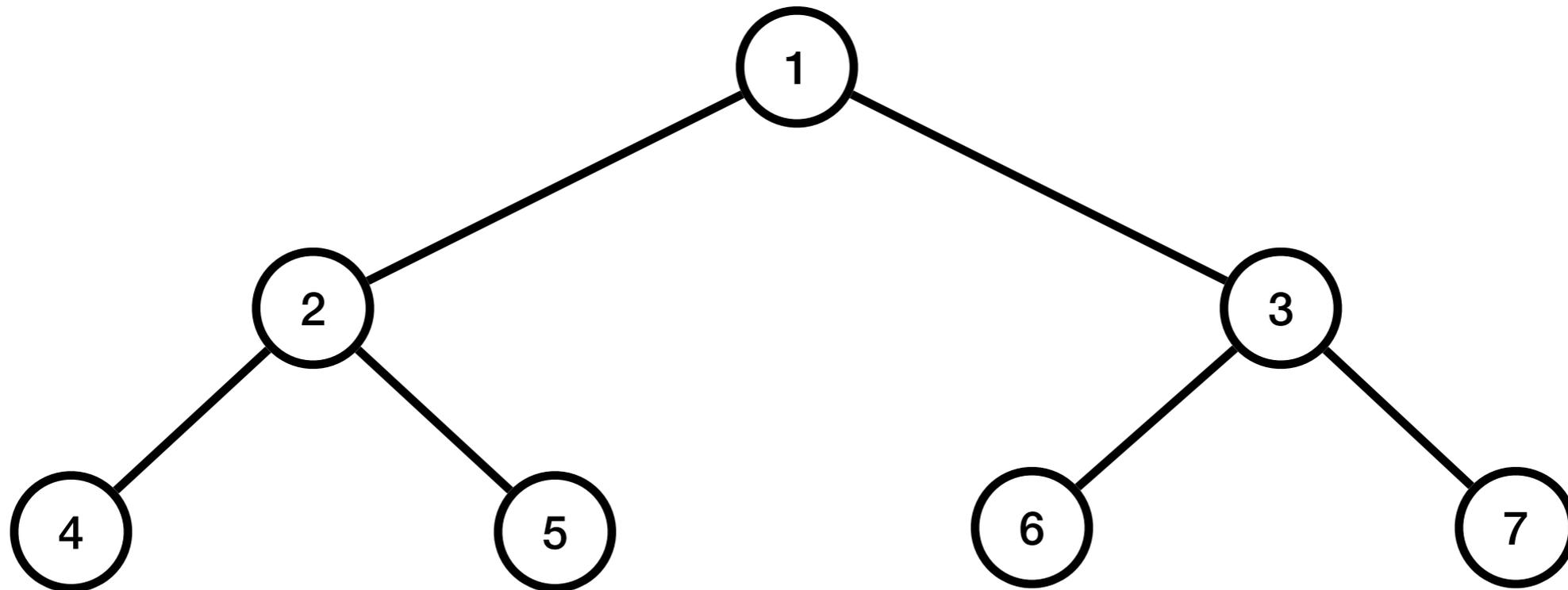
Parcours d'arbres binaires



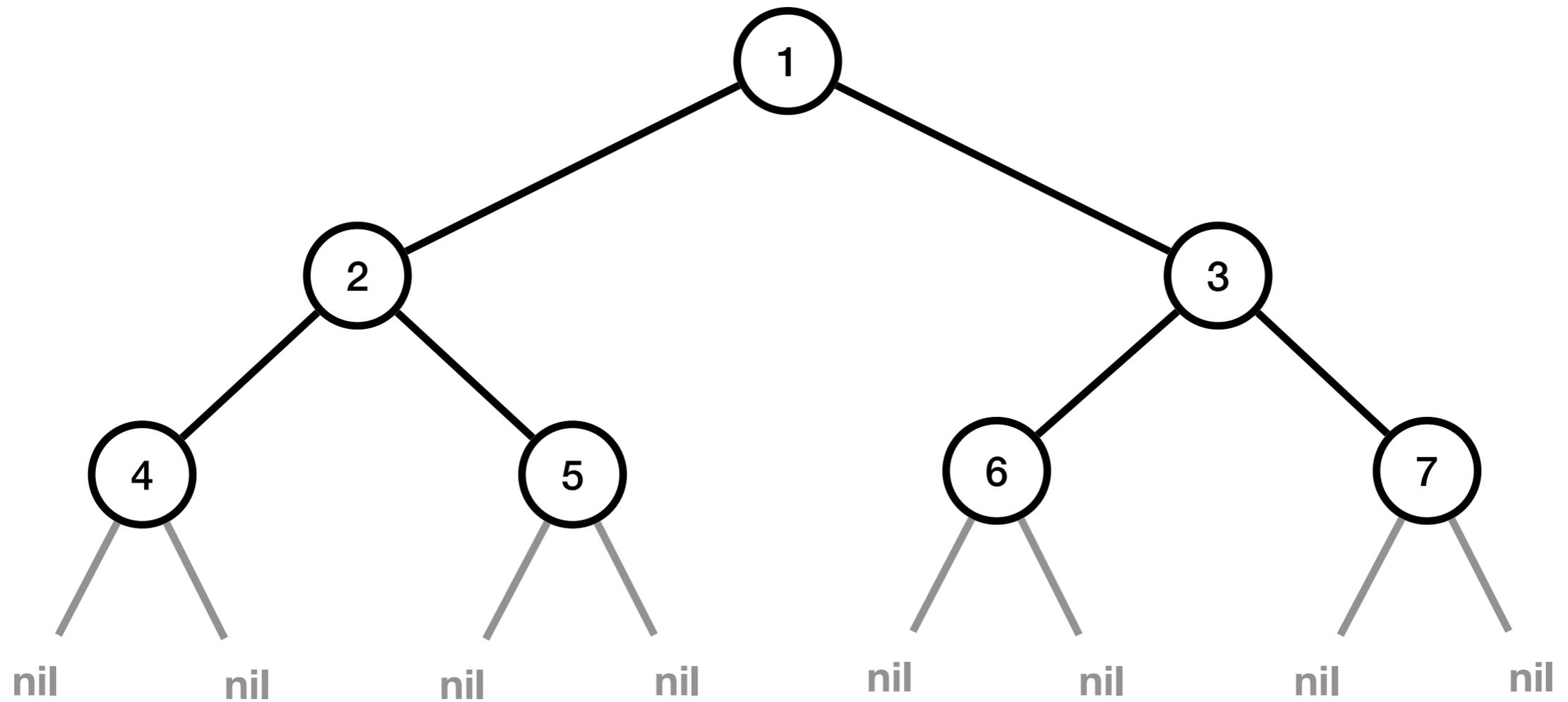
Parcours préfixe

```
def parcours_préfixe(arbre):  
    if not est_vide(arbre):  
        print(valeur(arbre))  
        parcours_préfixe(gauche(arbre))  
        parcours_préfixe(droite(arbre))
```

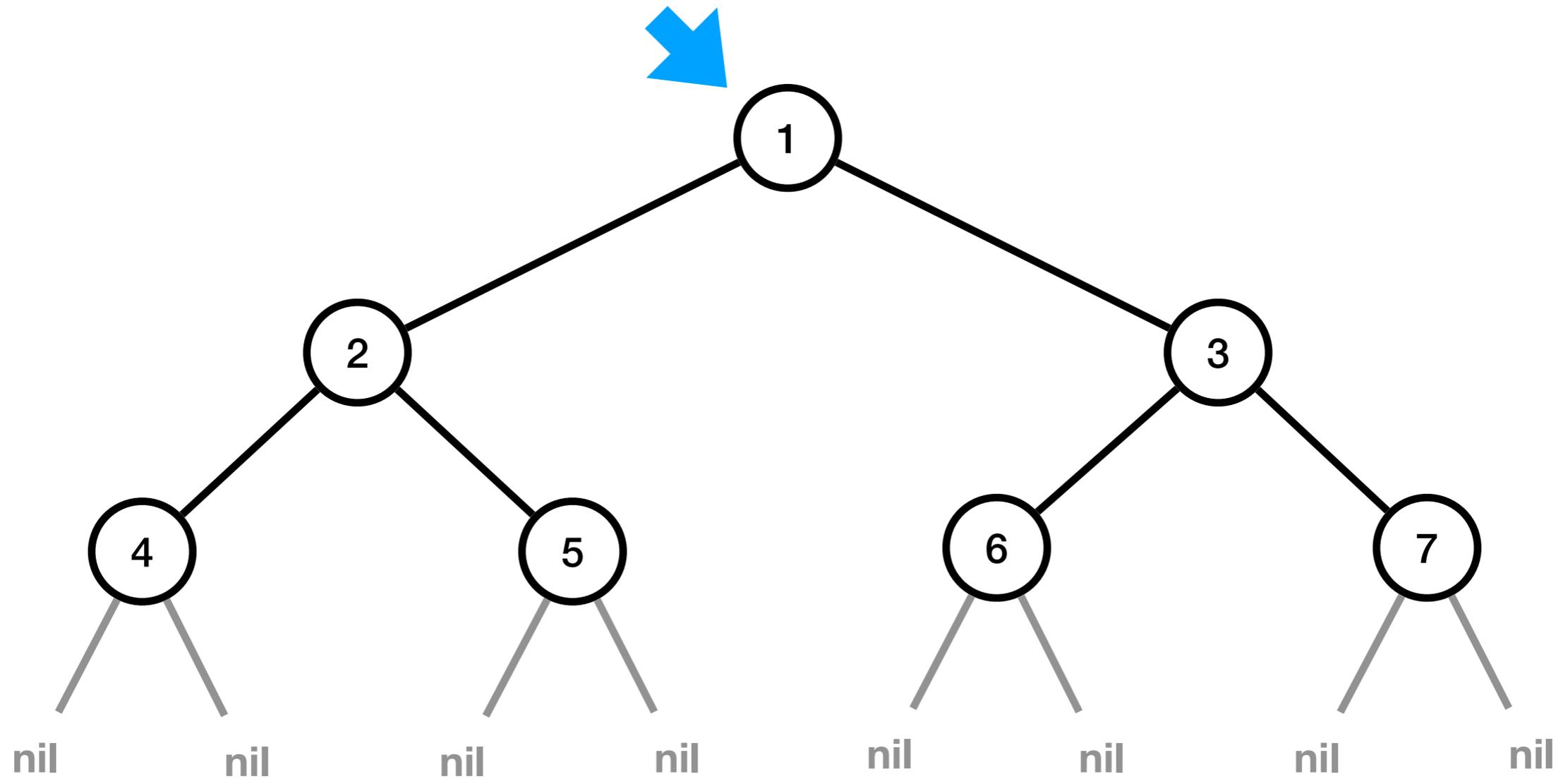
Parcours préfixe



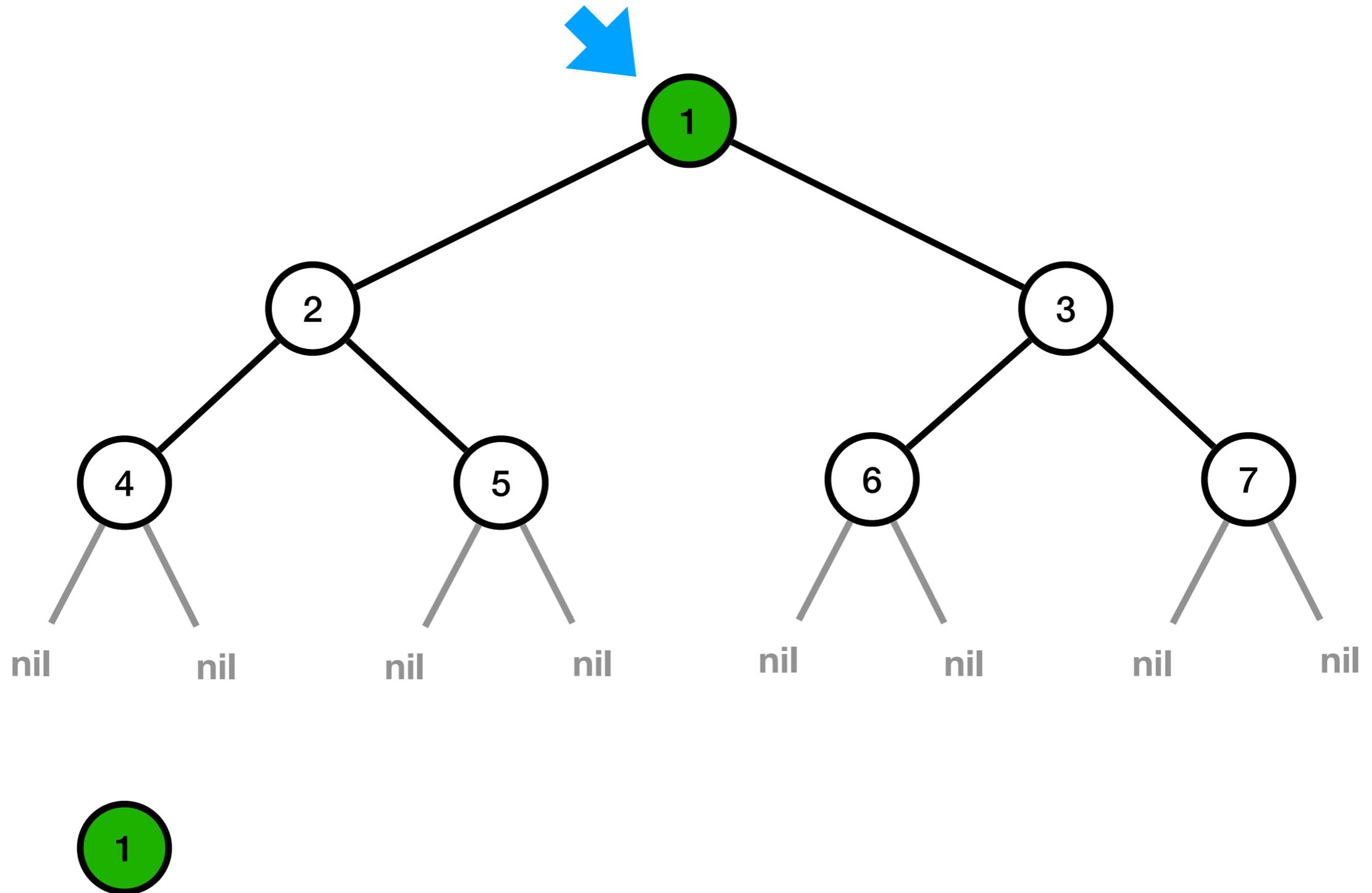
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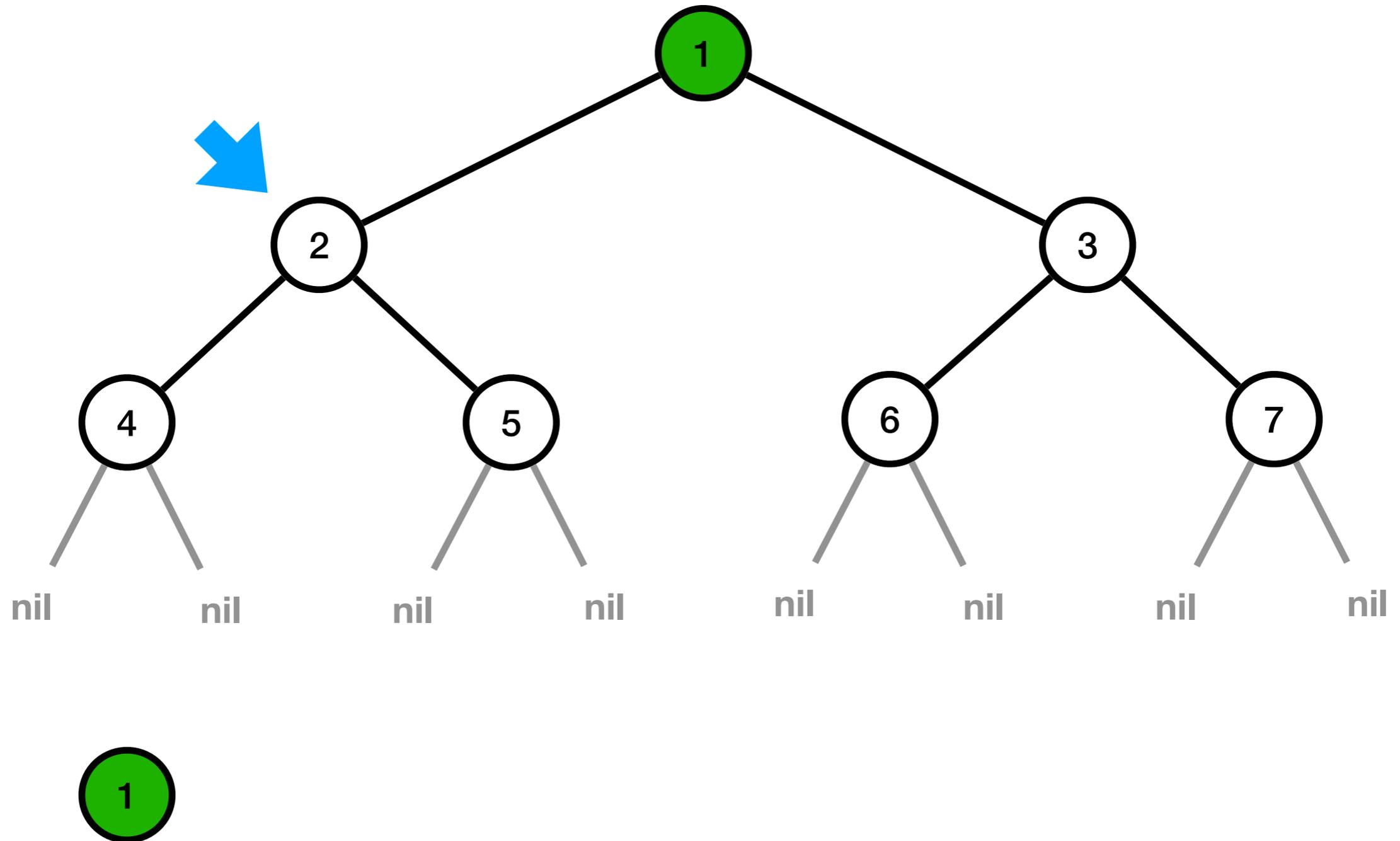
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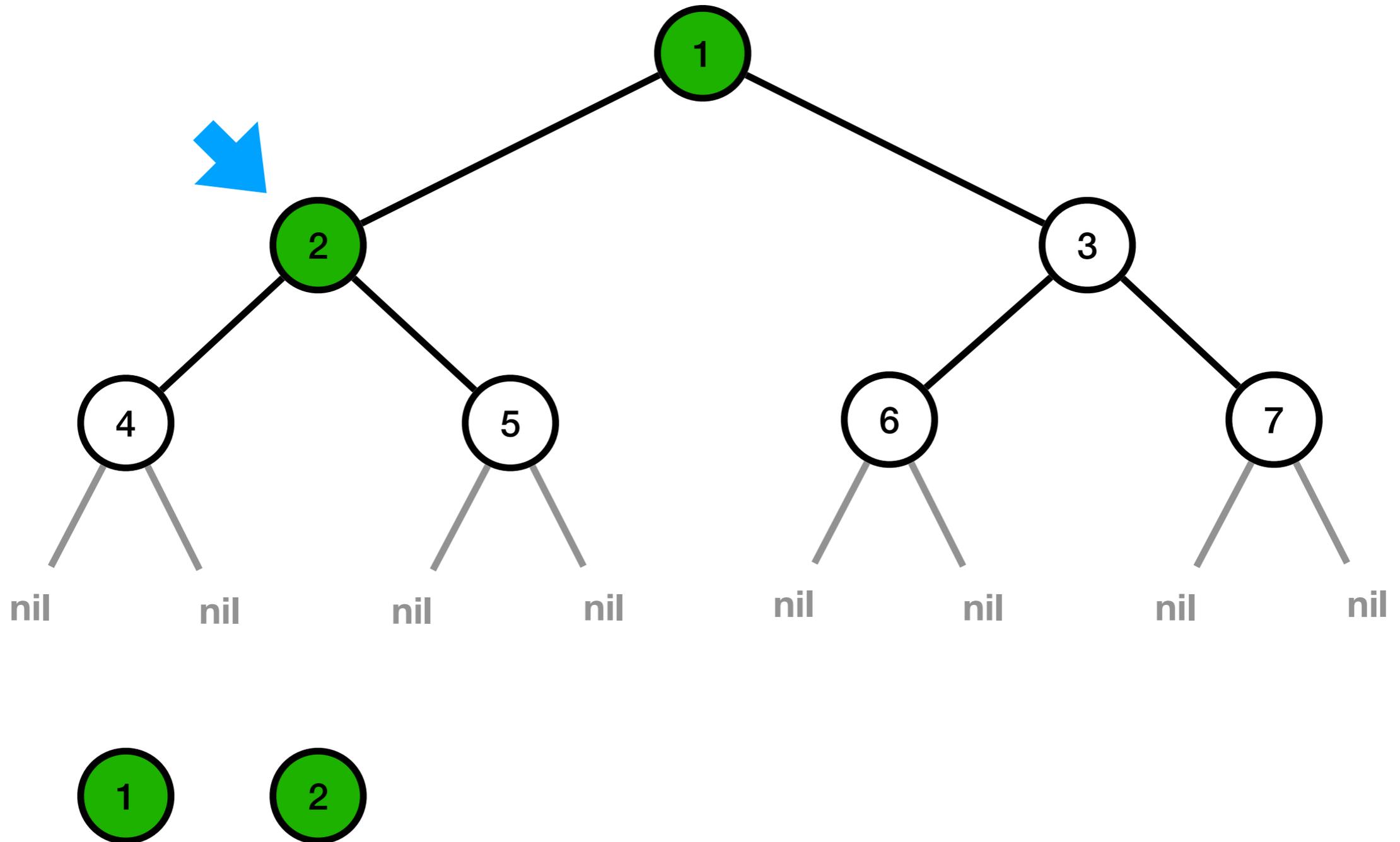
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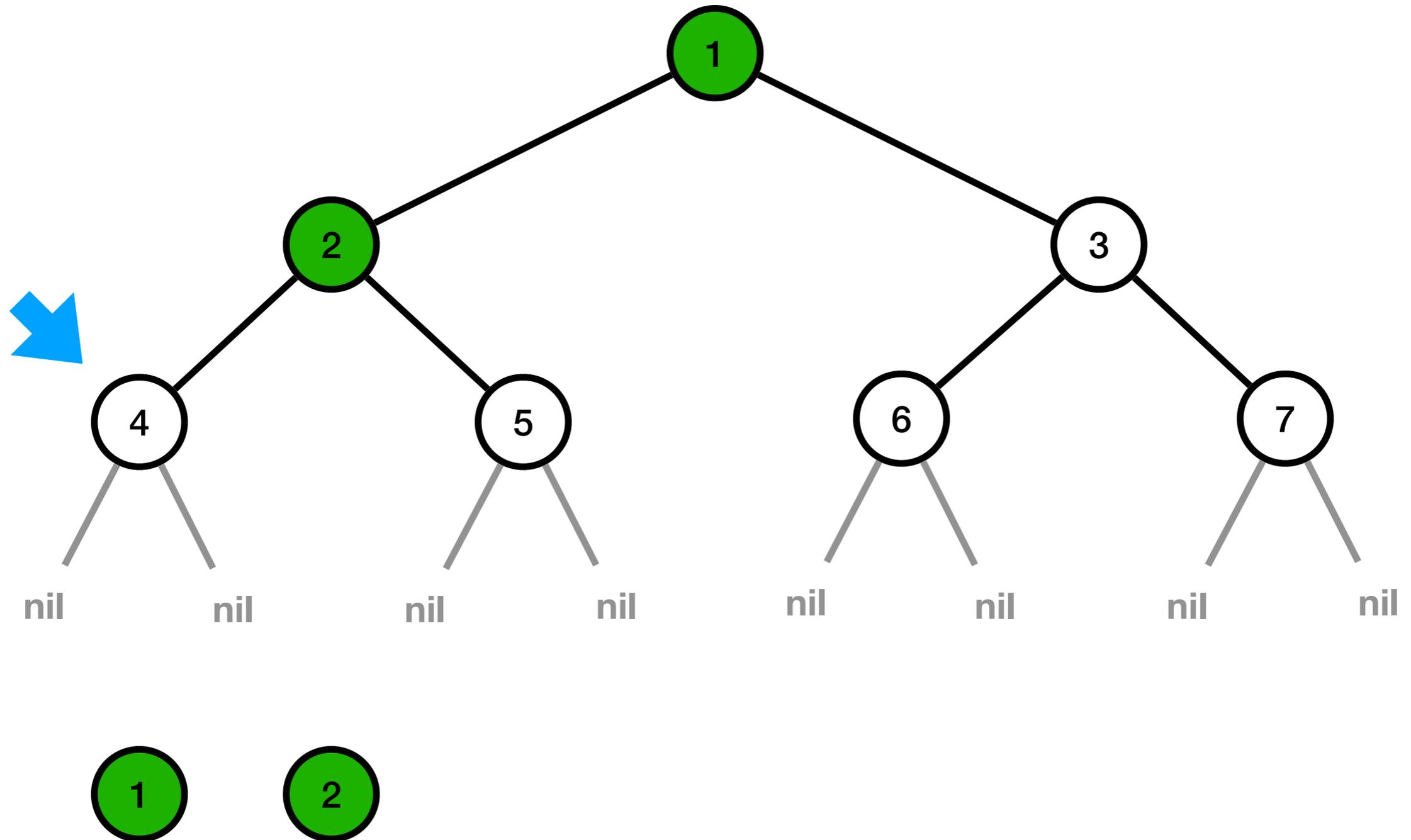
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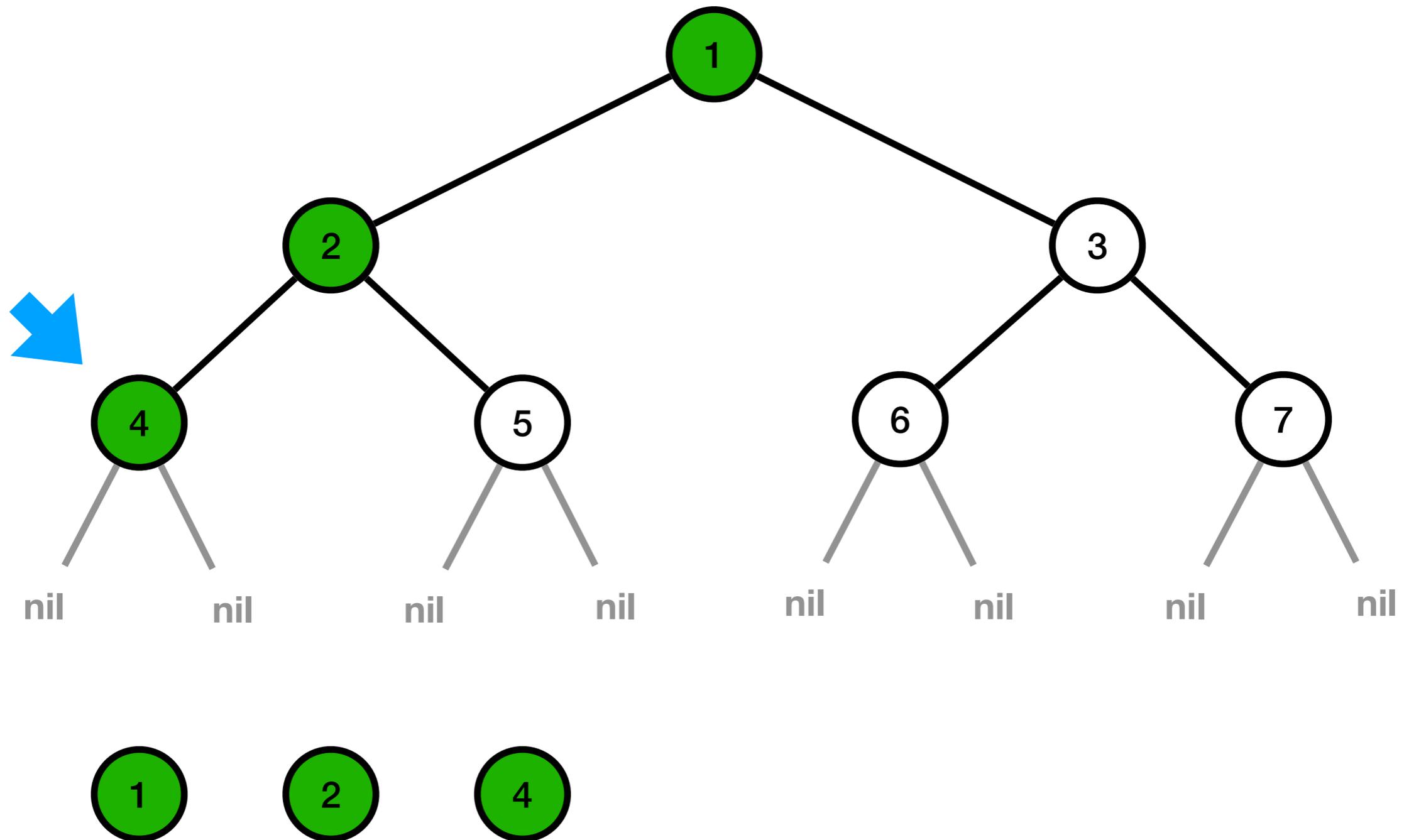
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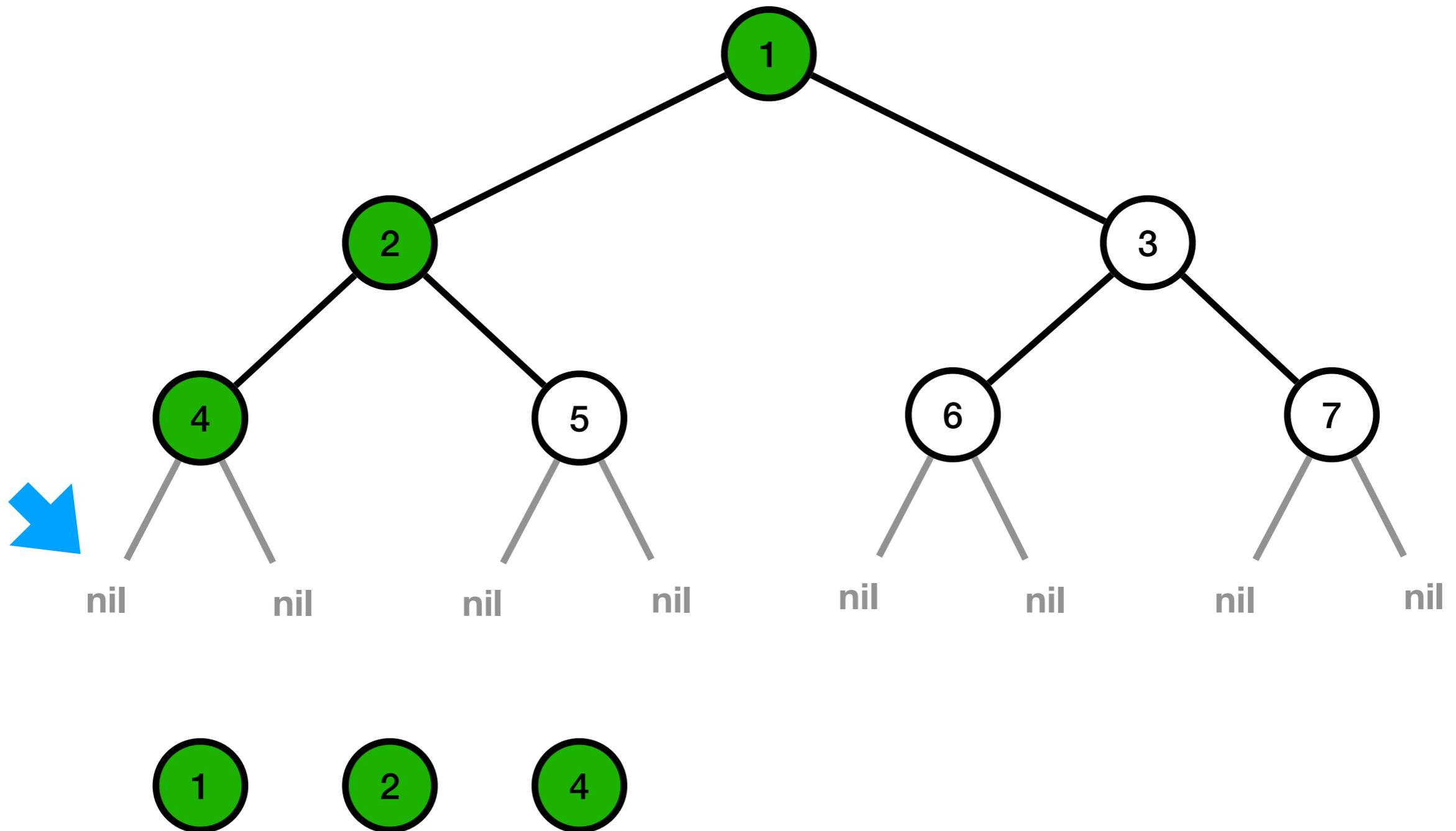
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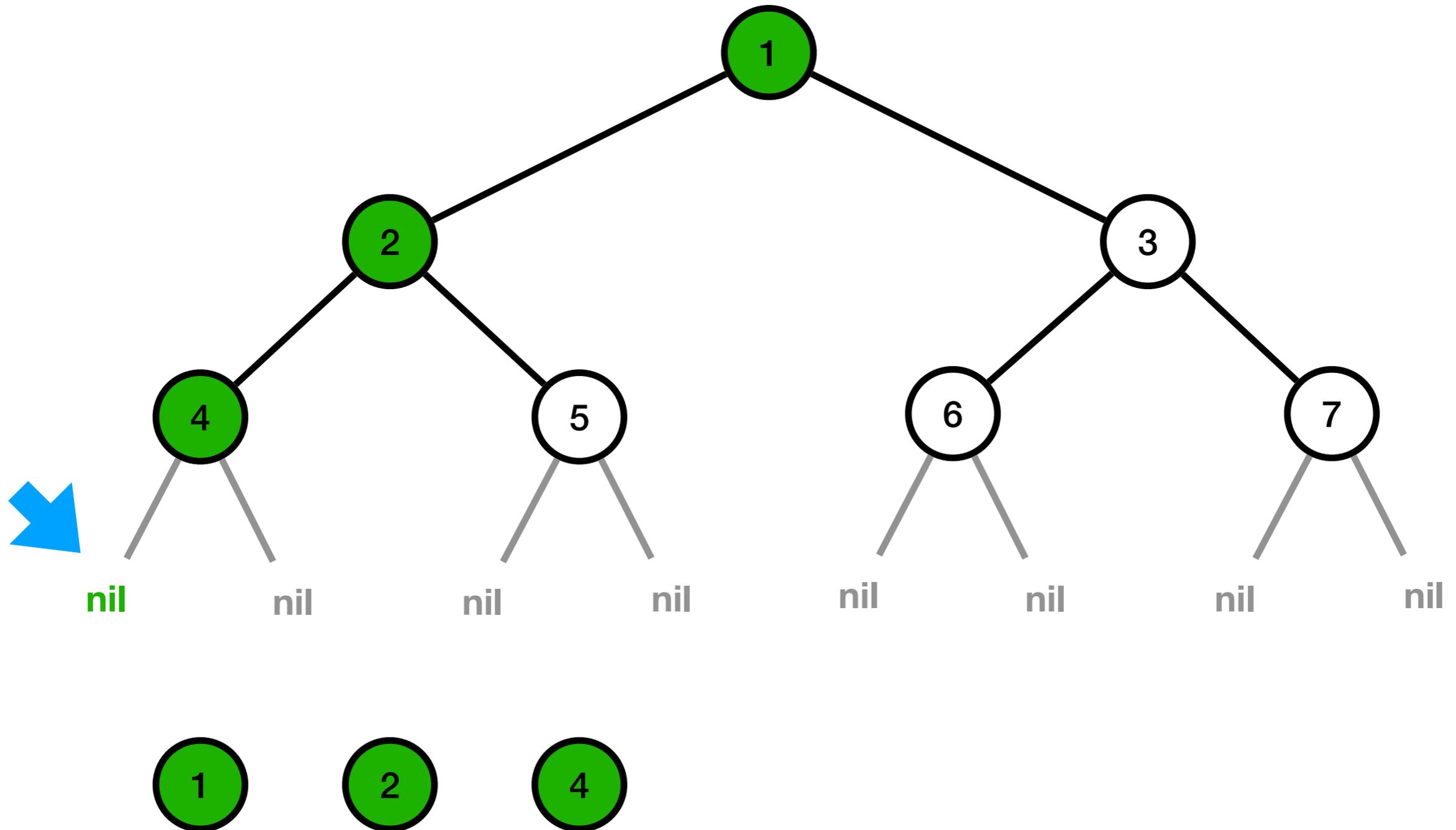
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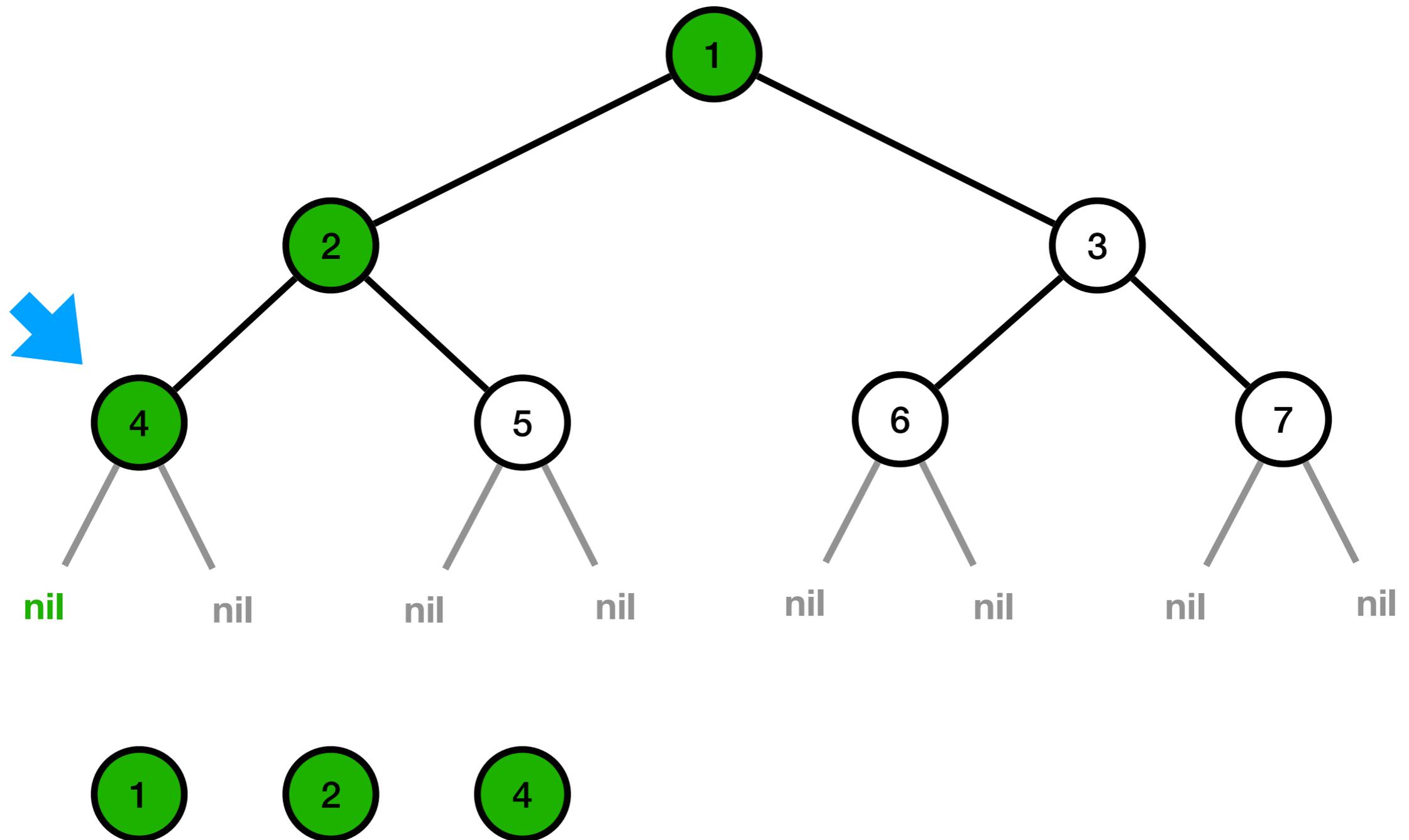
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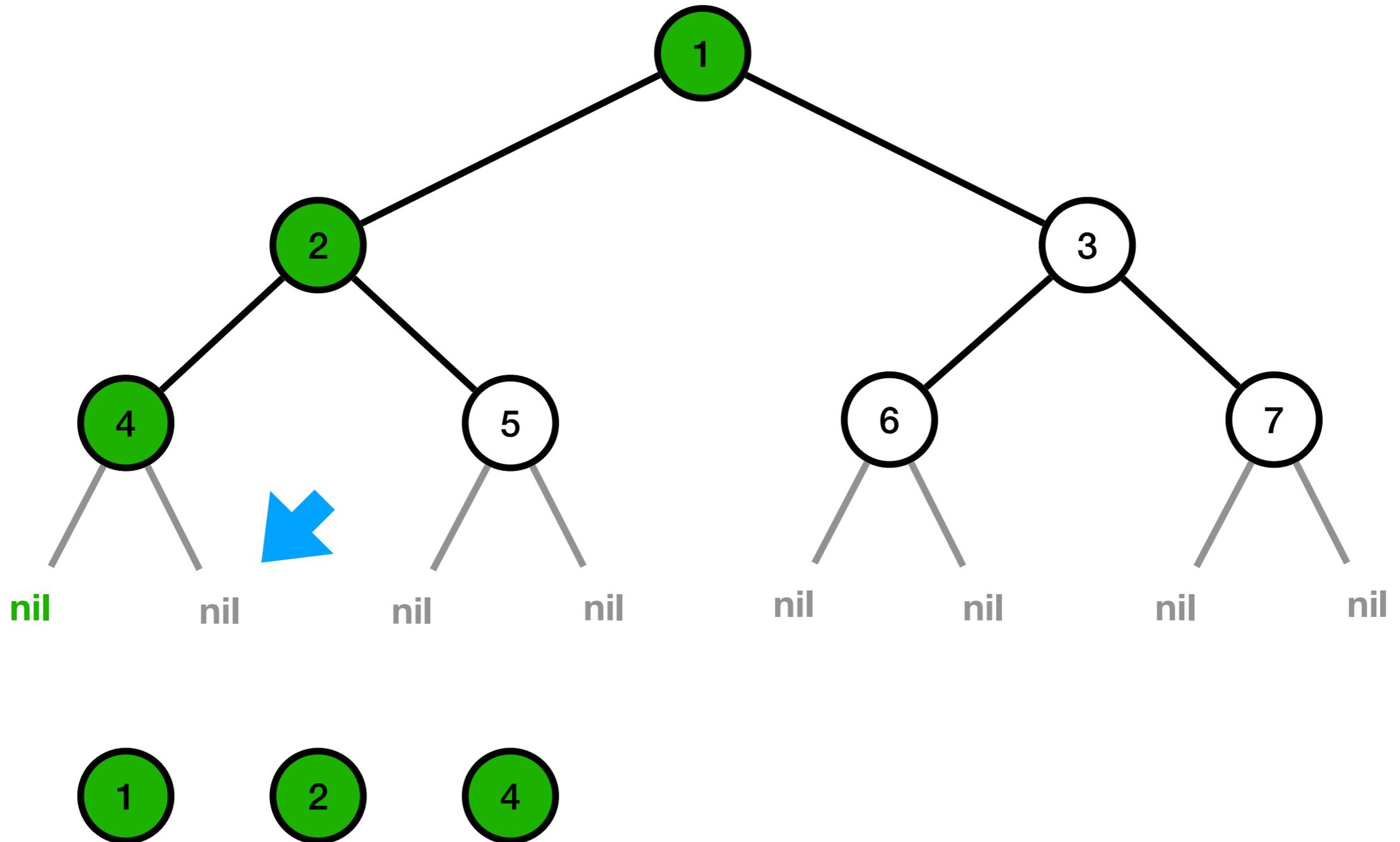
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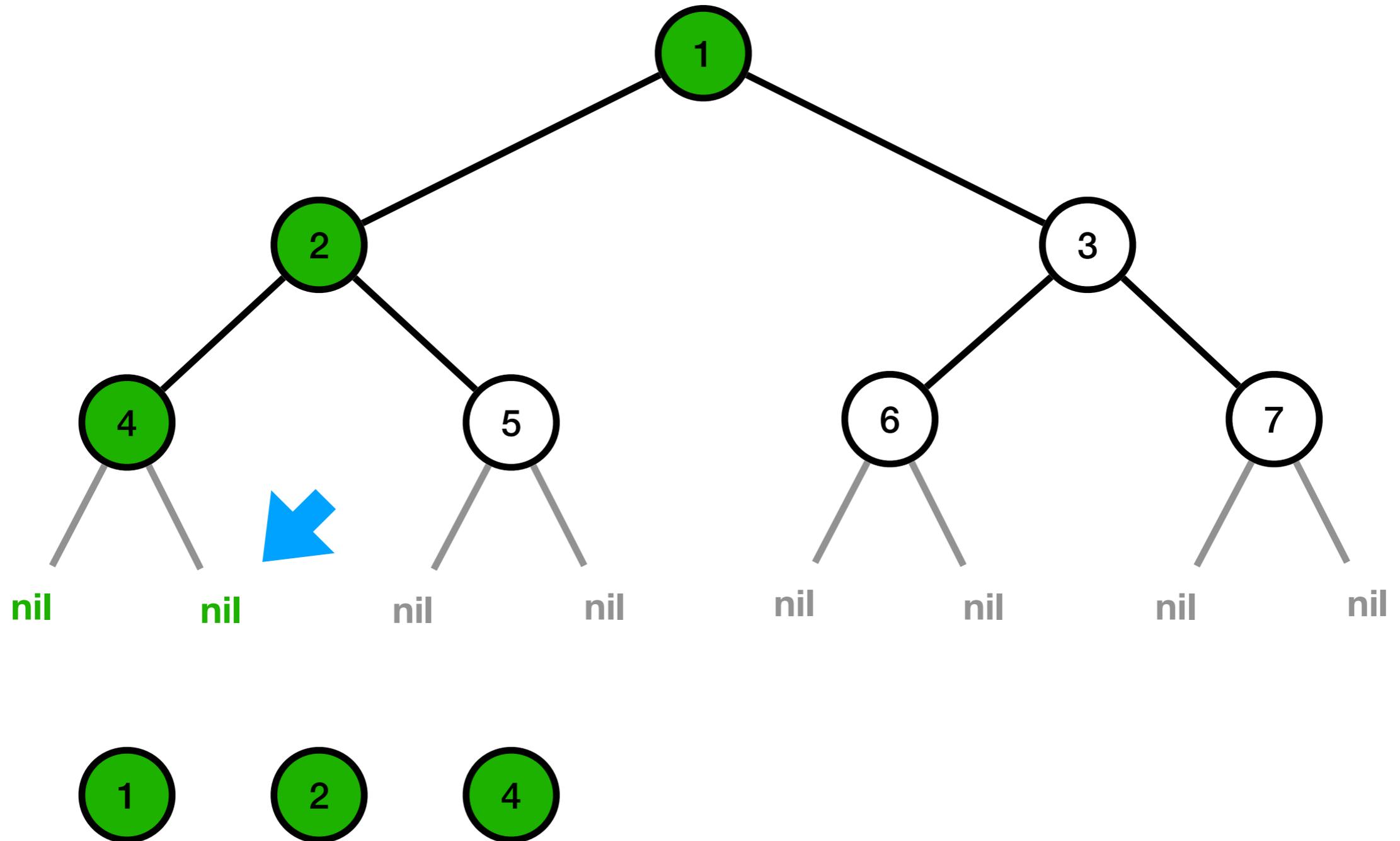
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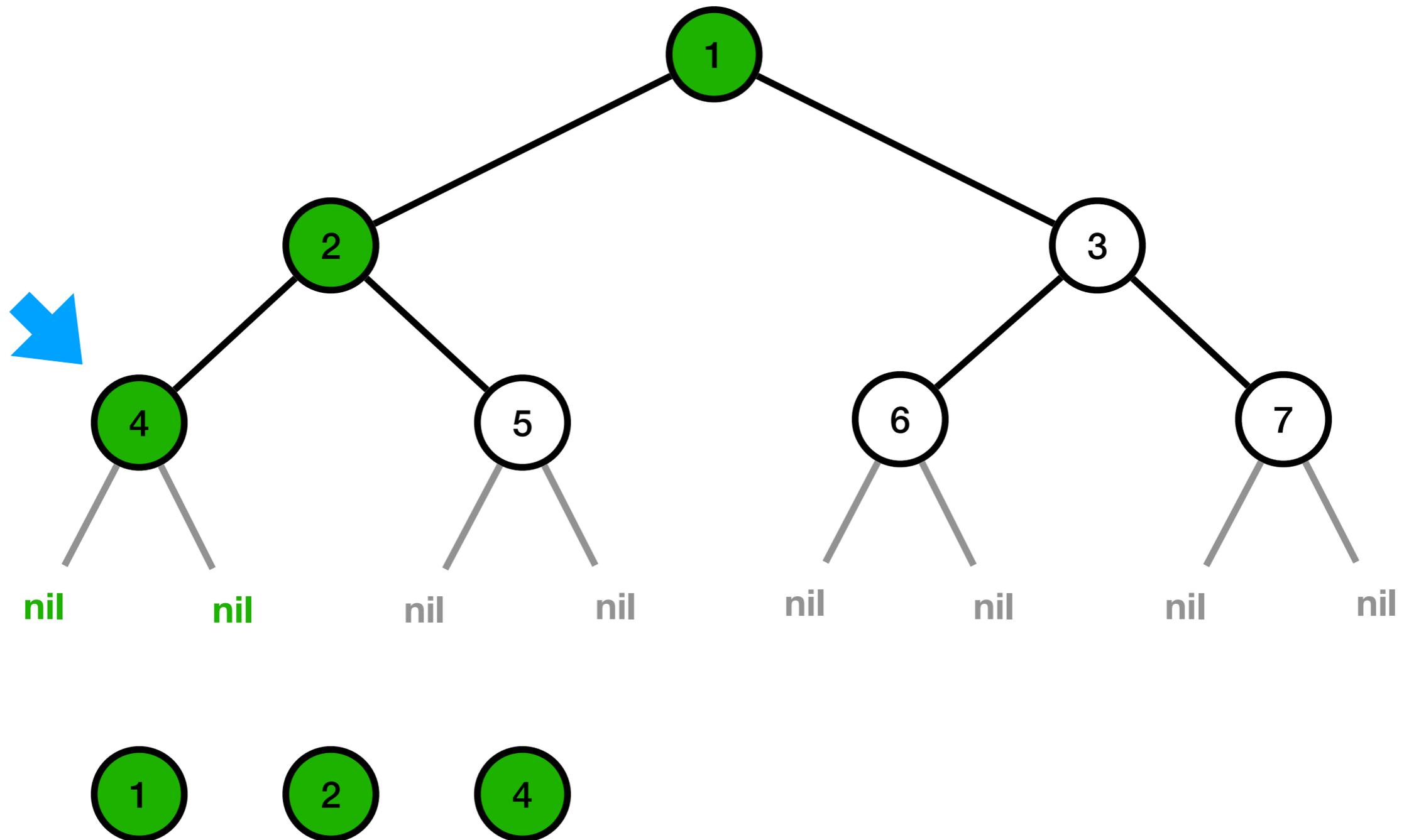
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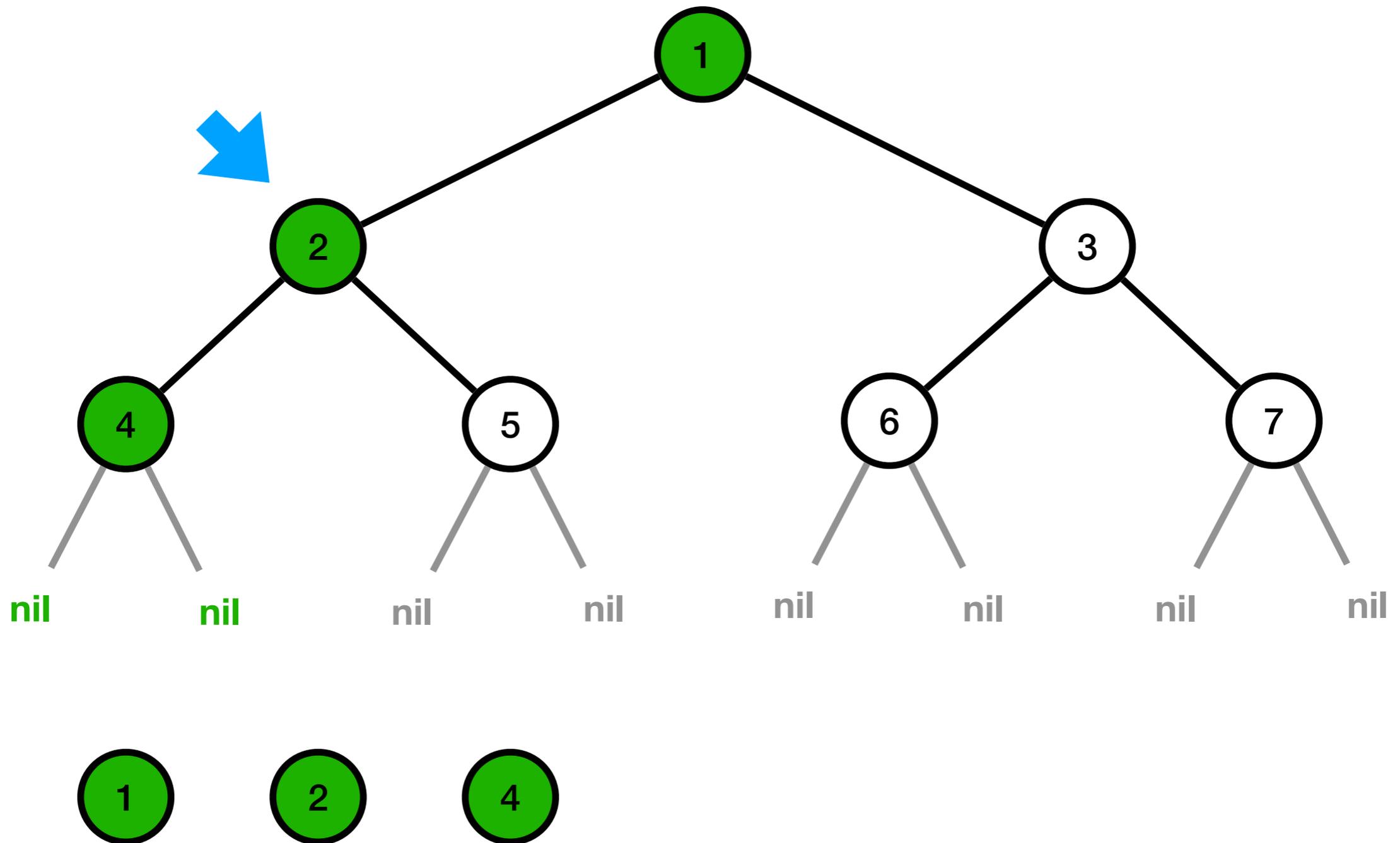
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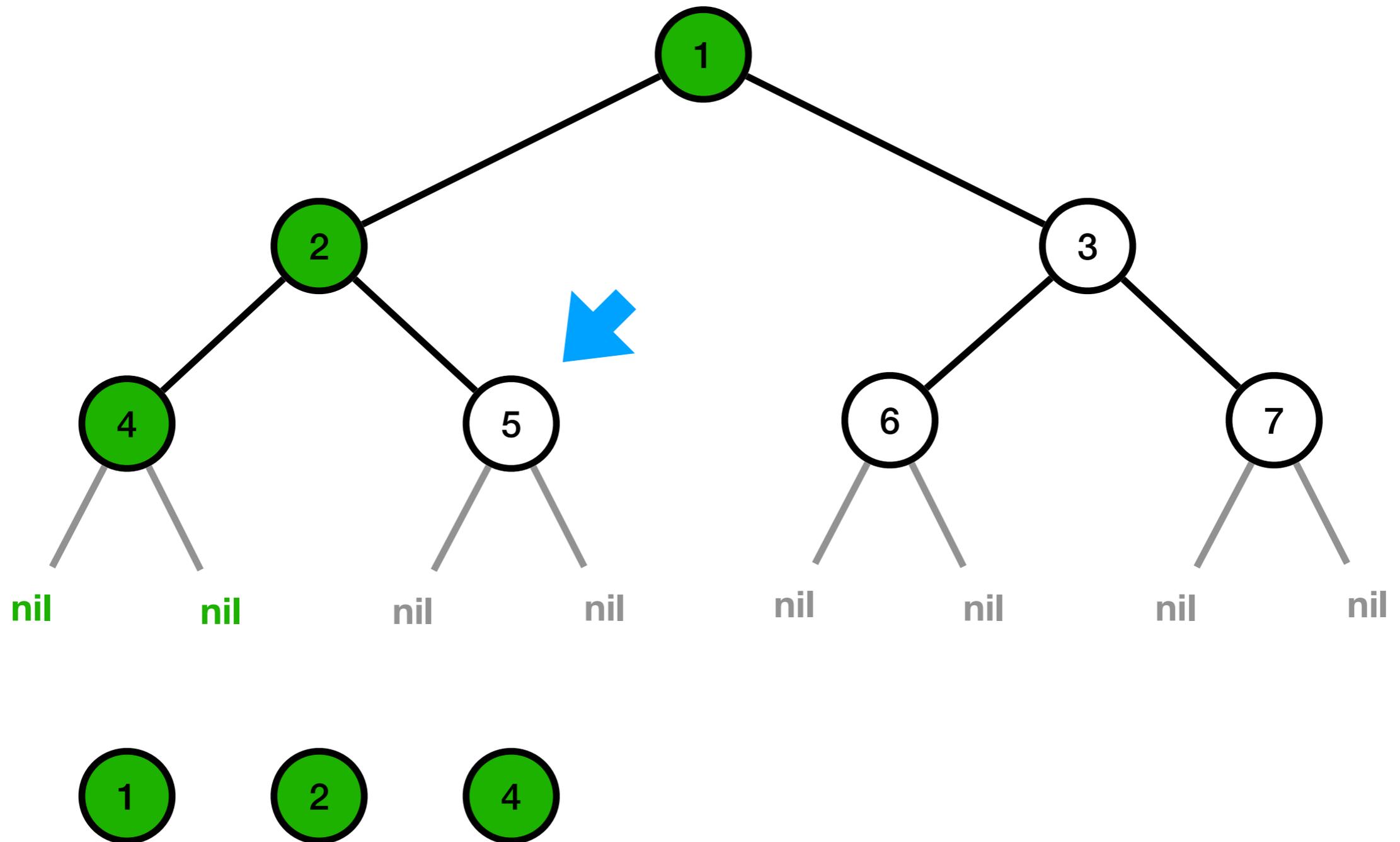
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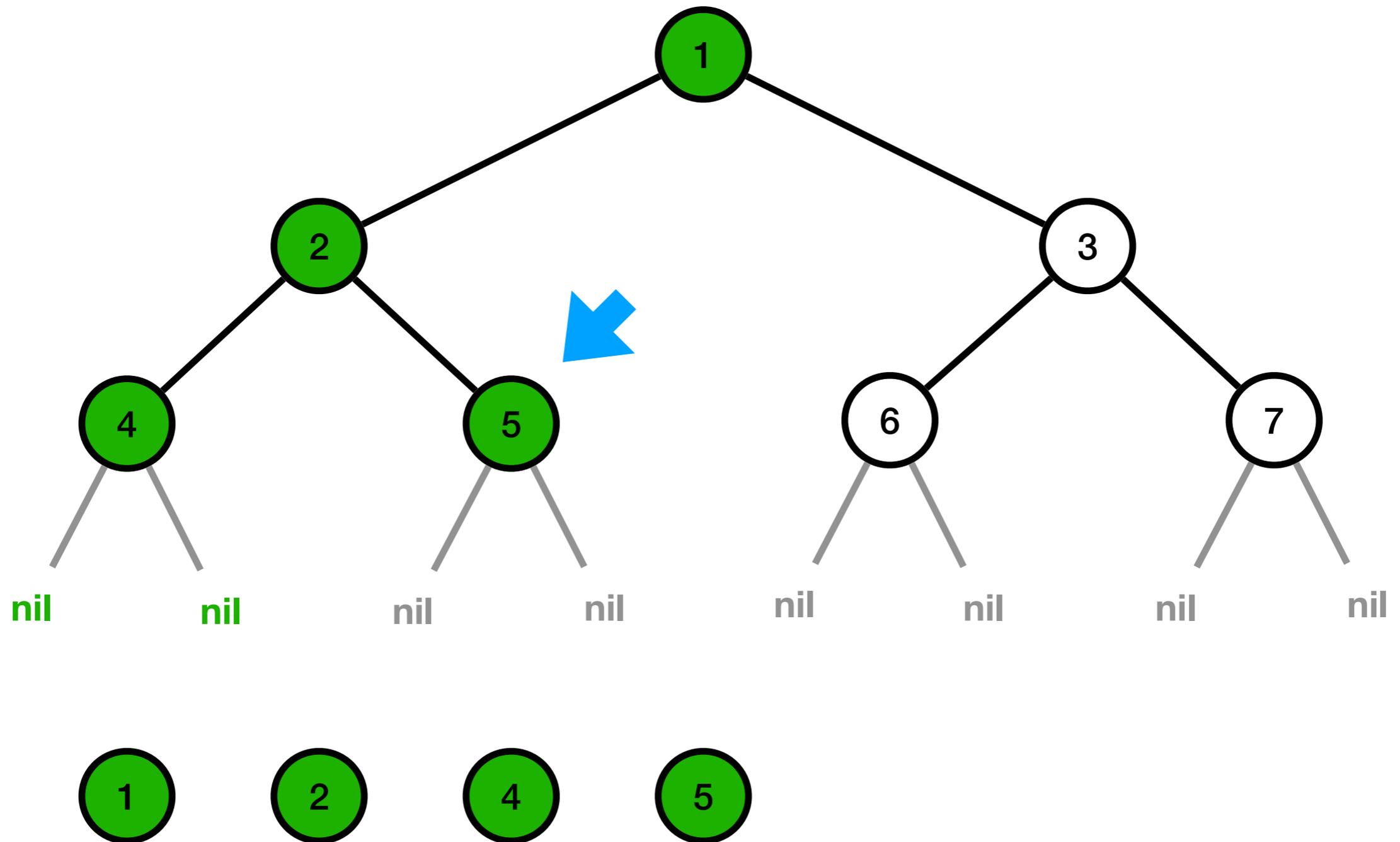
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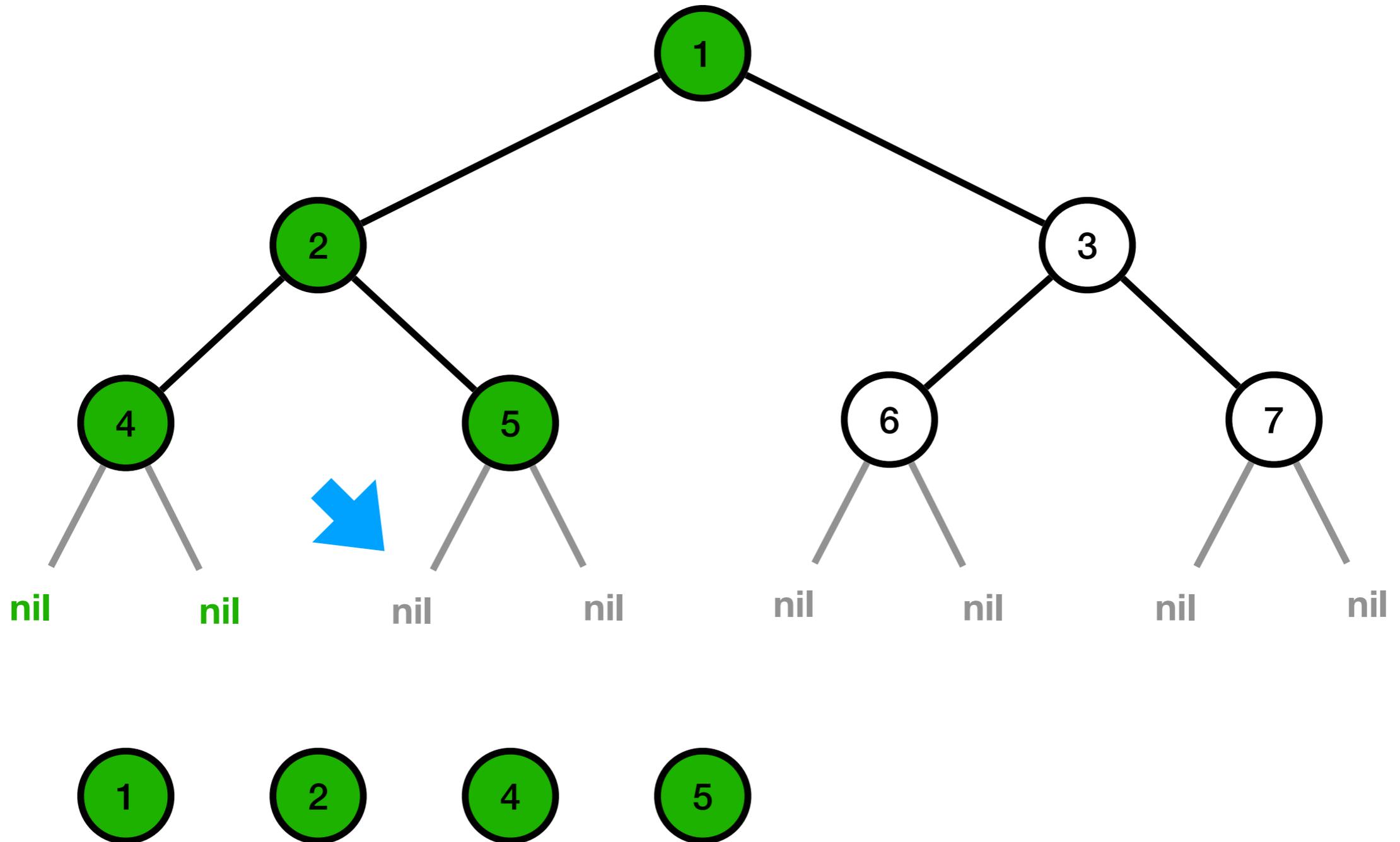
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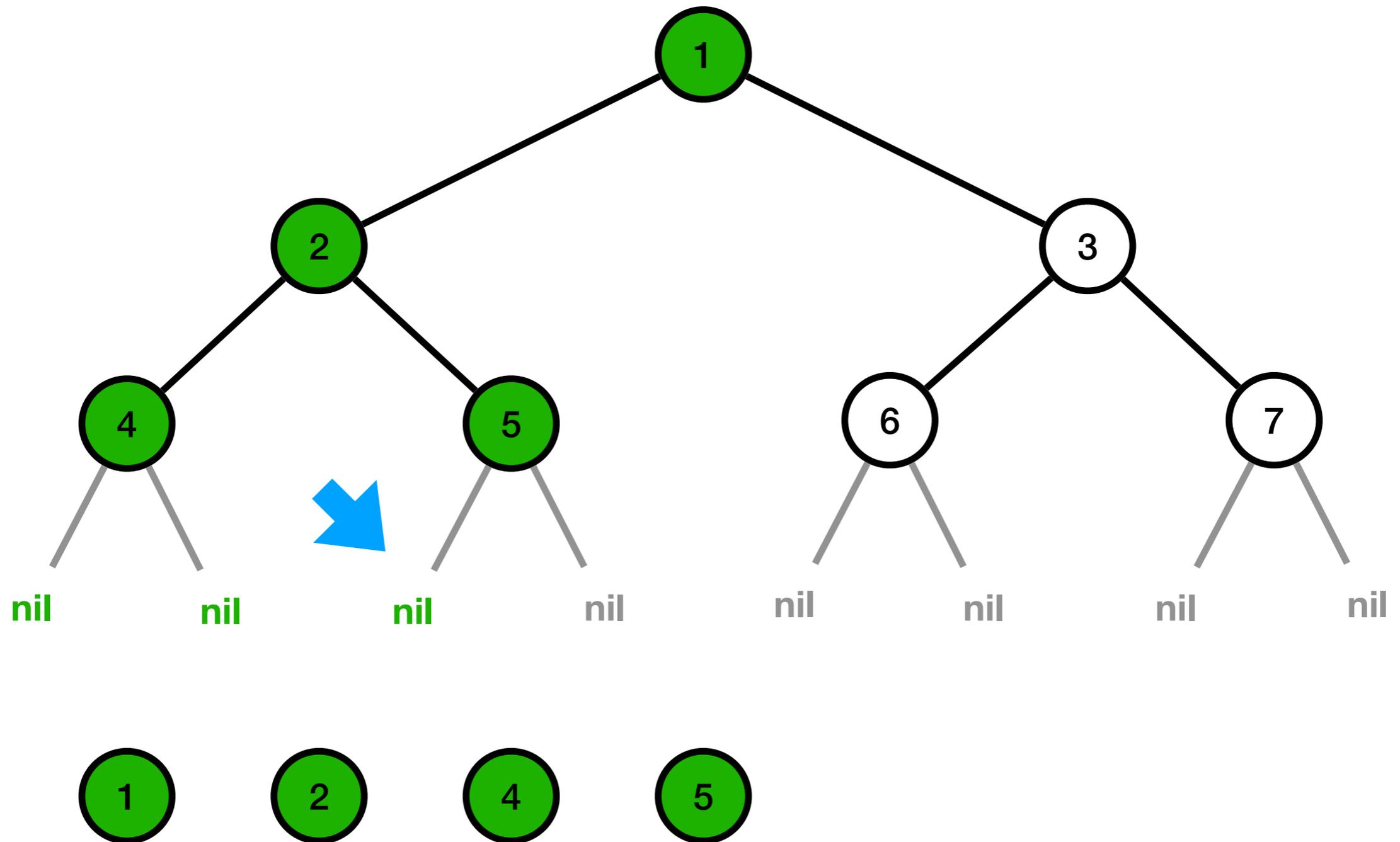
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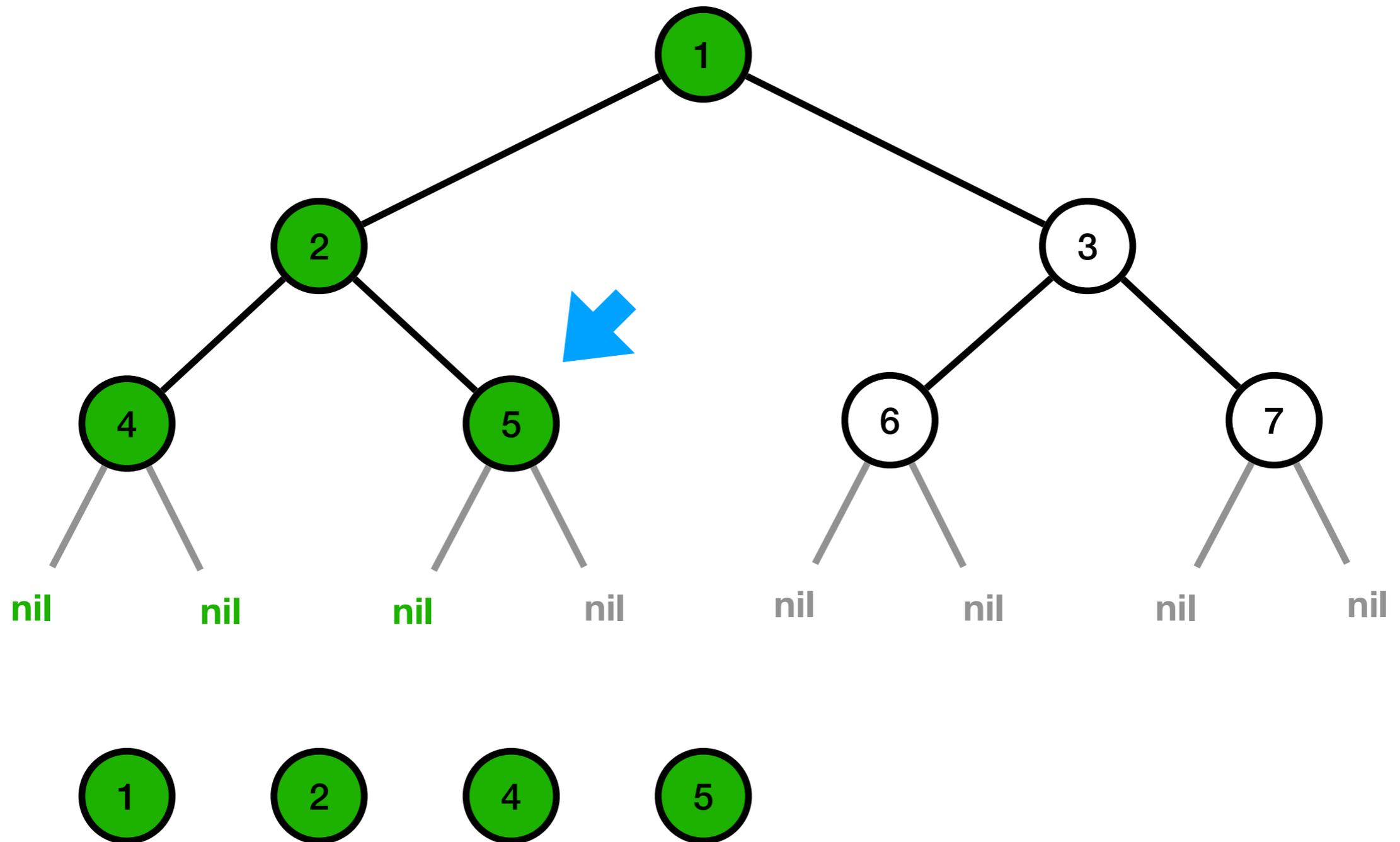
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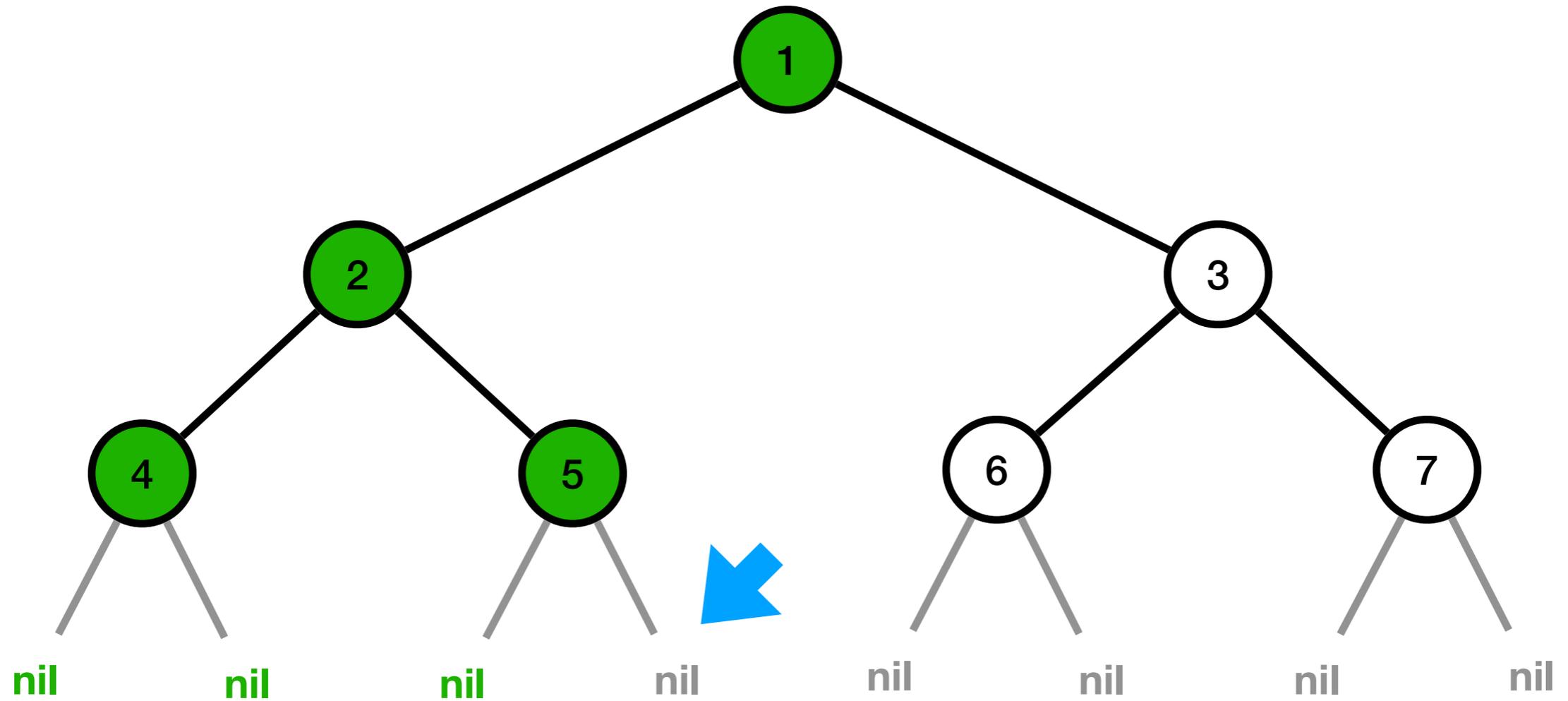
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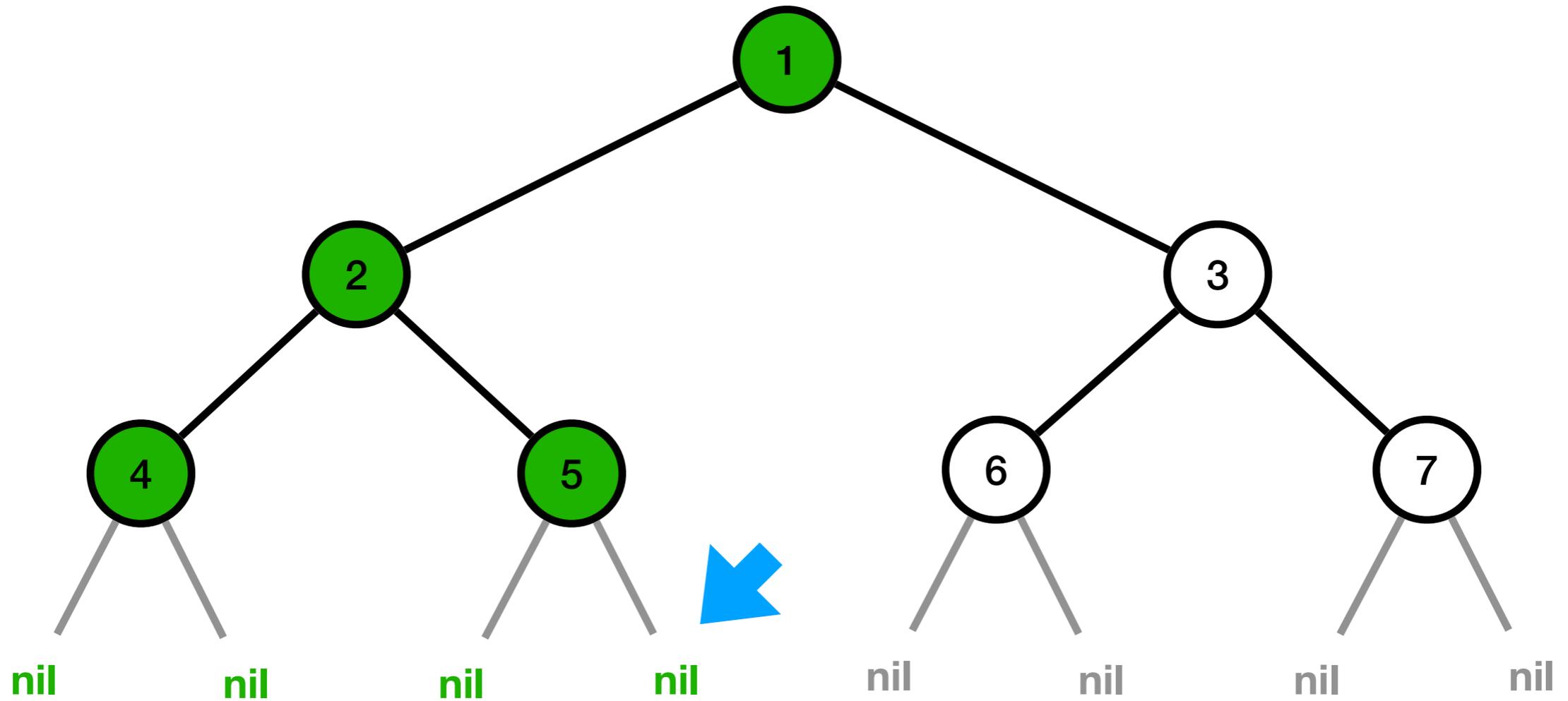
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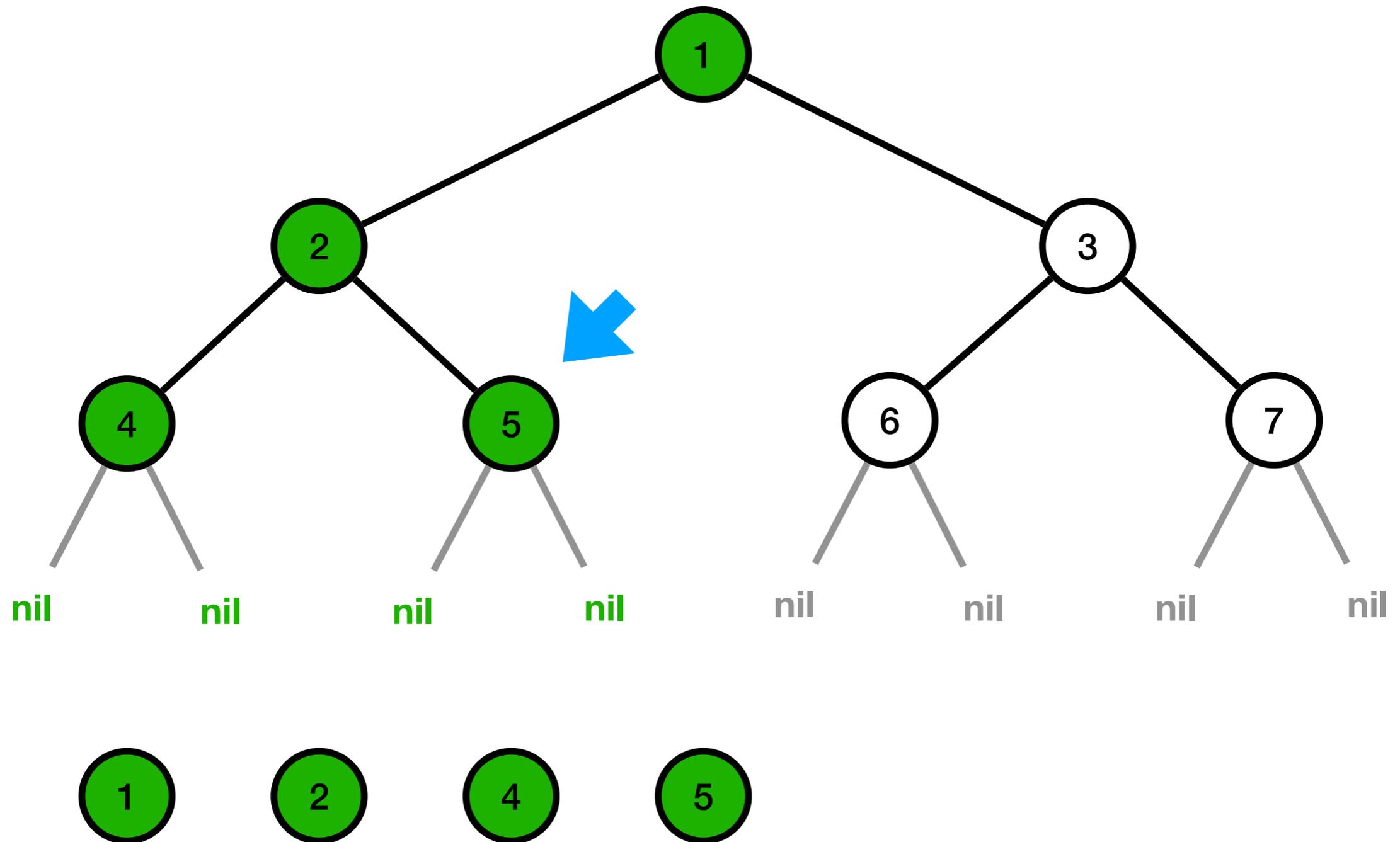
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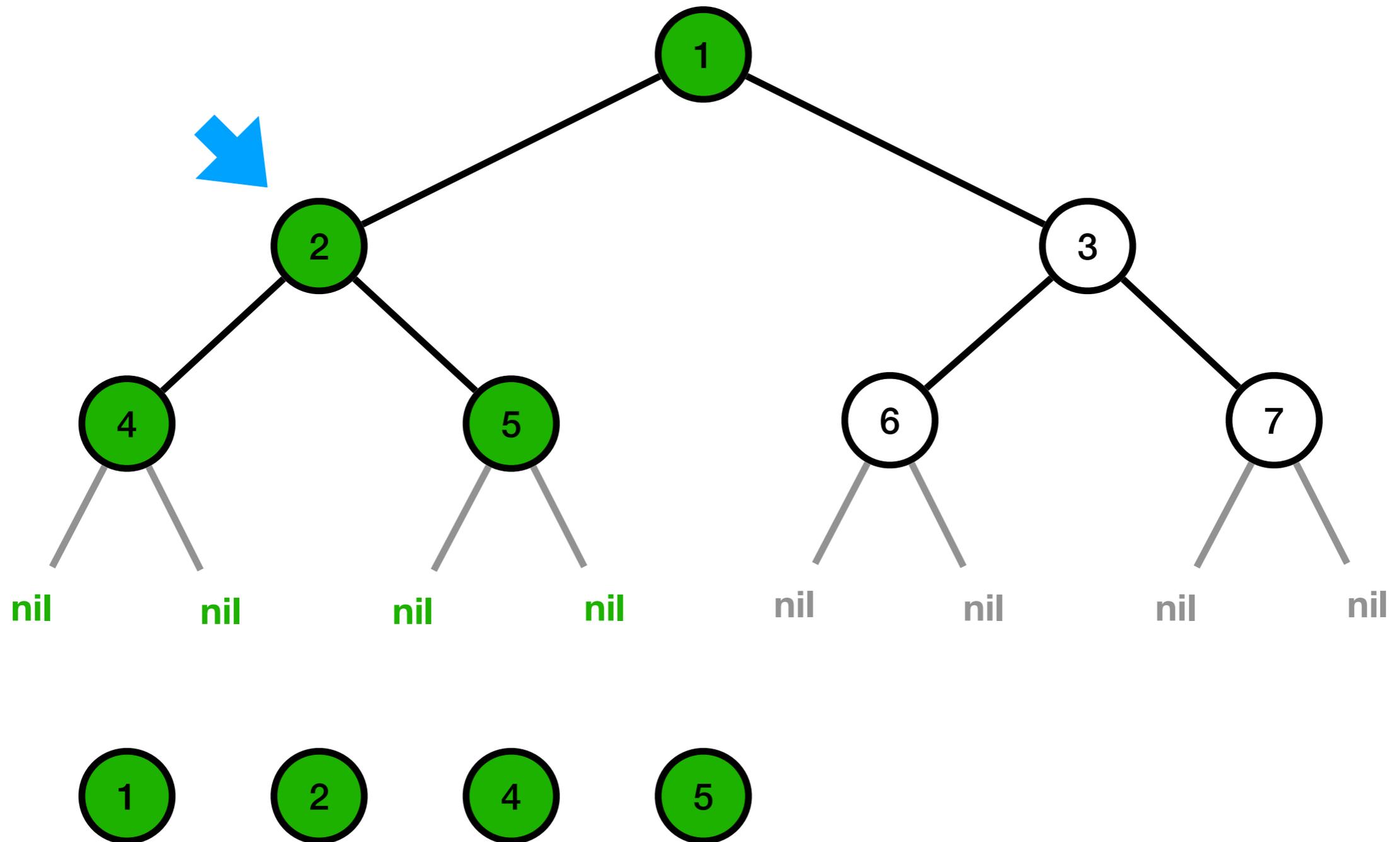
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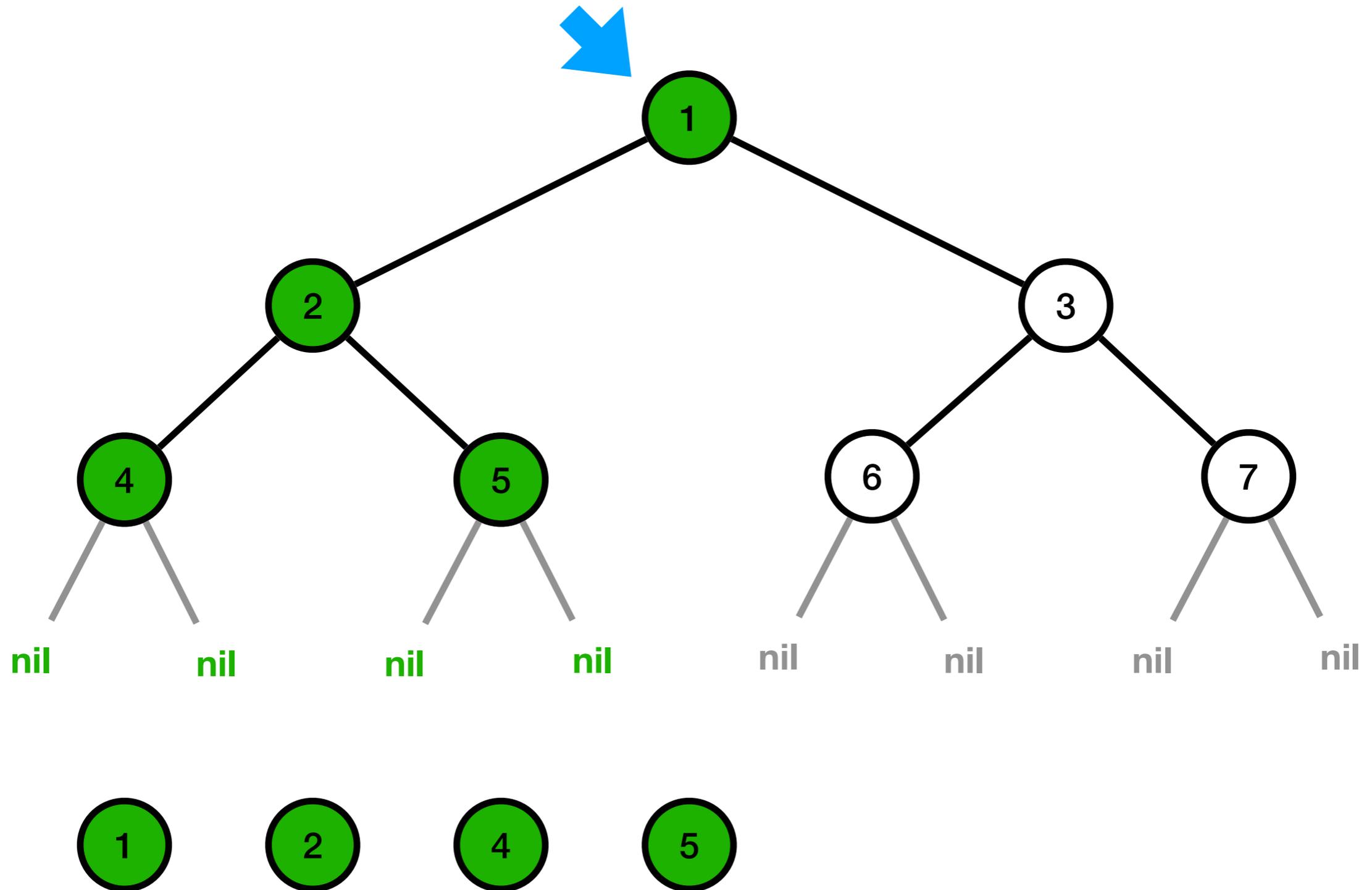
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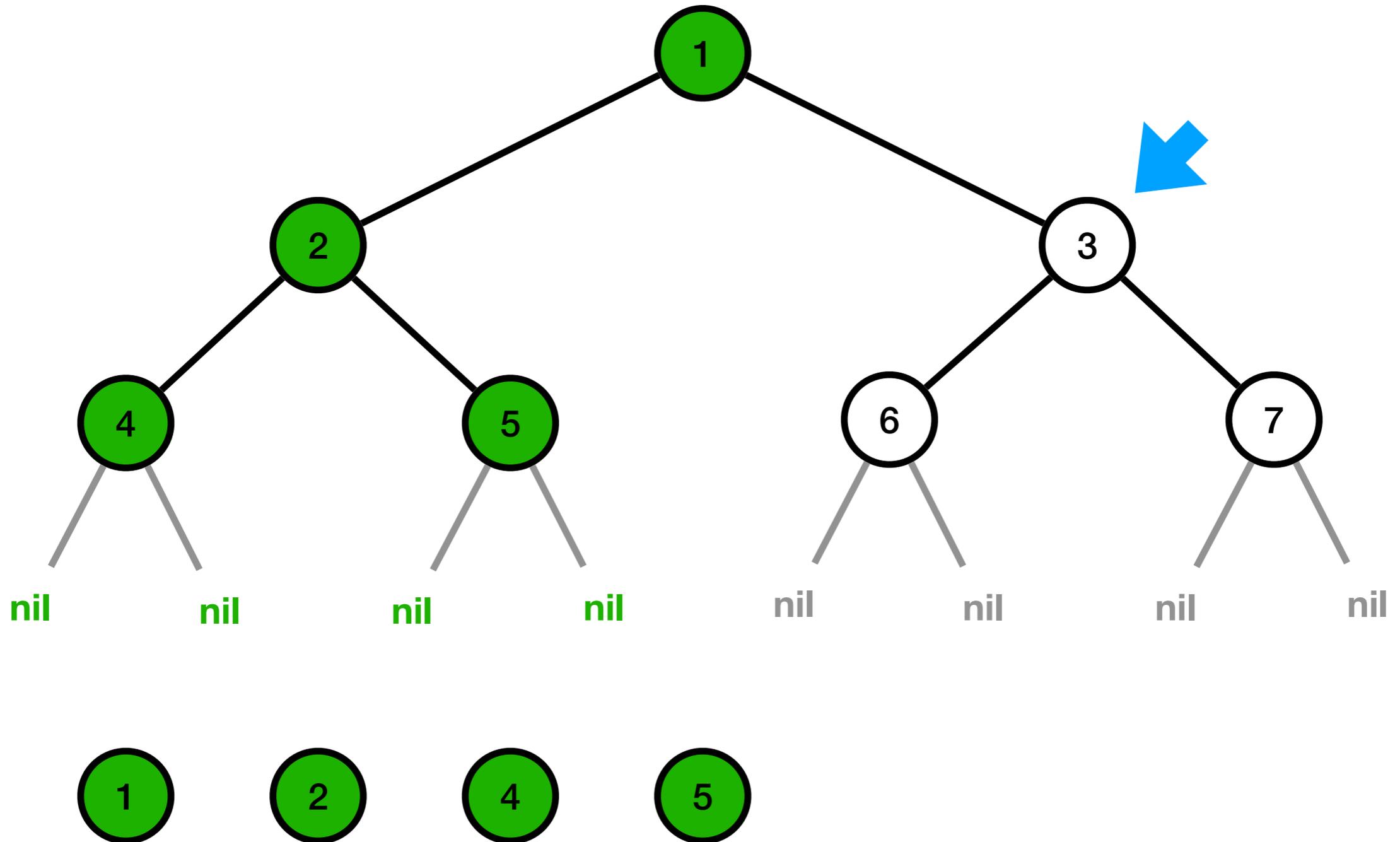
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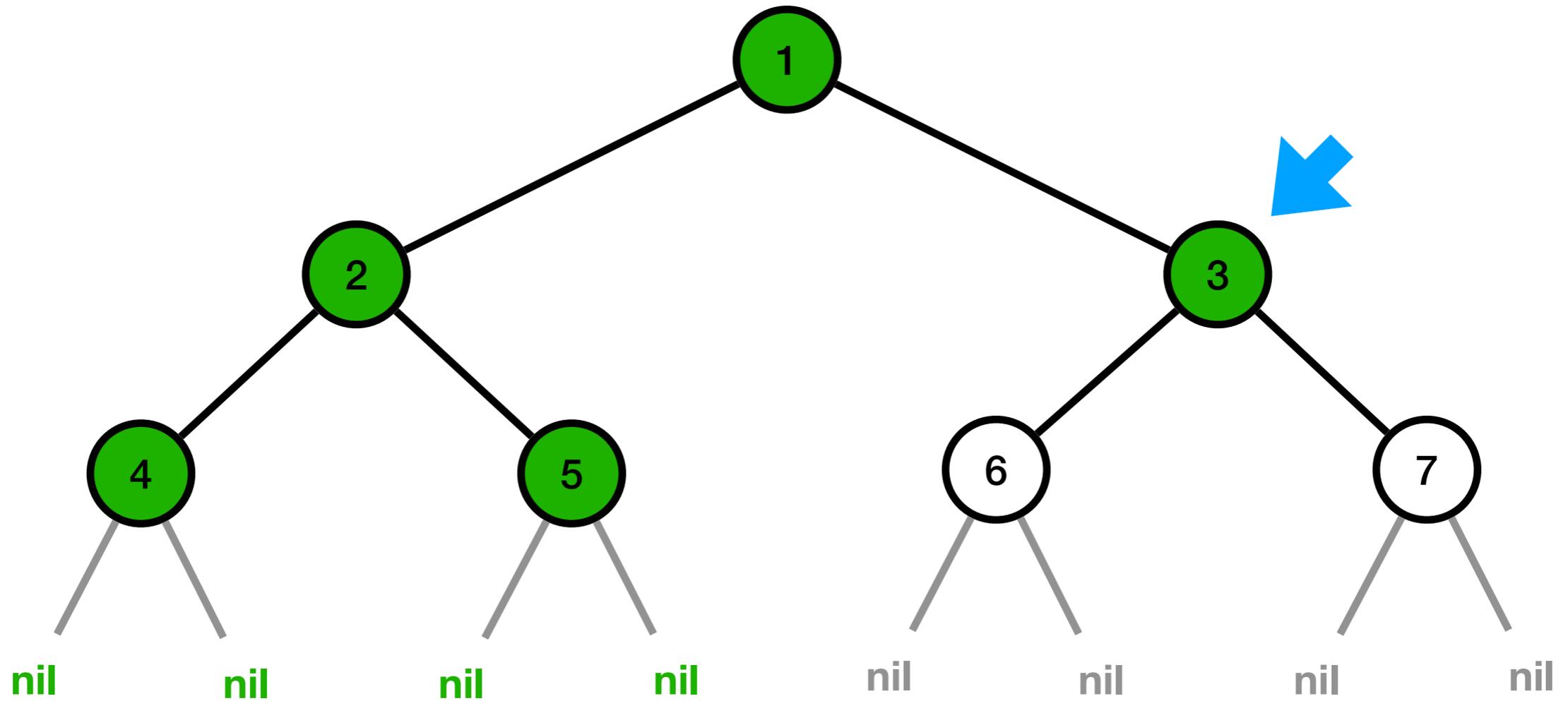
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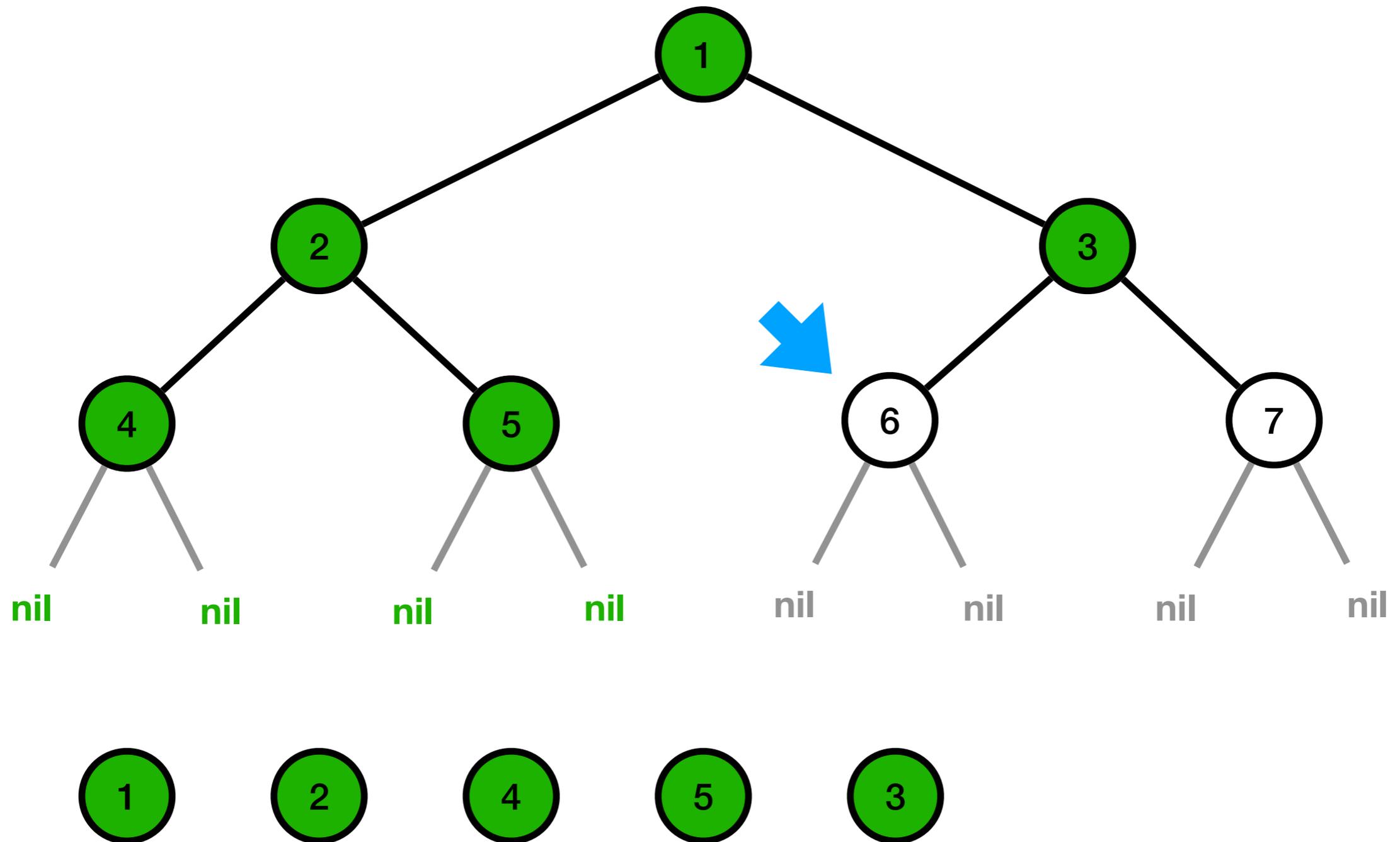
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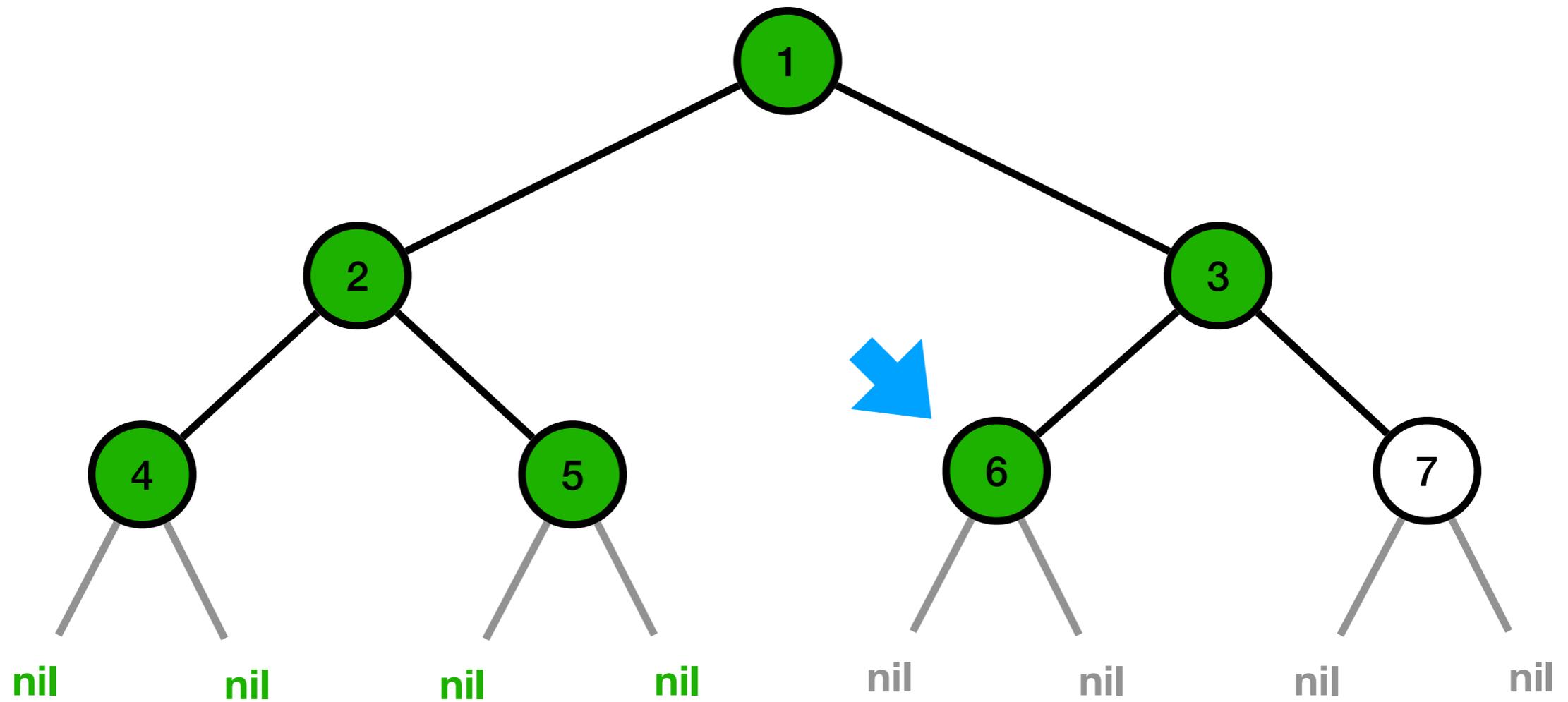
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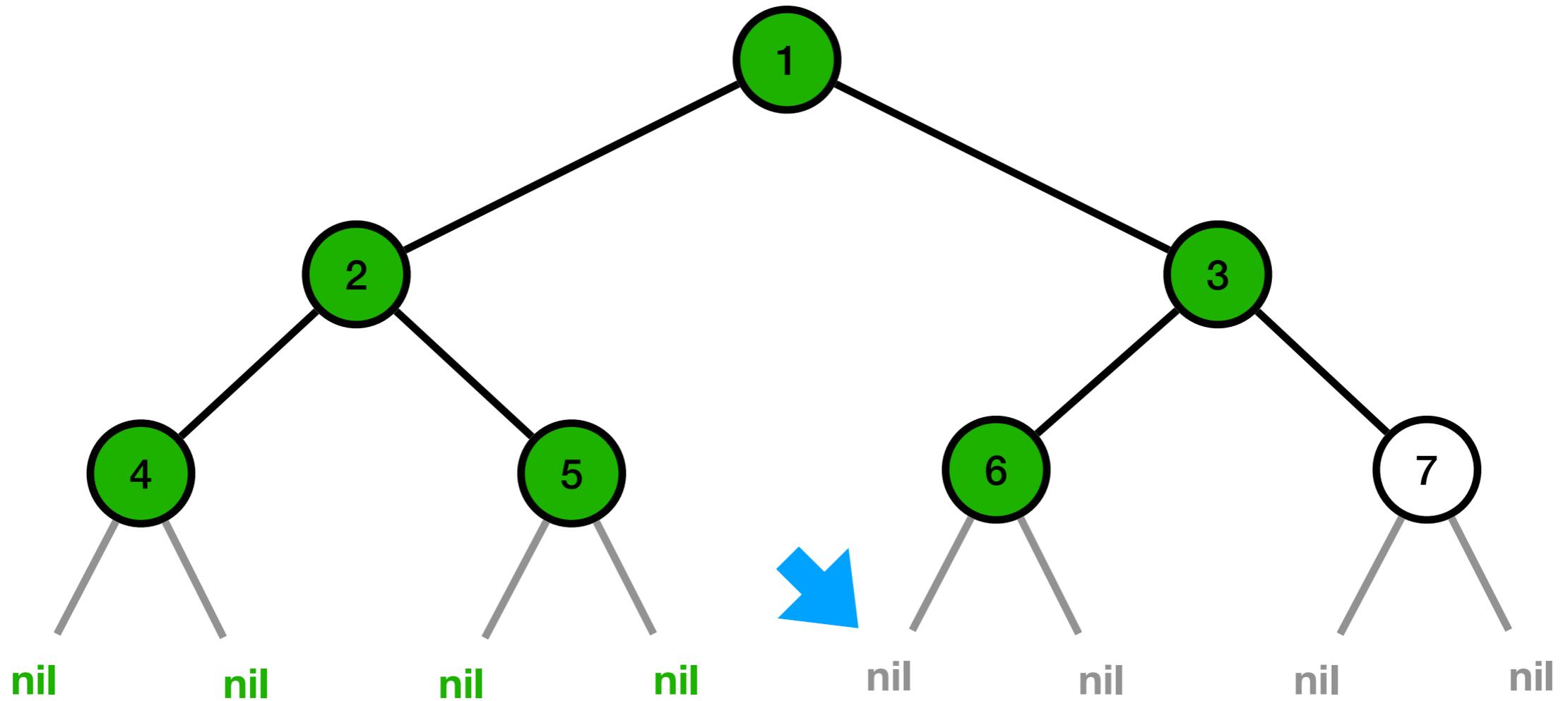
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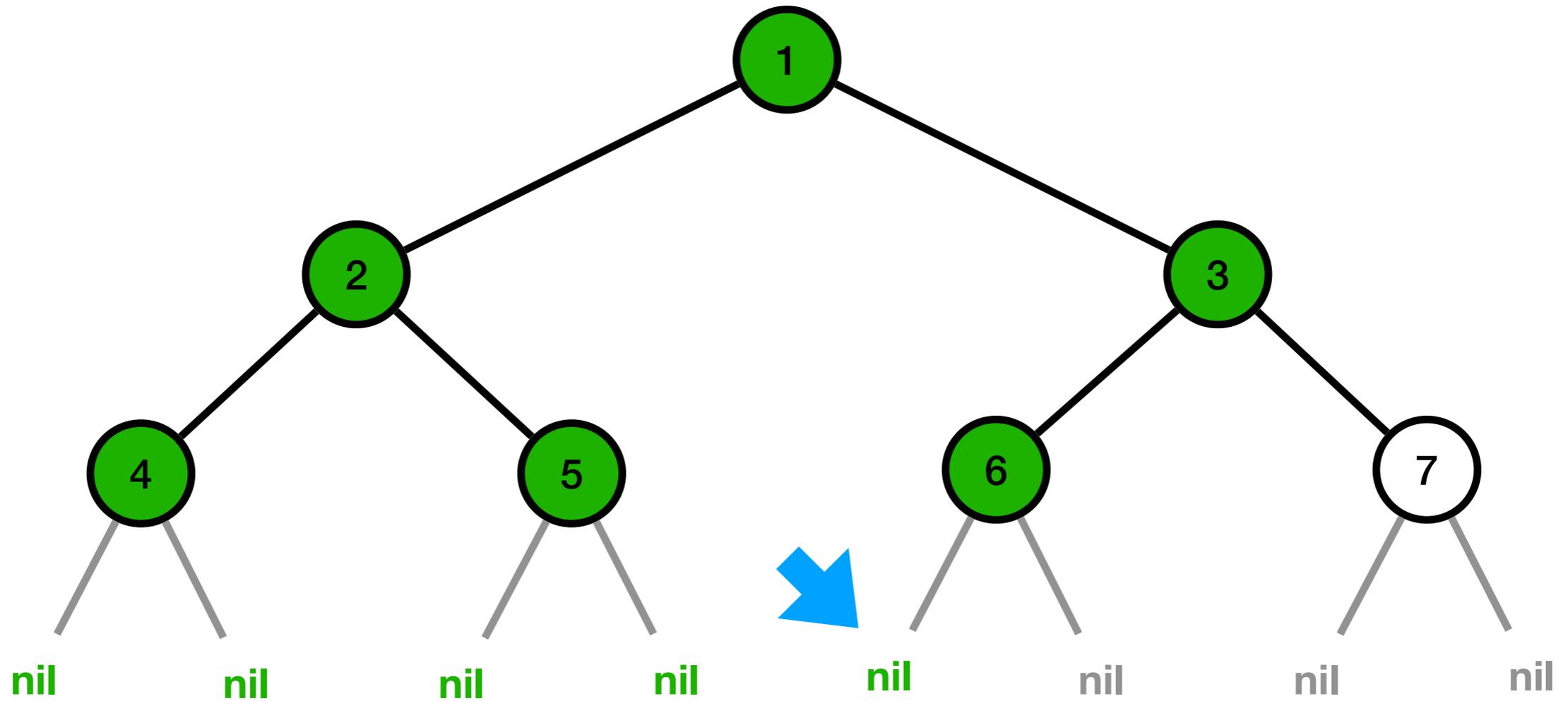
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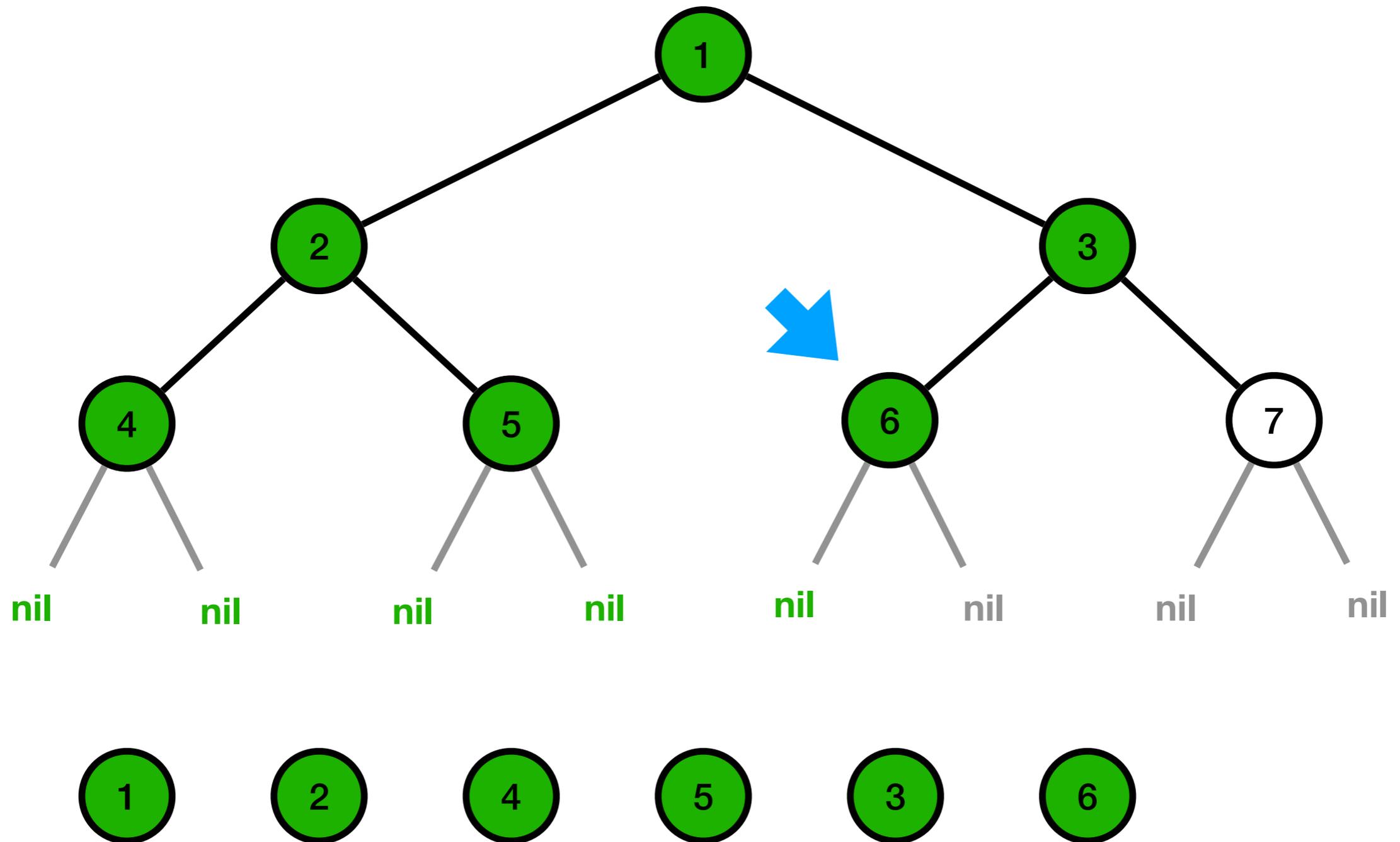
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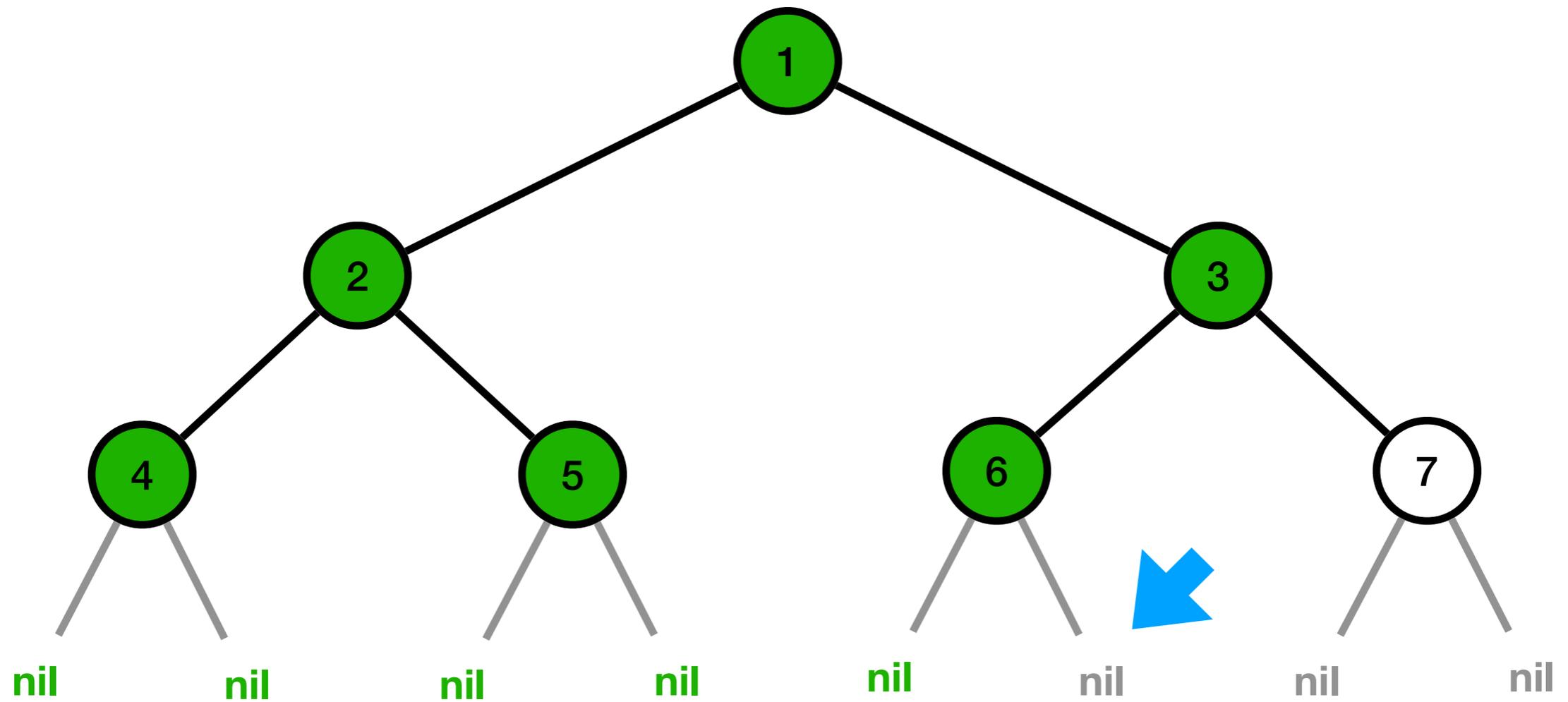
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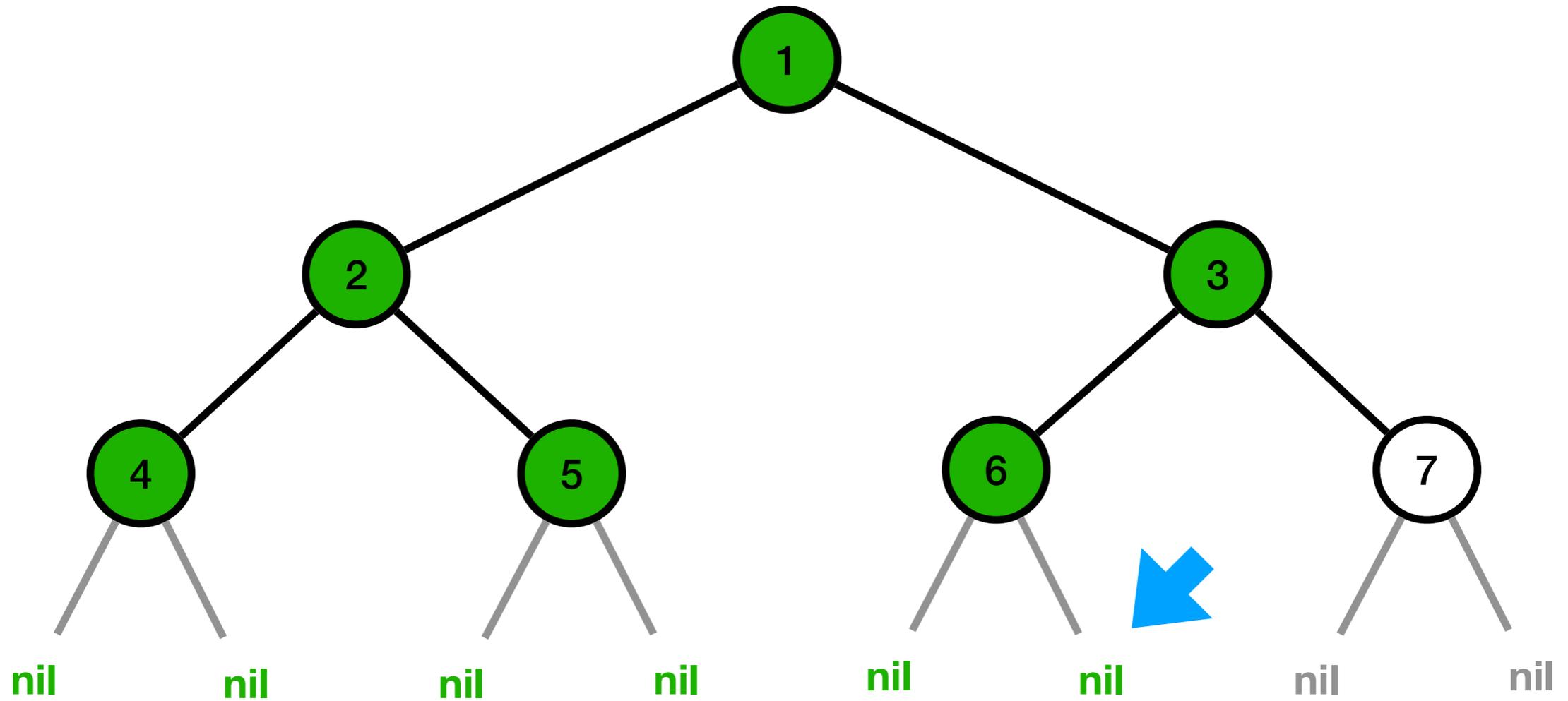
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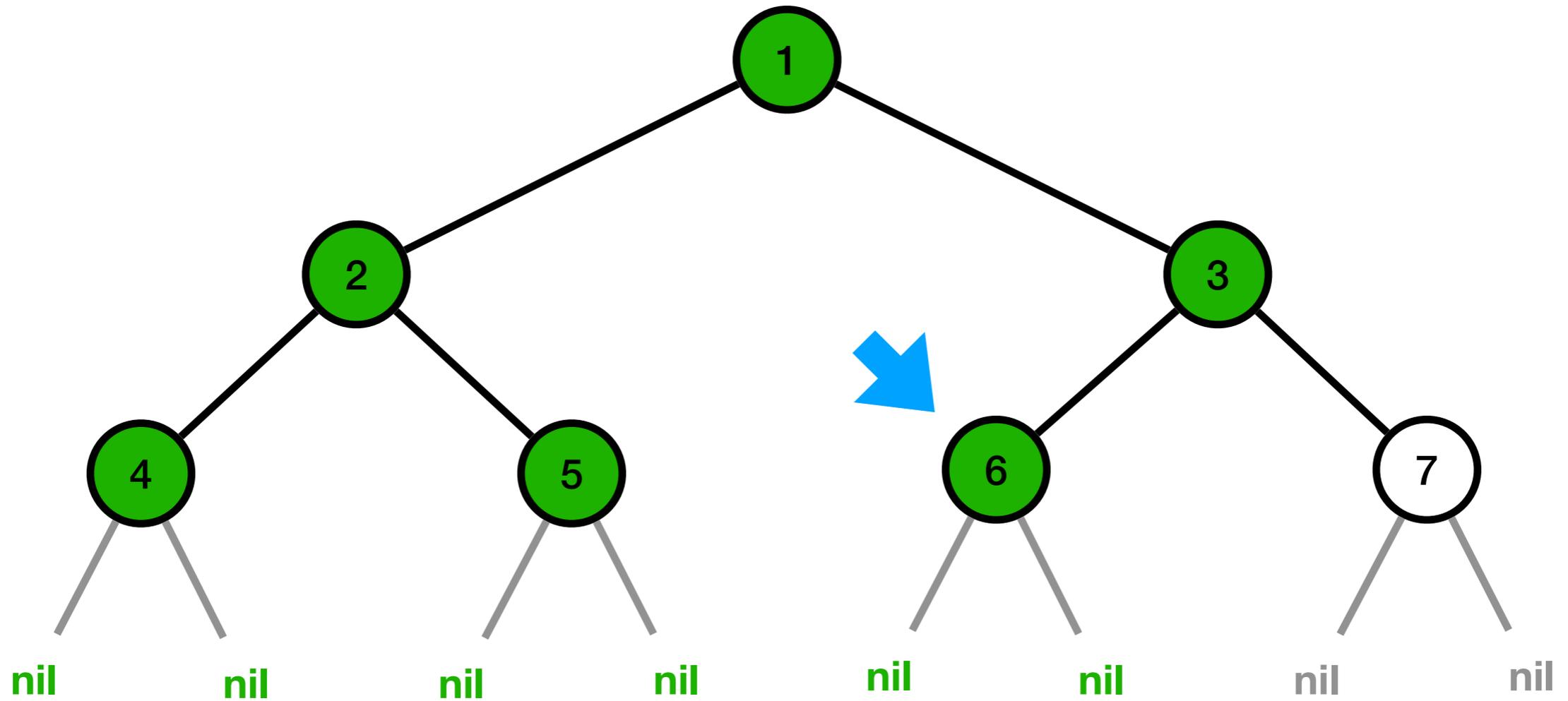
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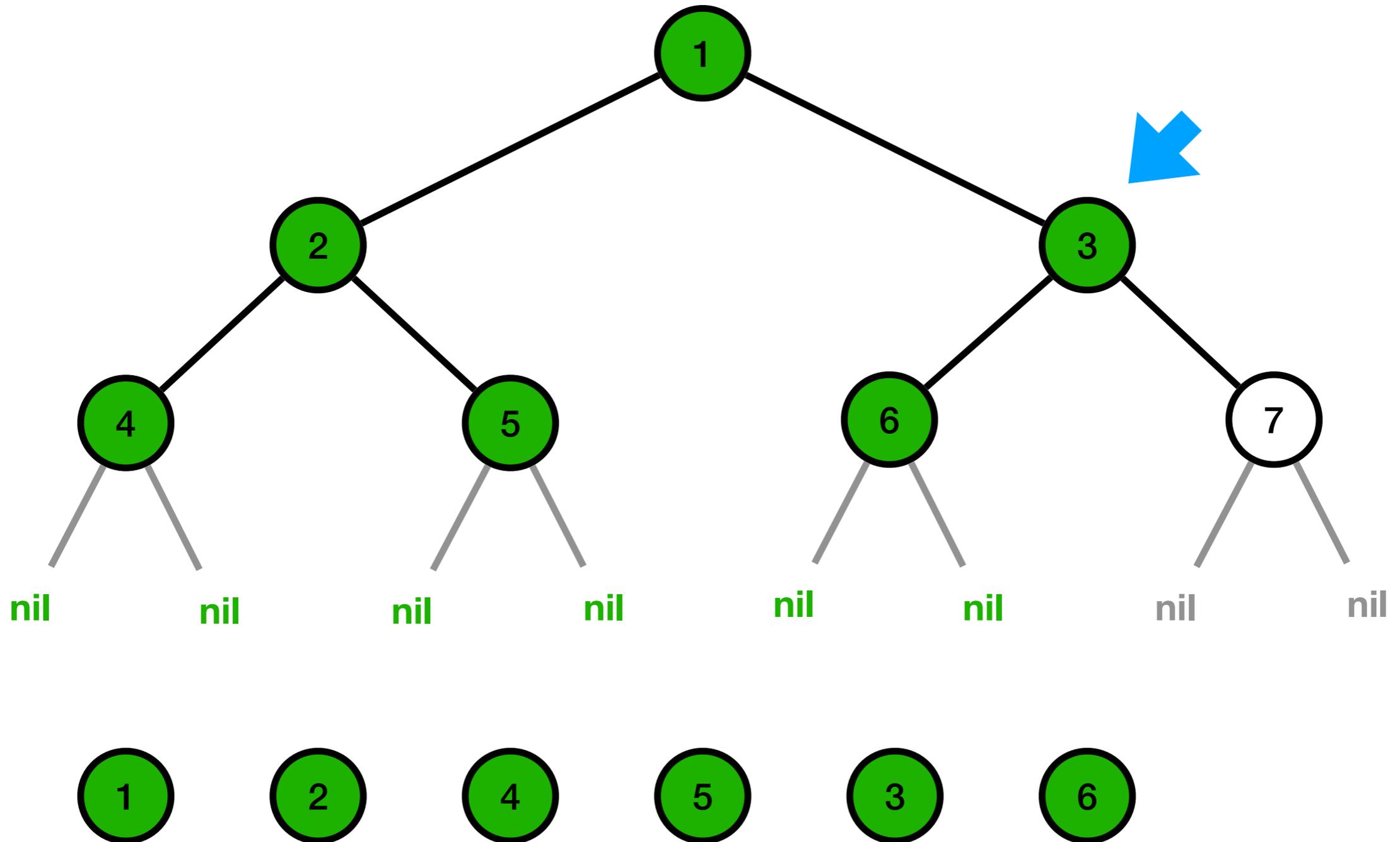
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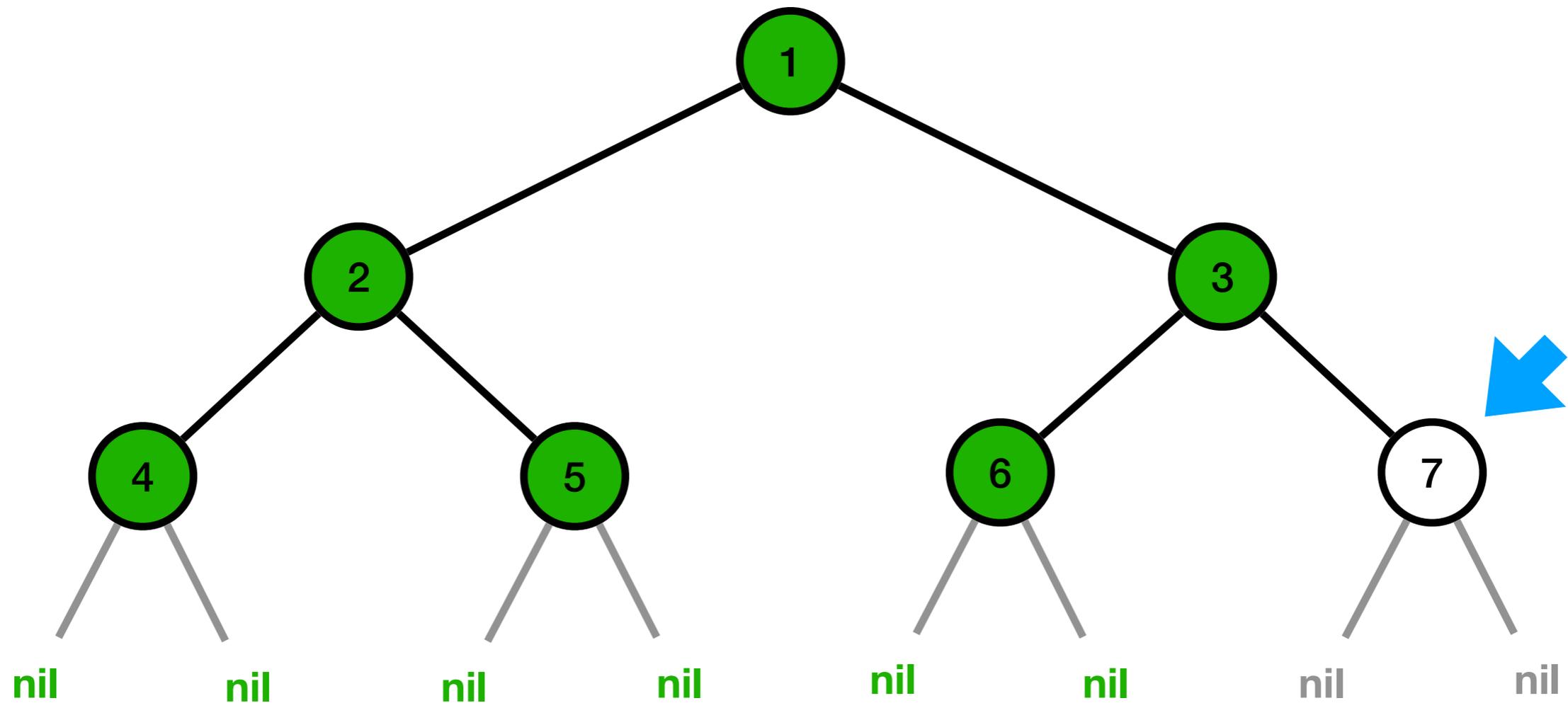
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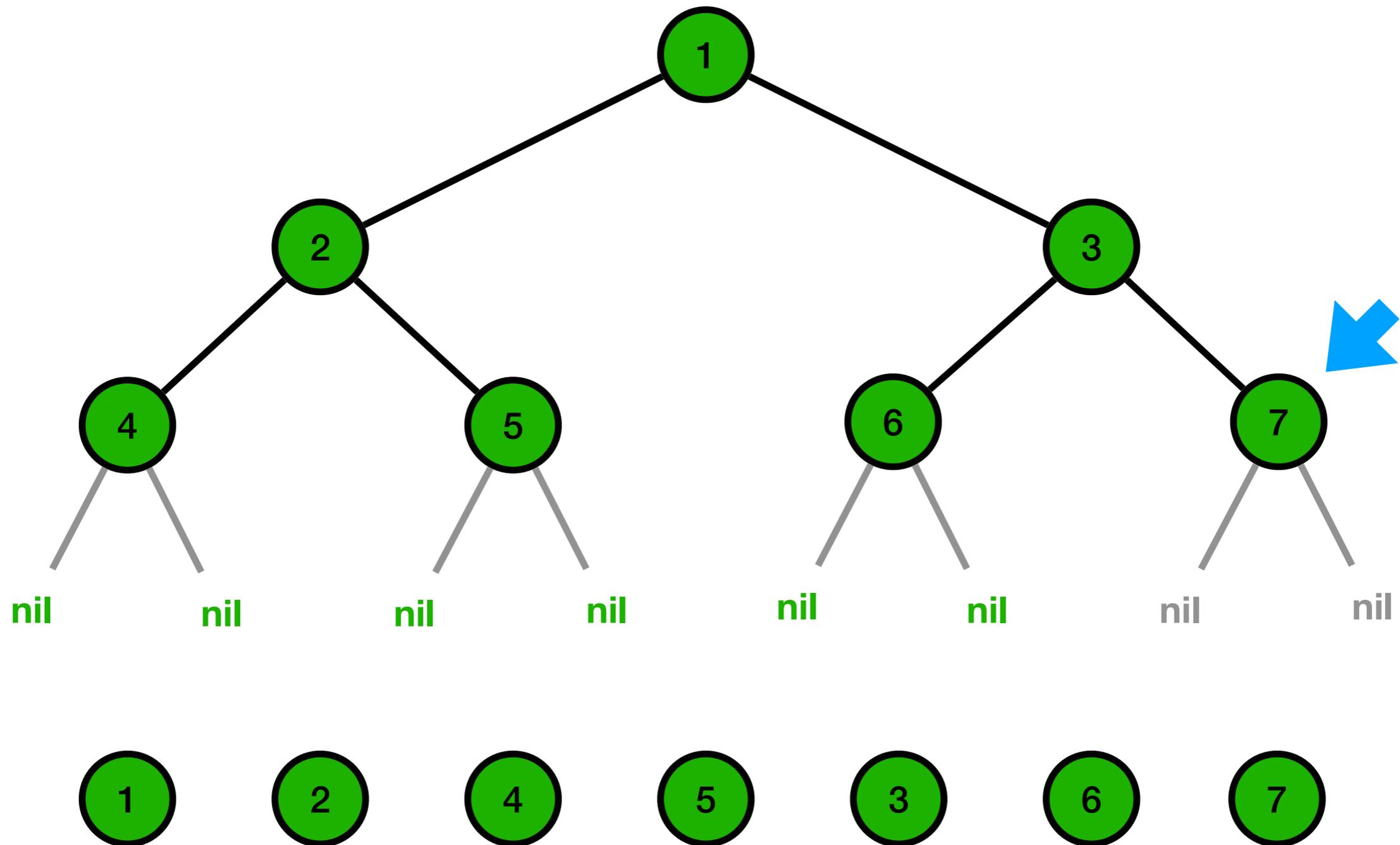
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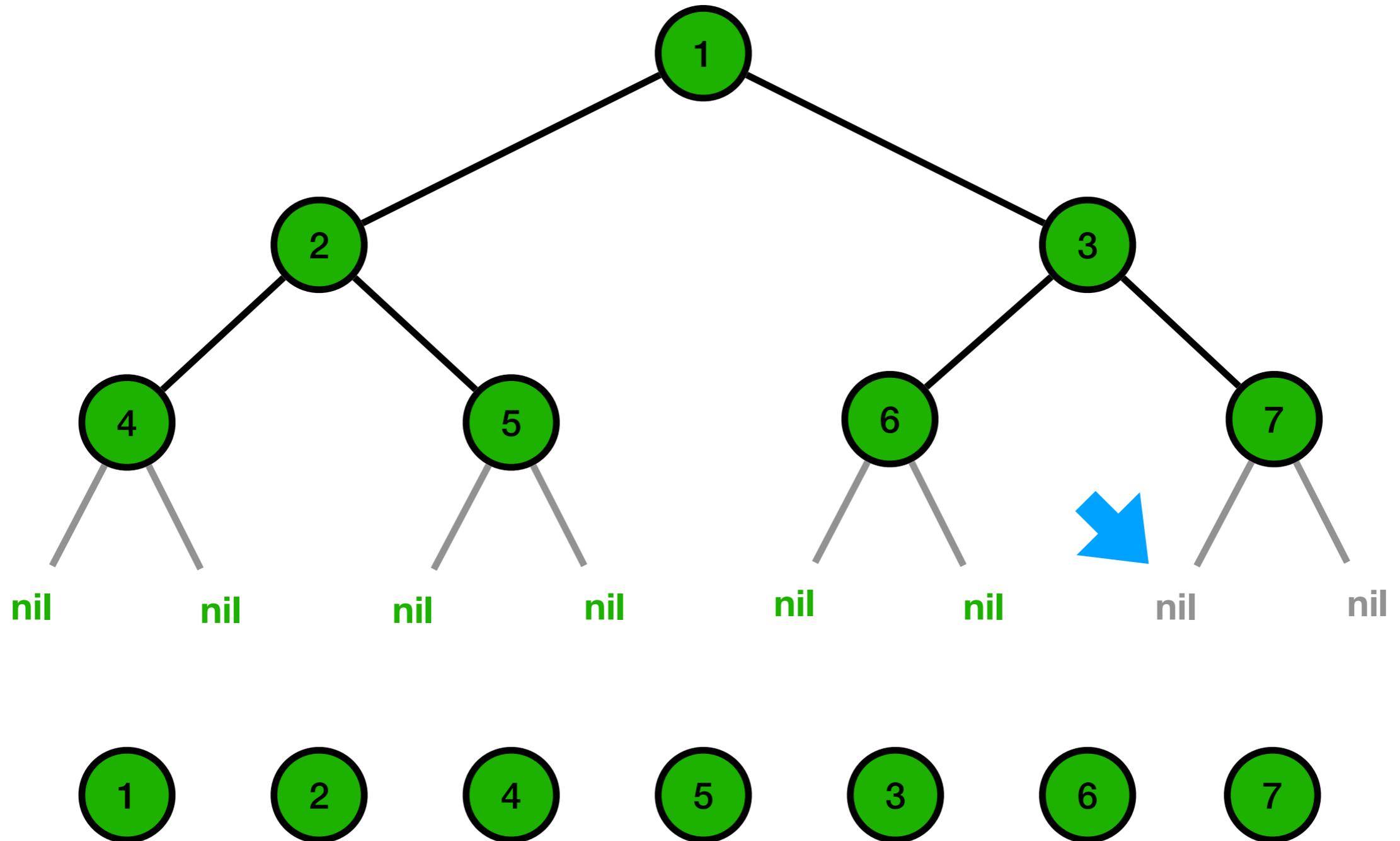
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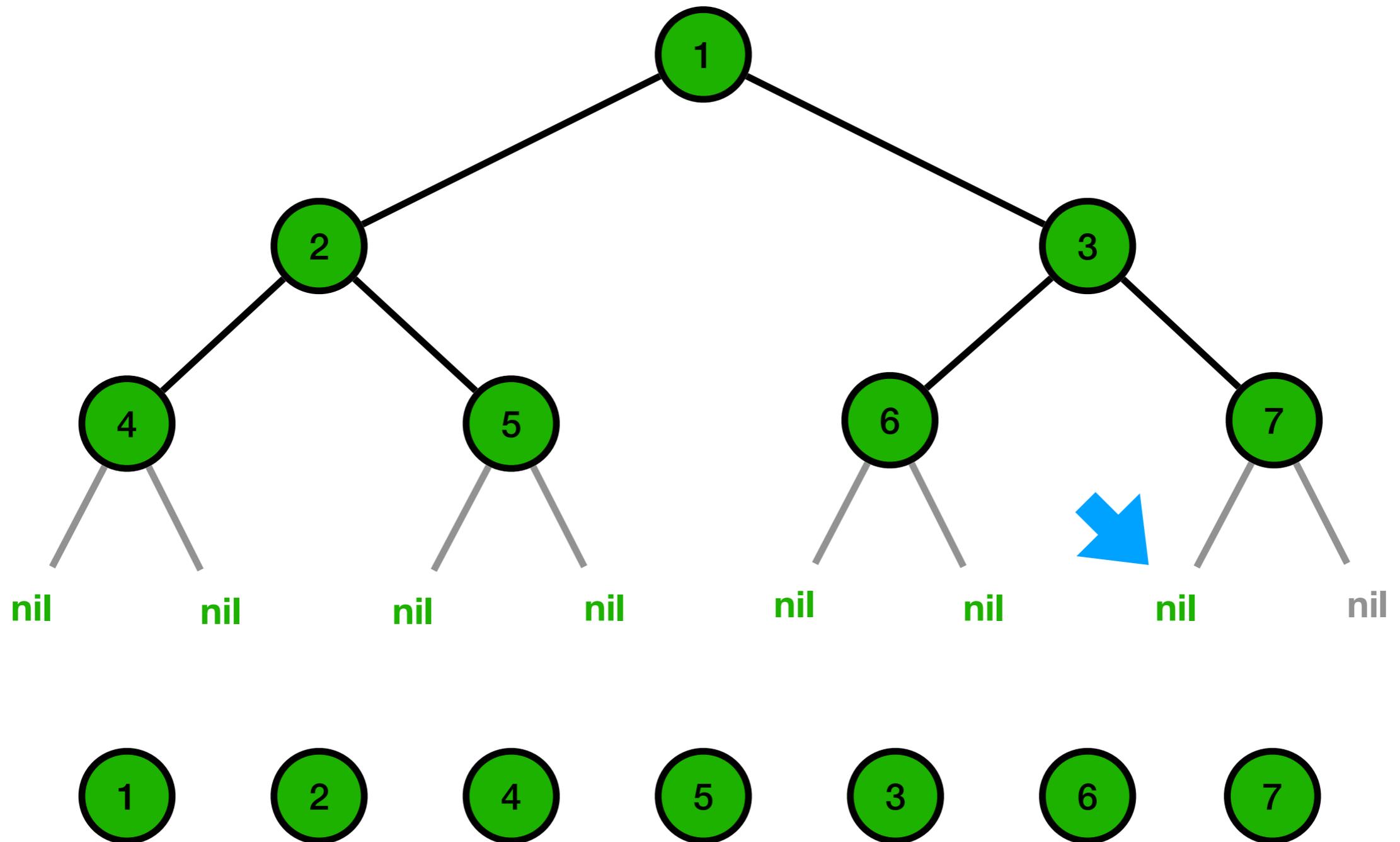
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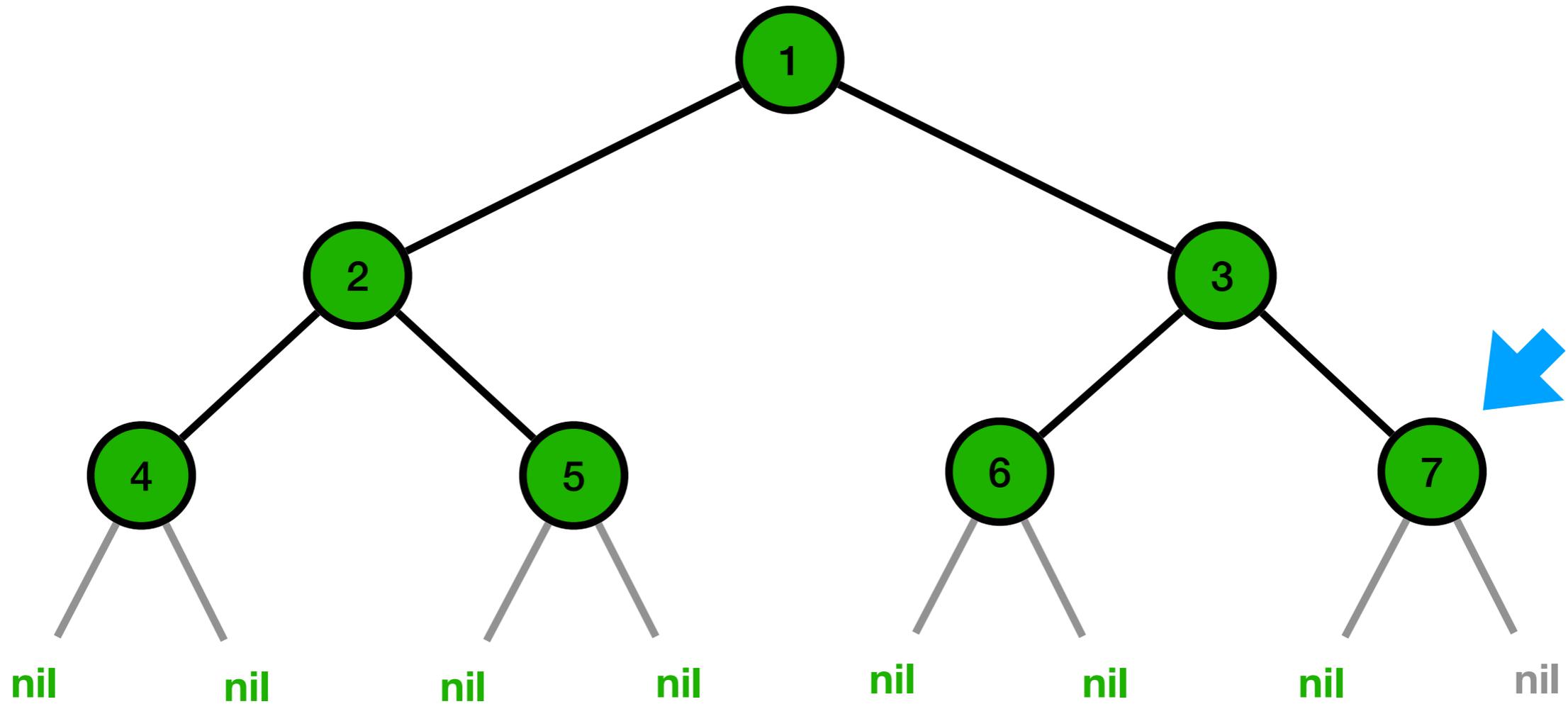
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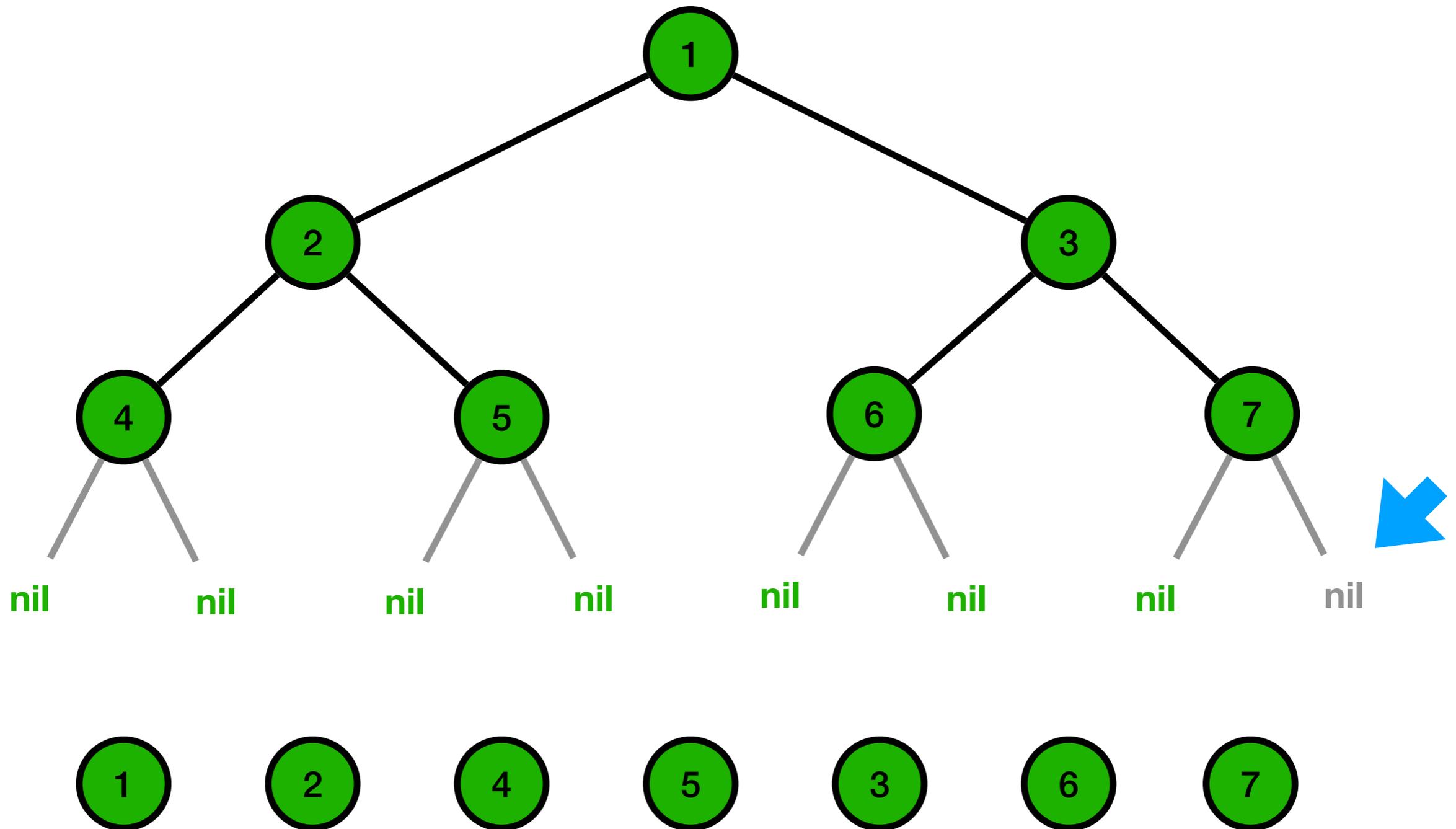
Parcours préfixe



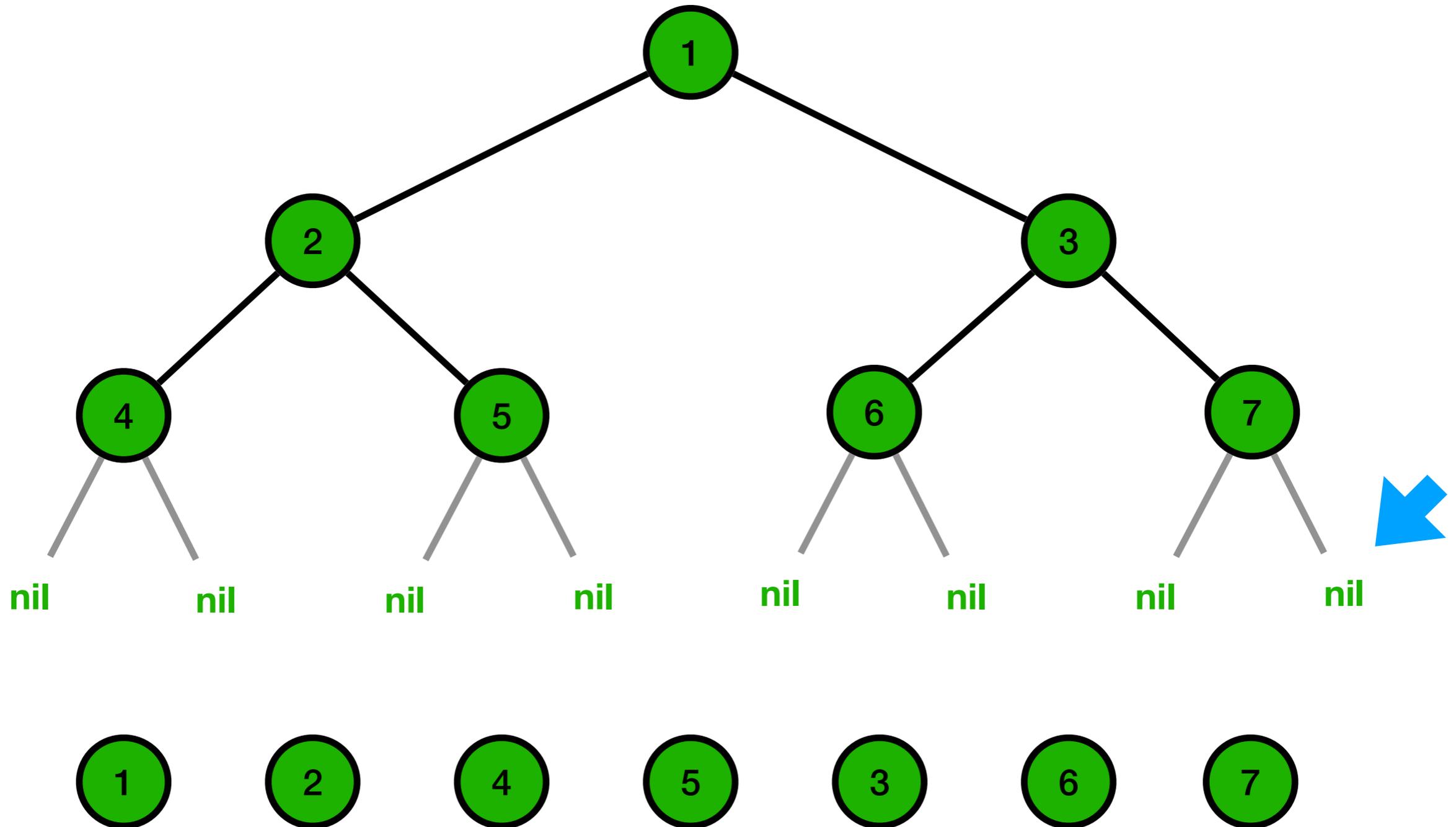
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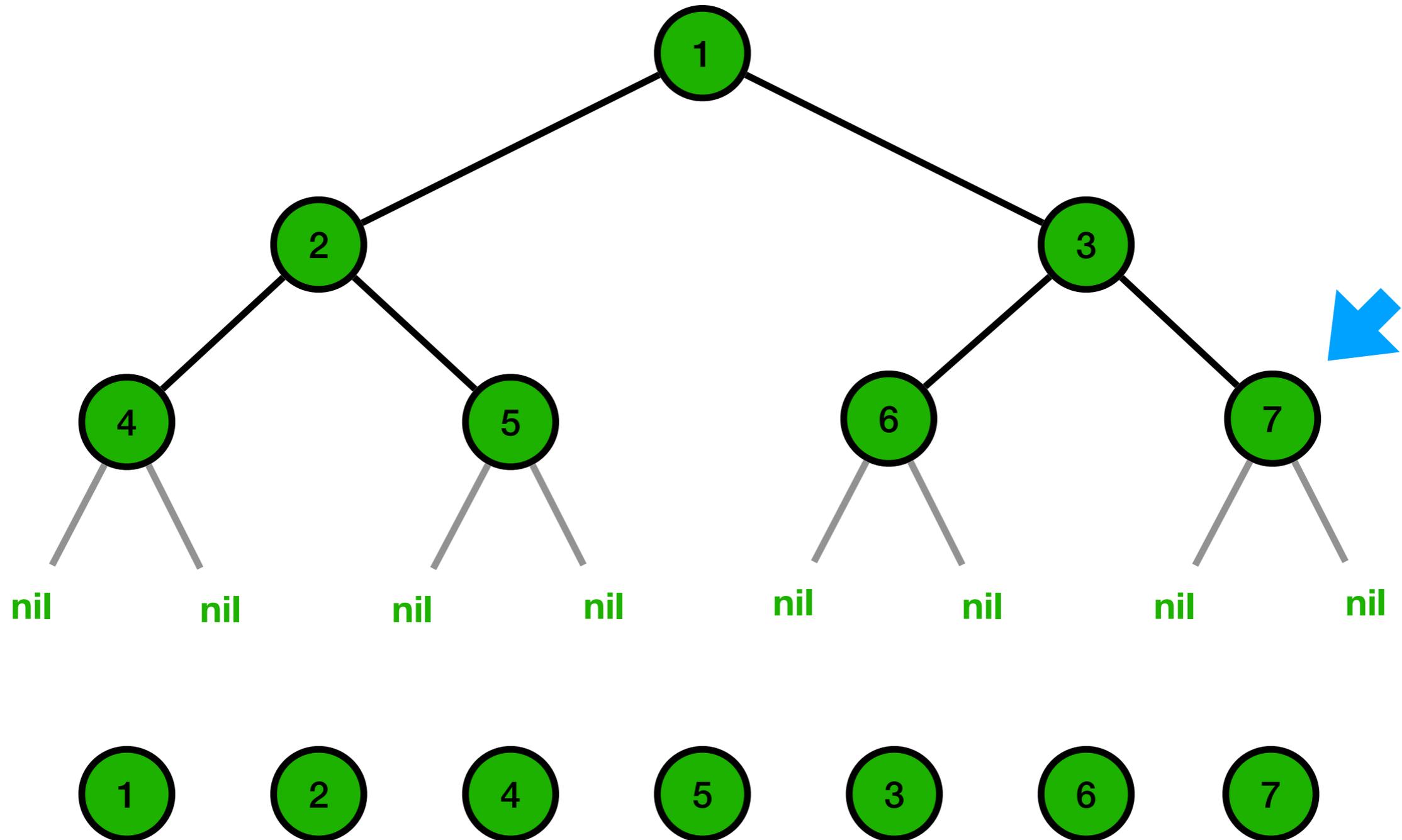
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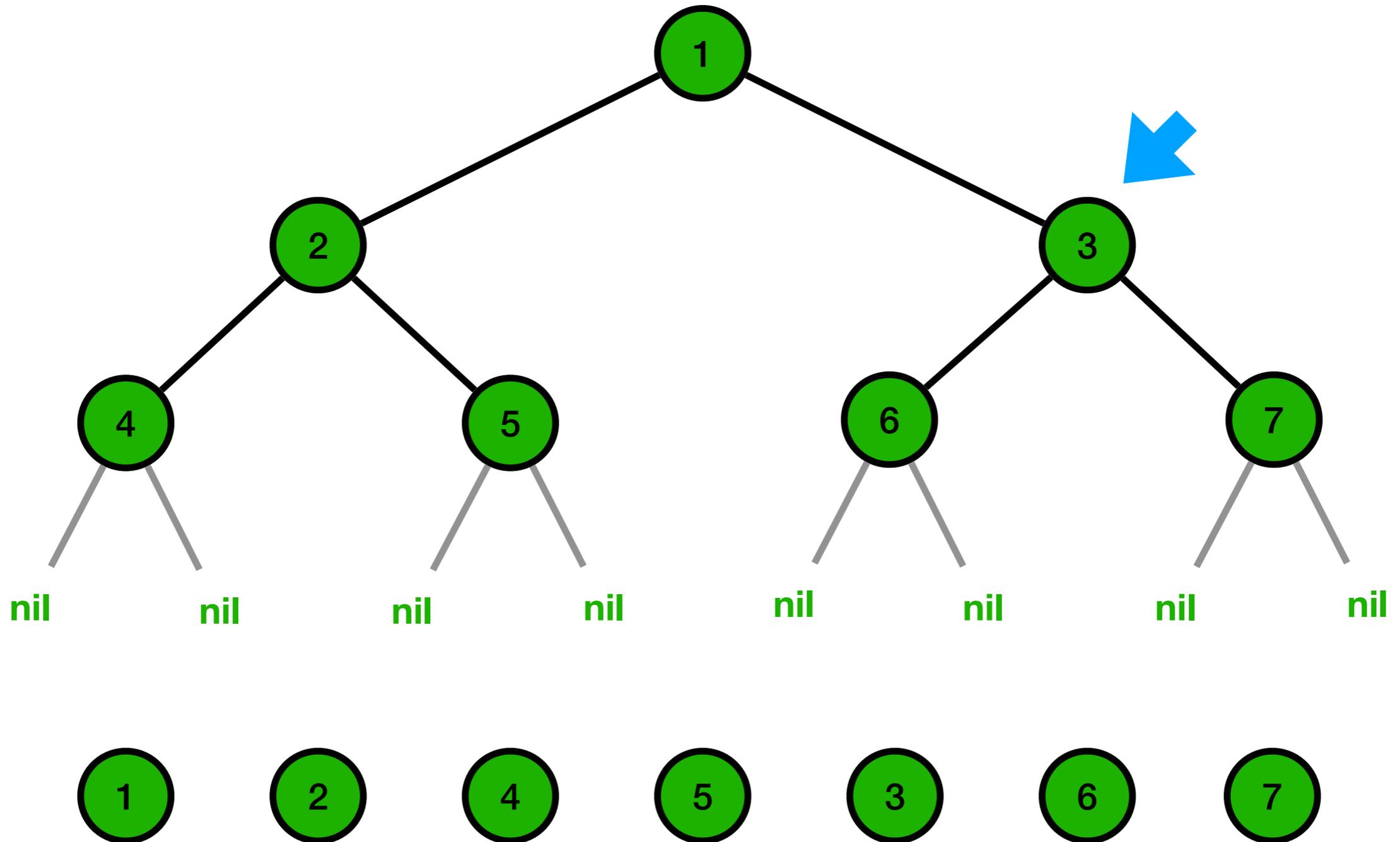
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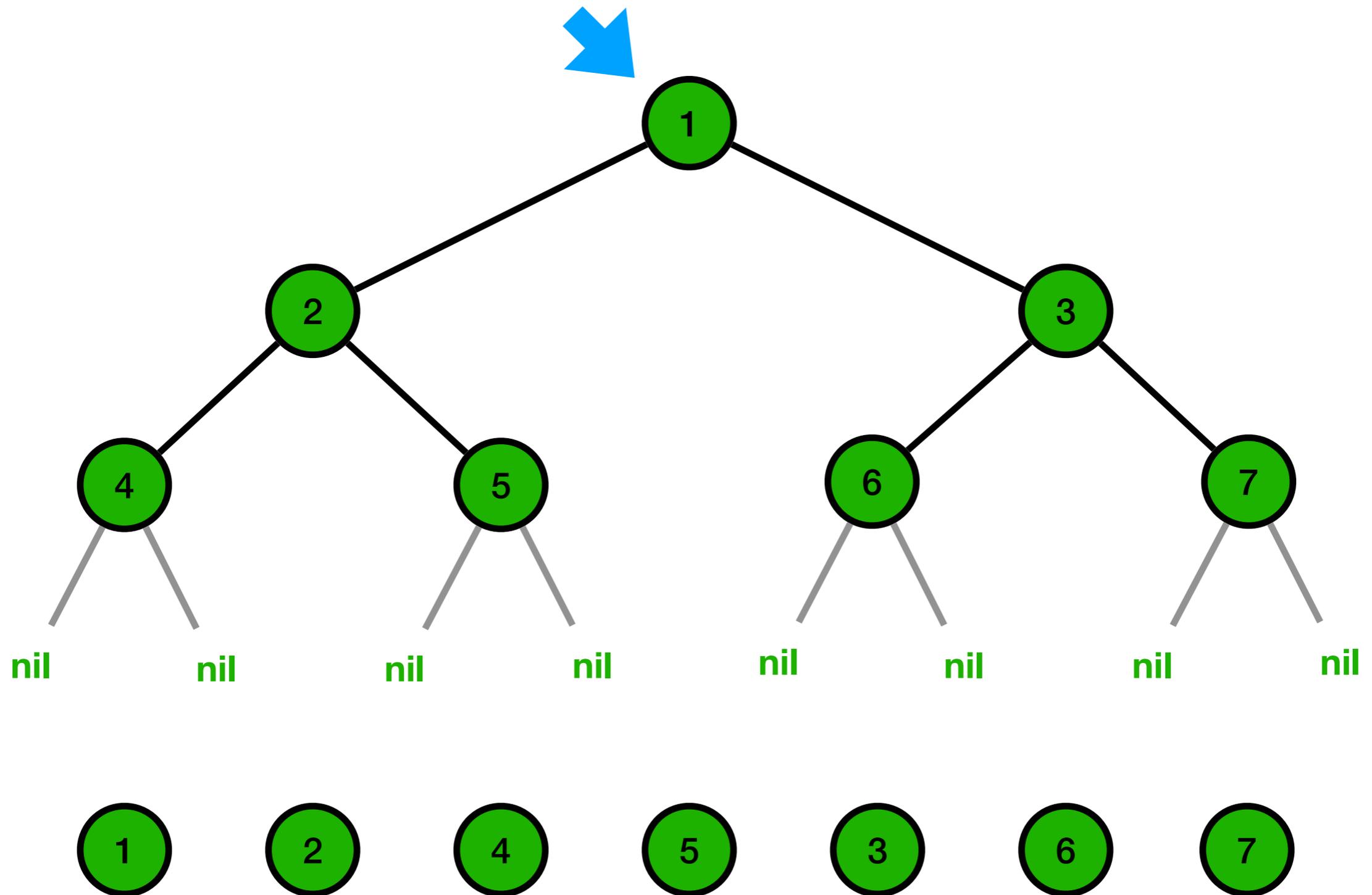
Parcours préfixe



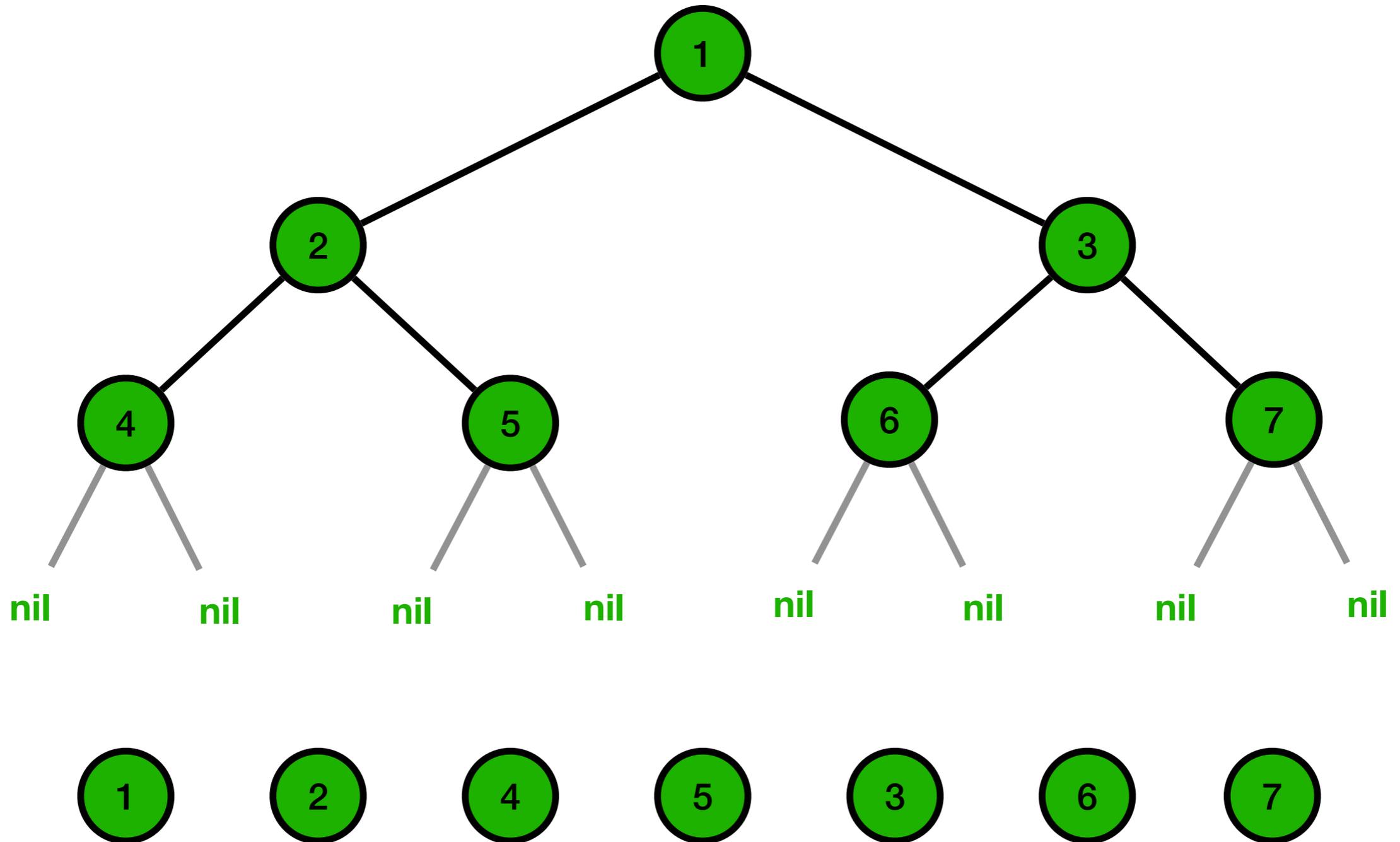
Parcours préfixe



Parcours préfixe



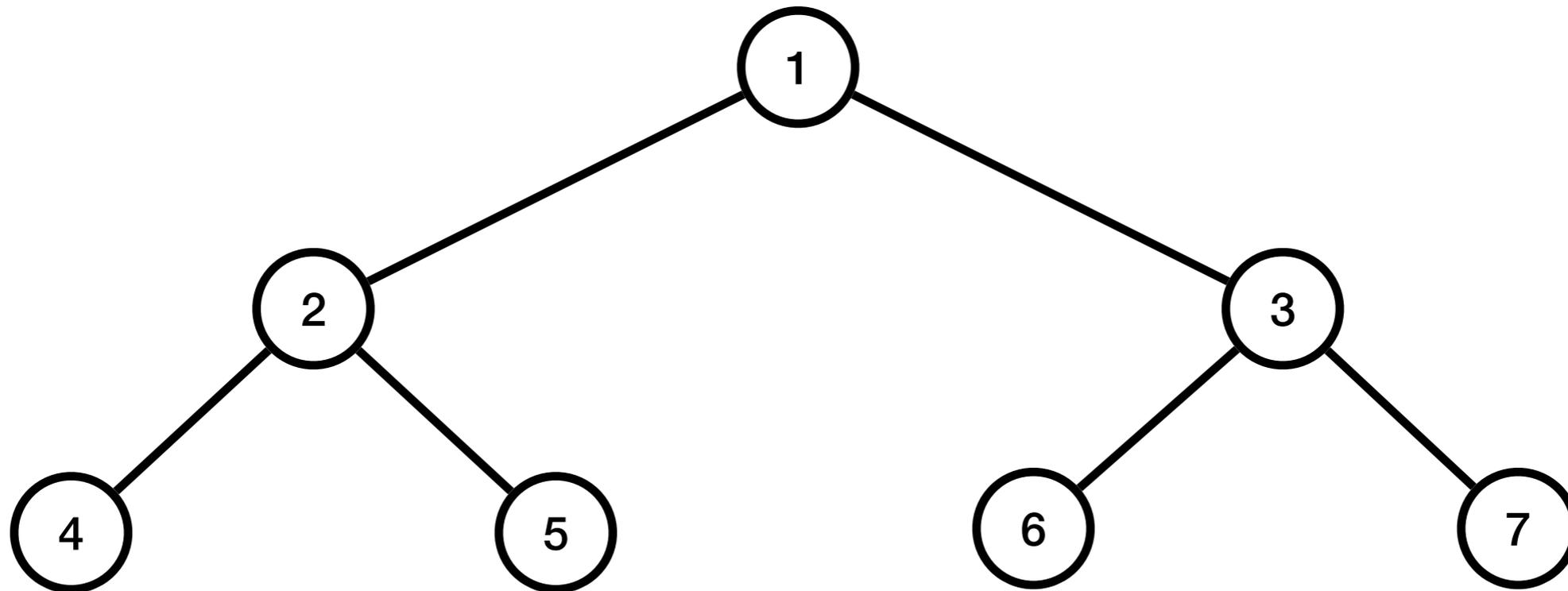
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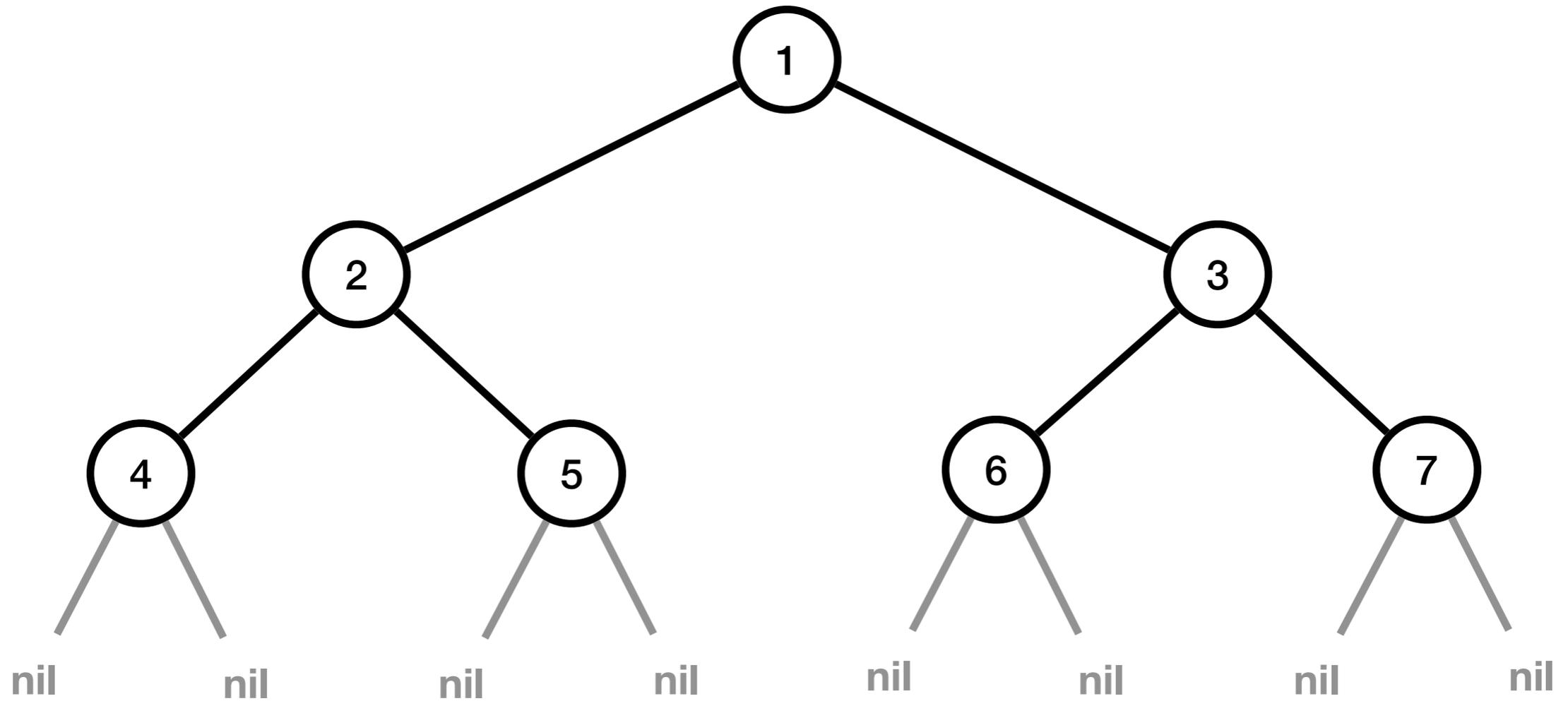
Parcours postfixe (ou suffixe)

```
def parcours_postfixe(arbre):  
    if not est_vide(arbre):  
        parcours_postfixe(gauche(arbre))  
        parcours_postfixe(droite(arbre))  
        print(valeur(arbre))
```

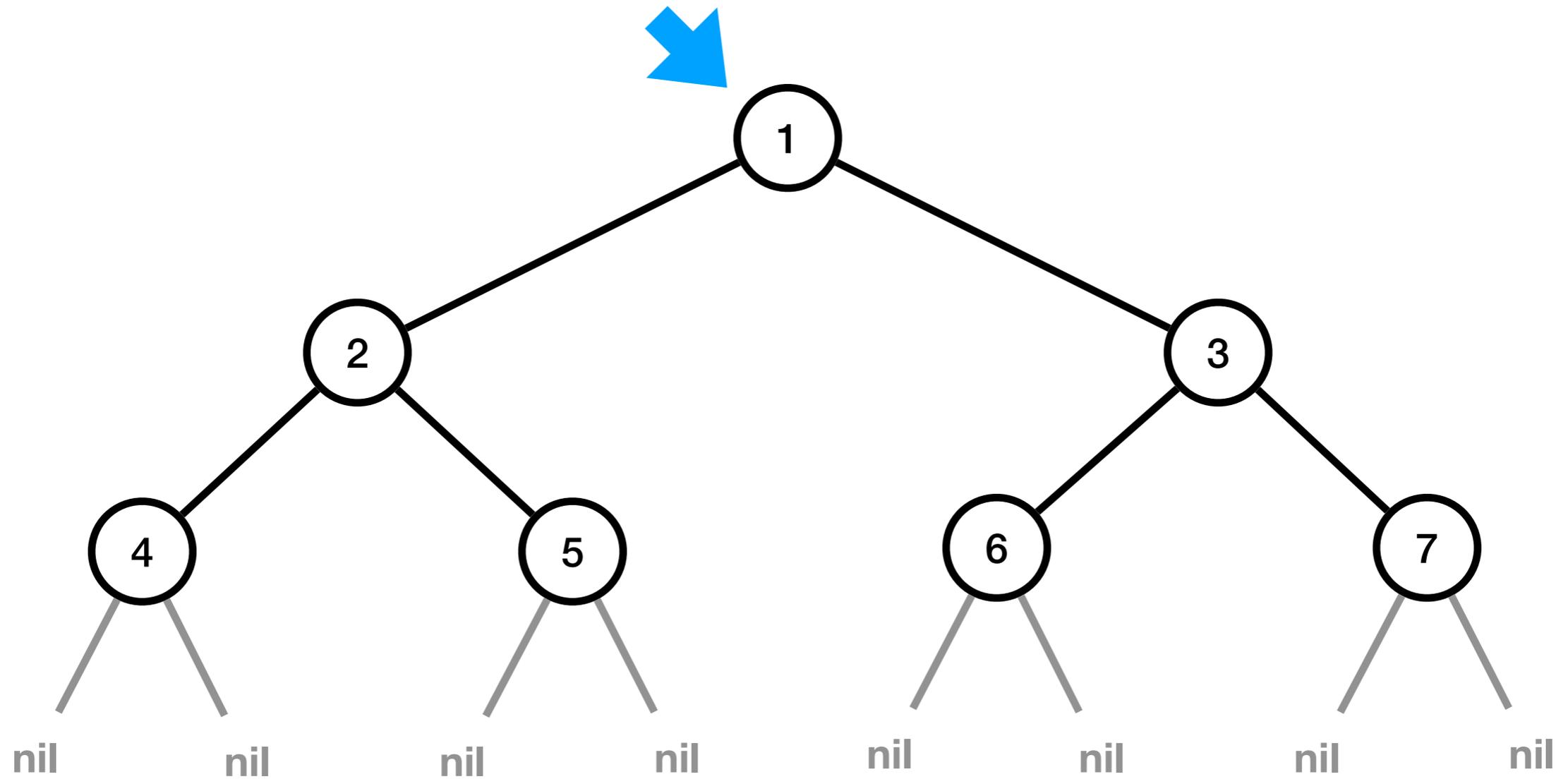
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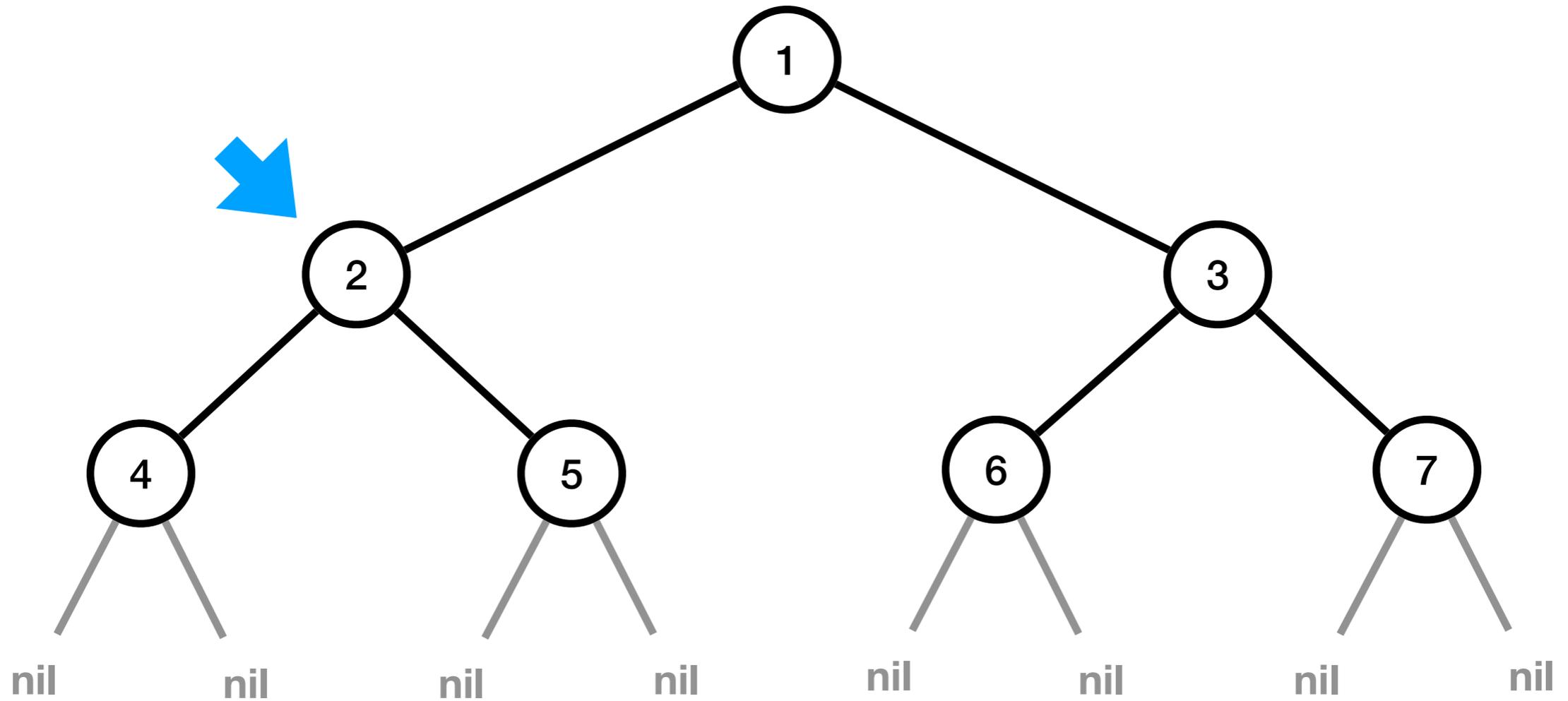
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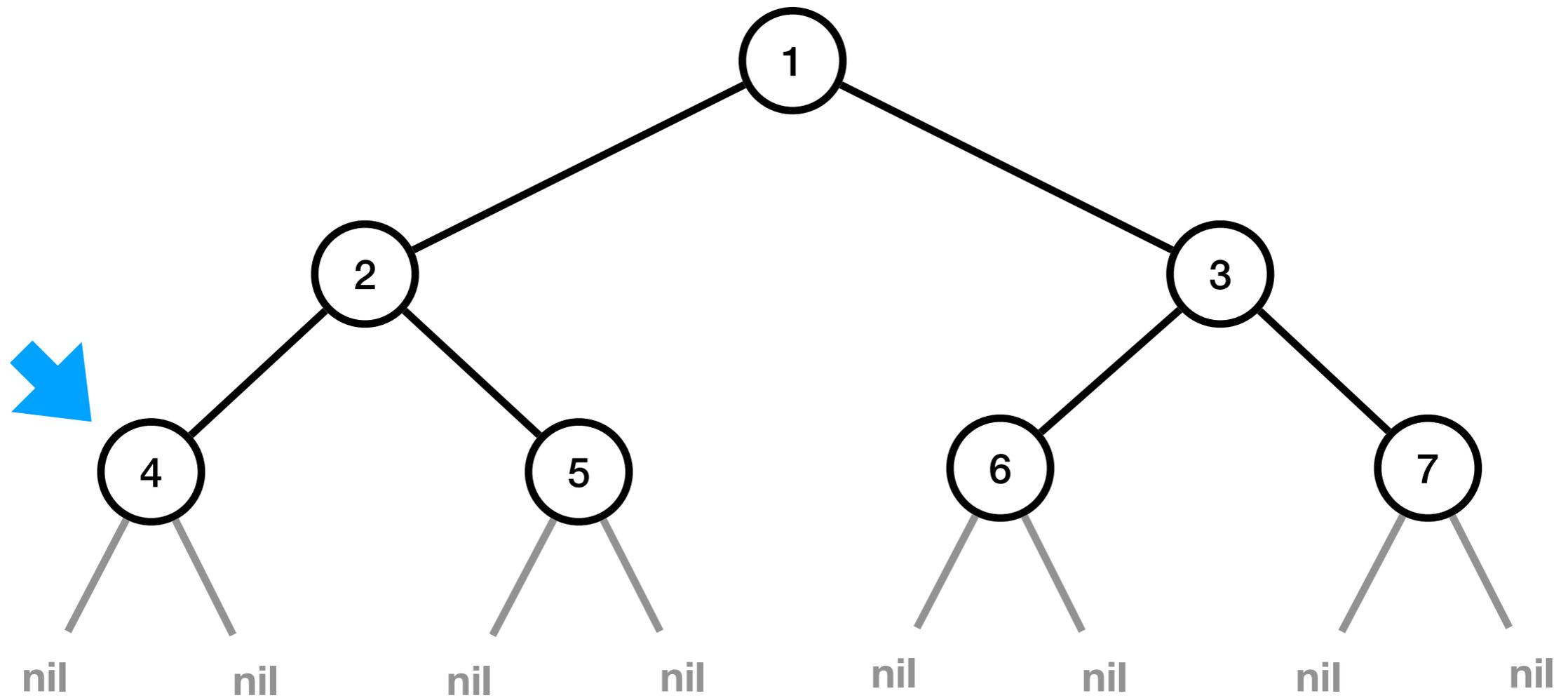
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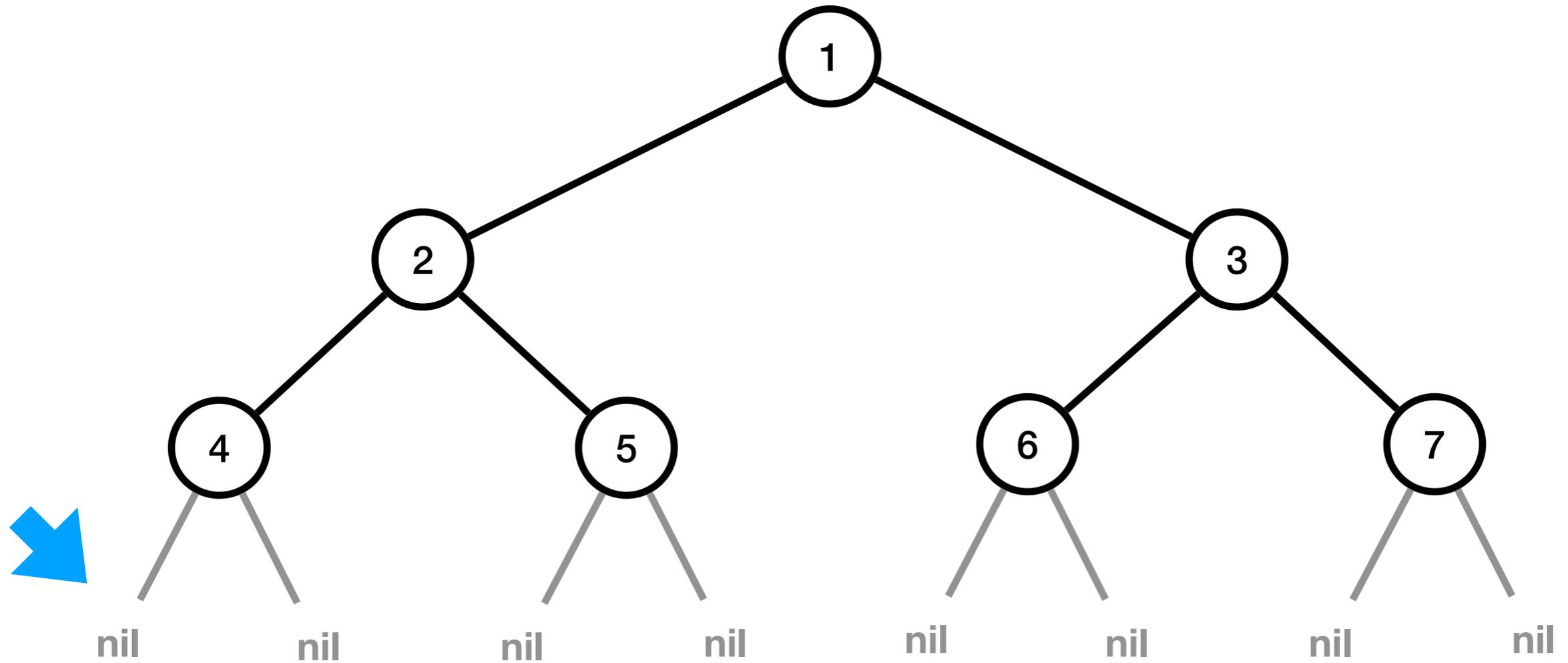
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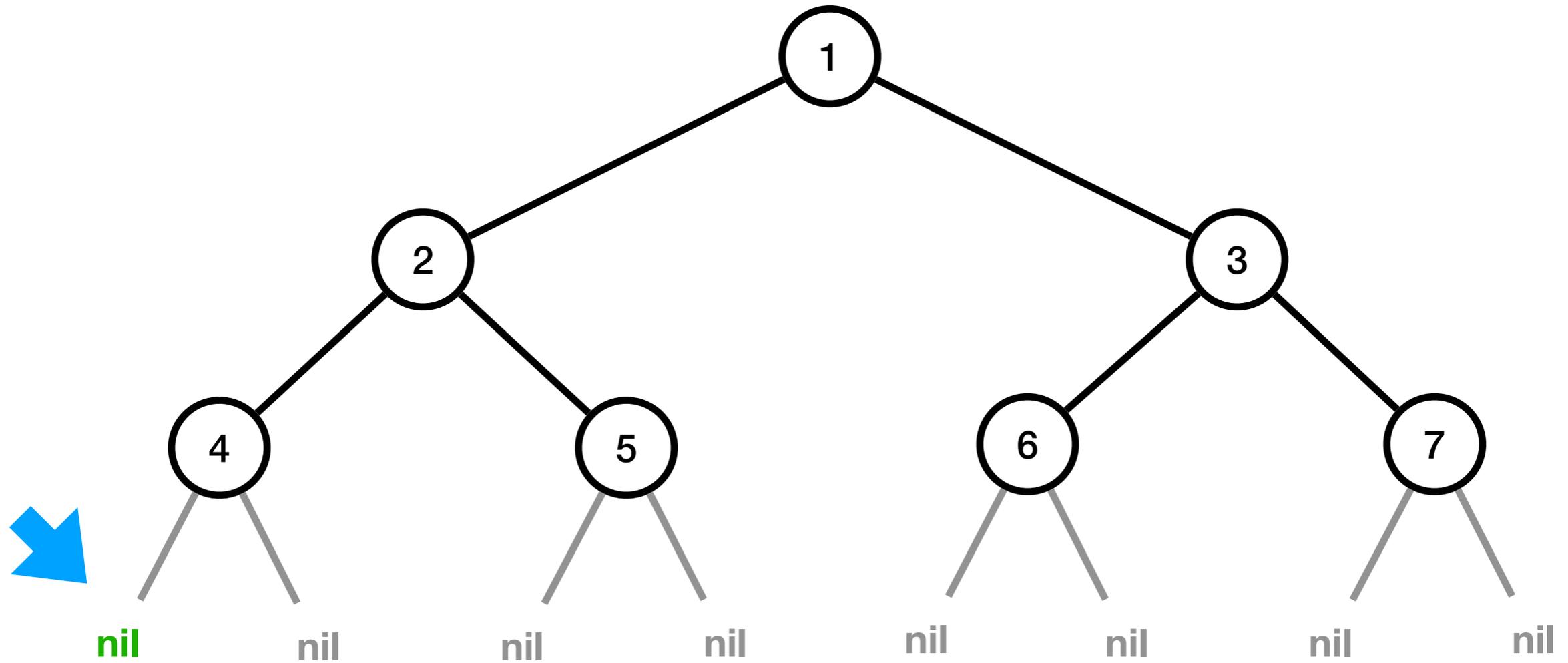
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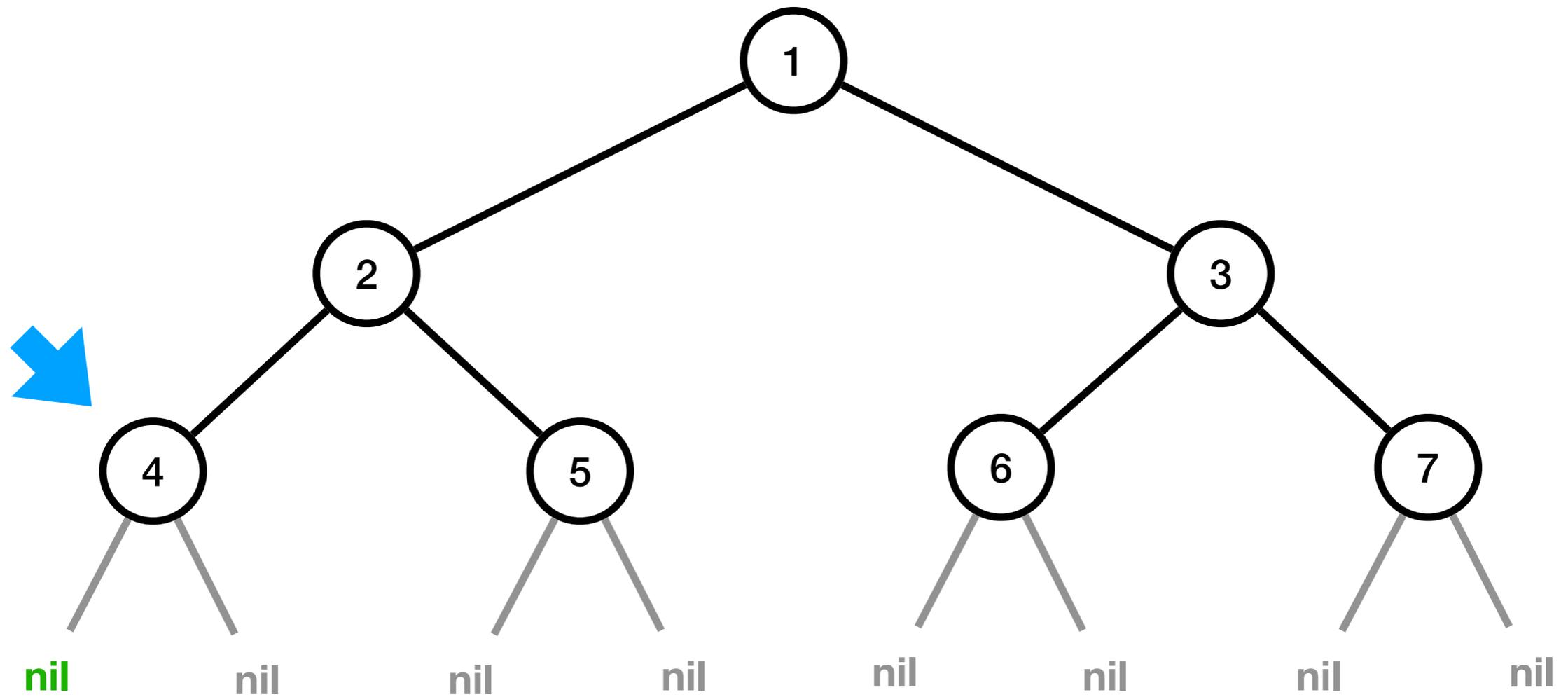
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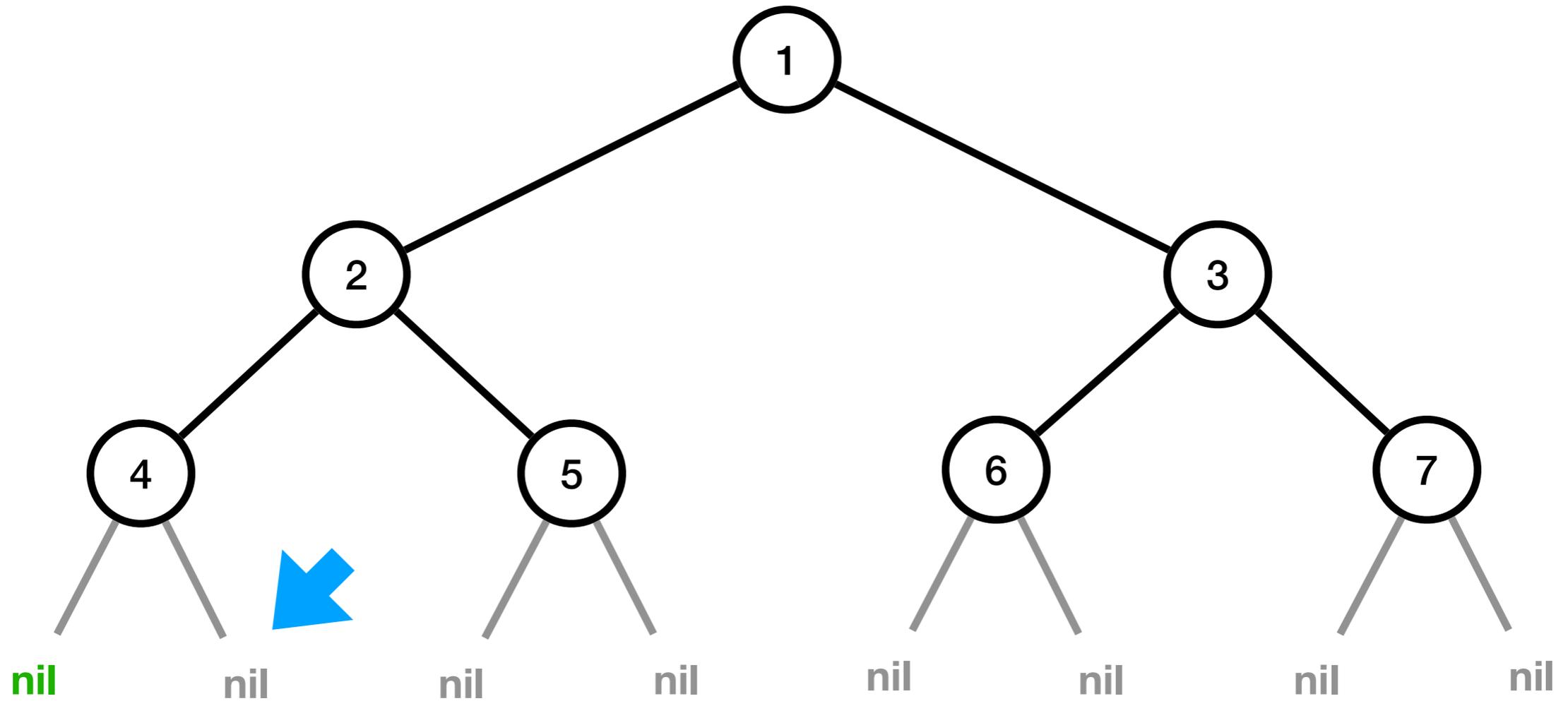
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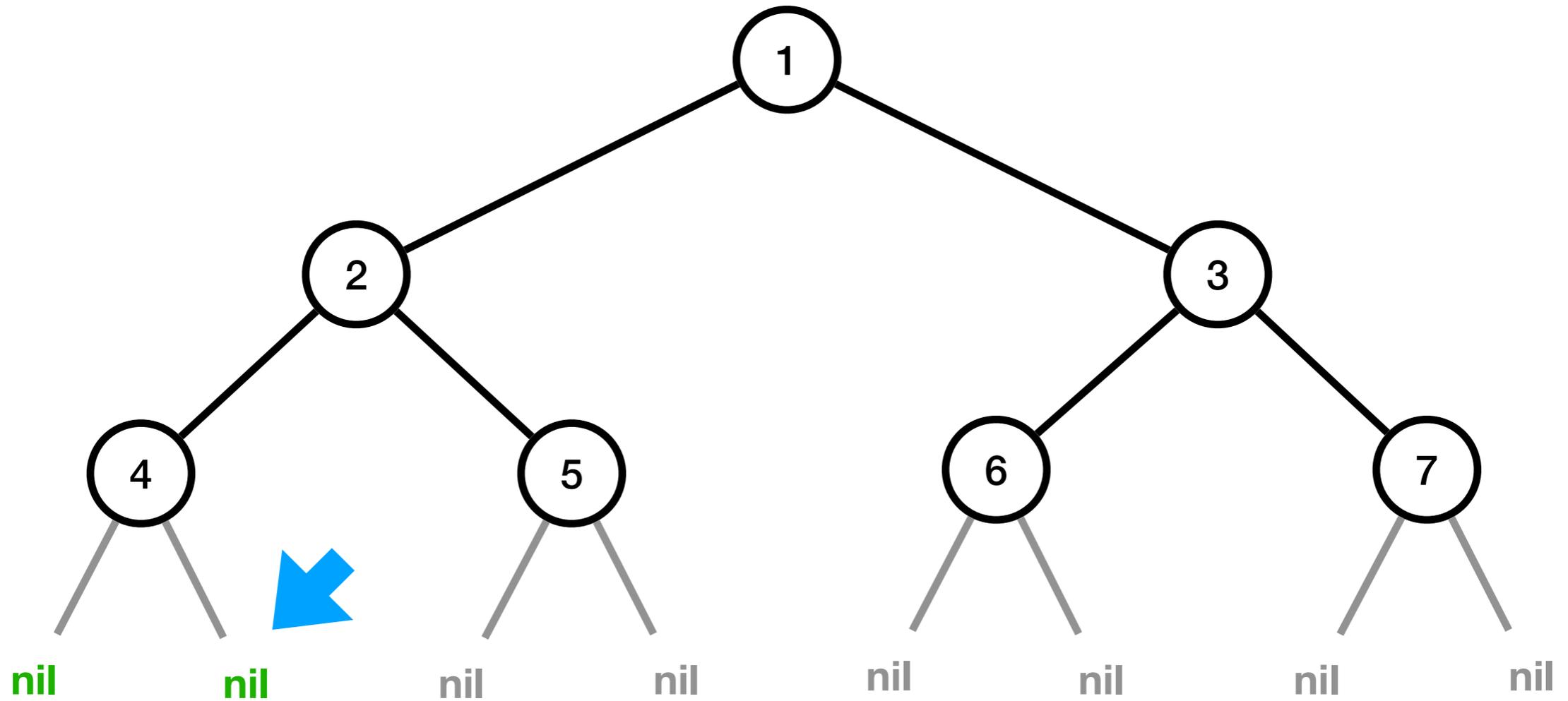
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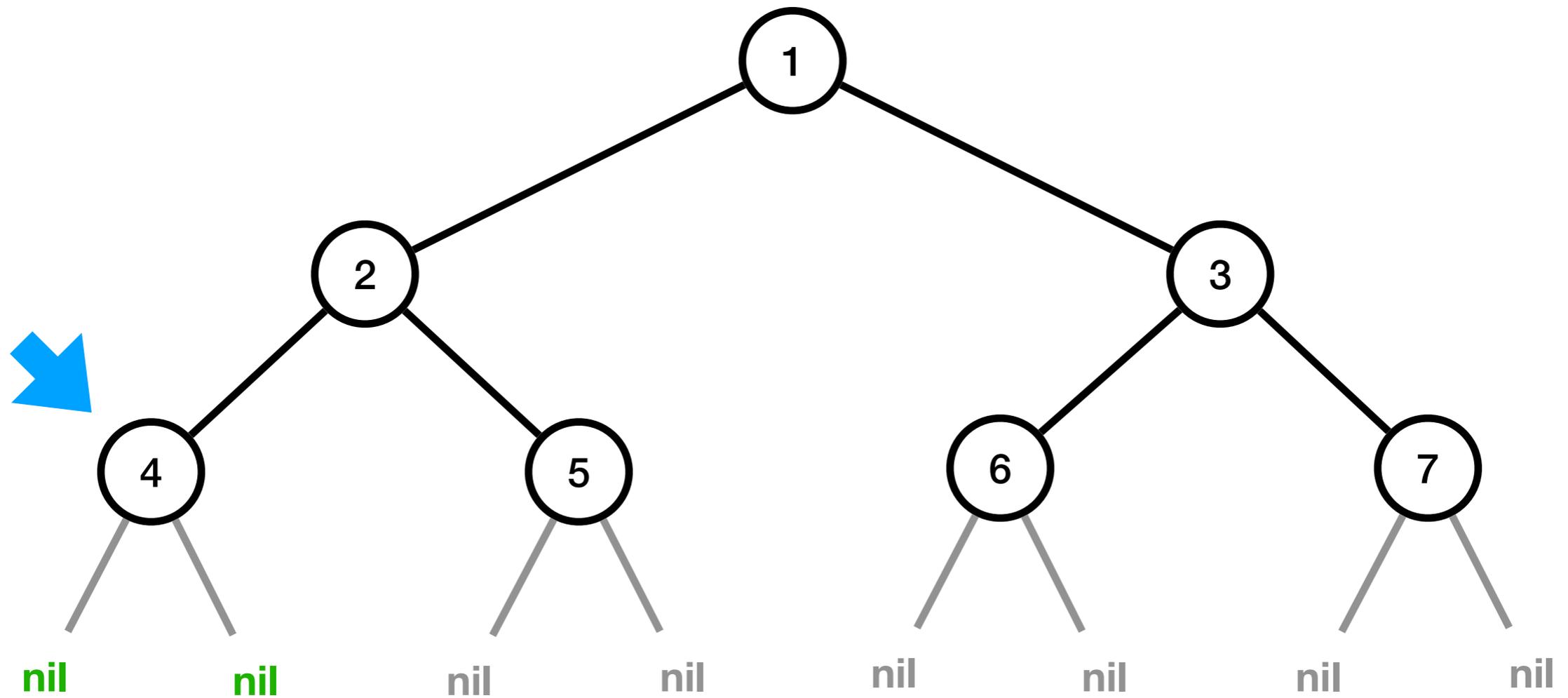
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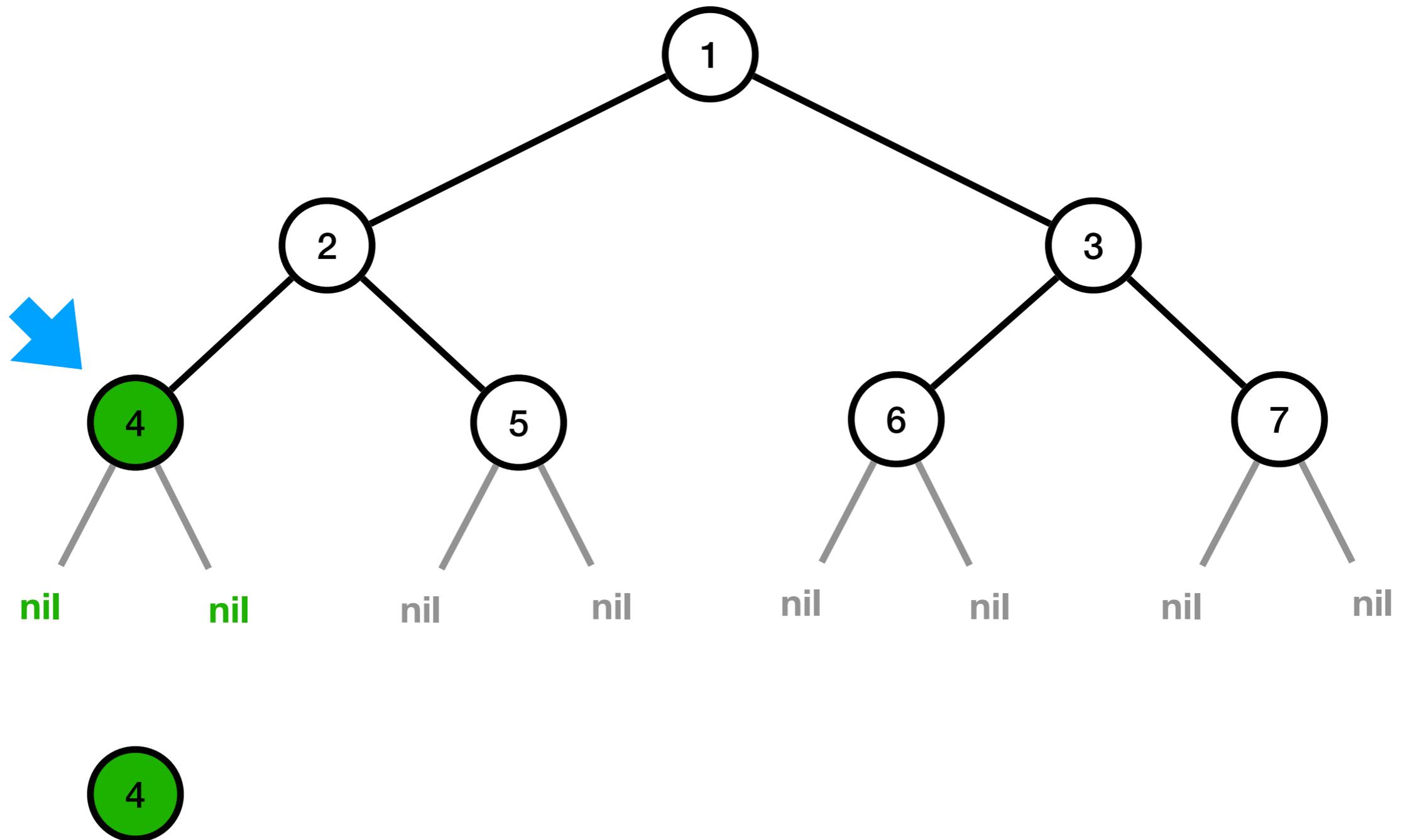
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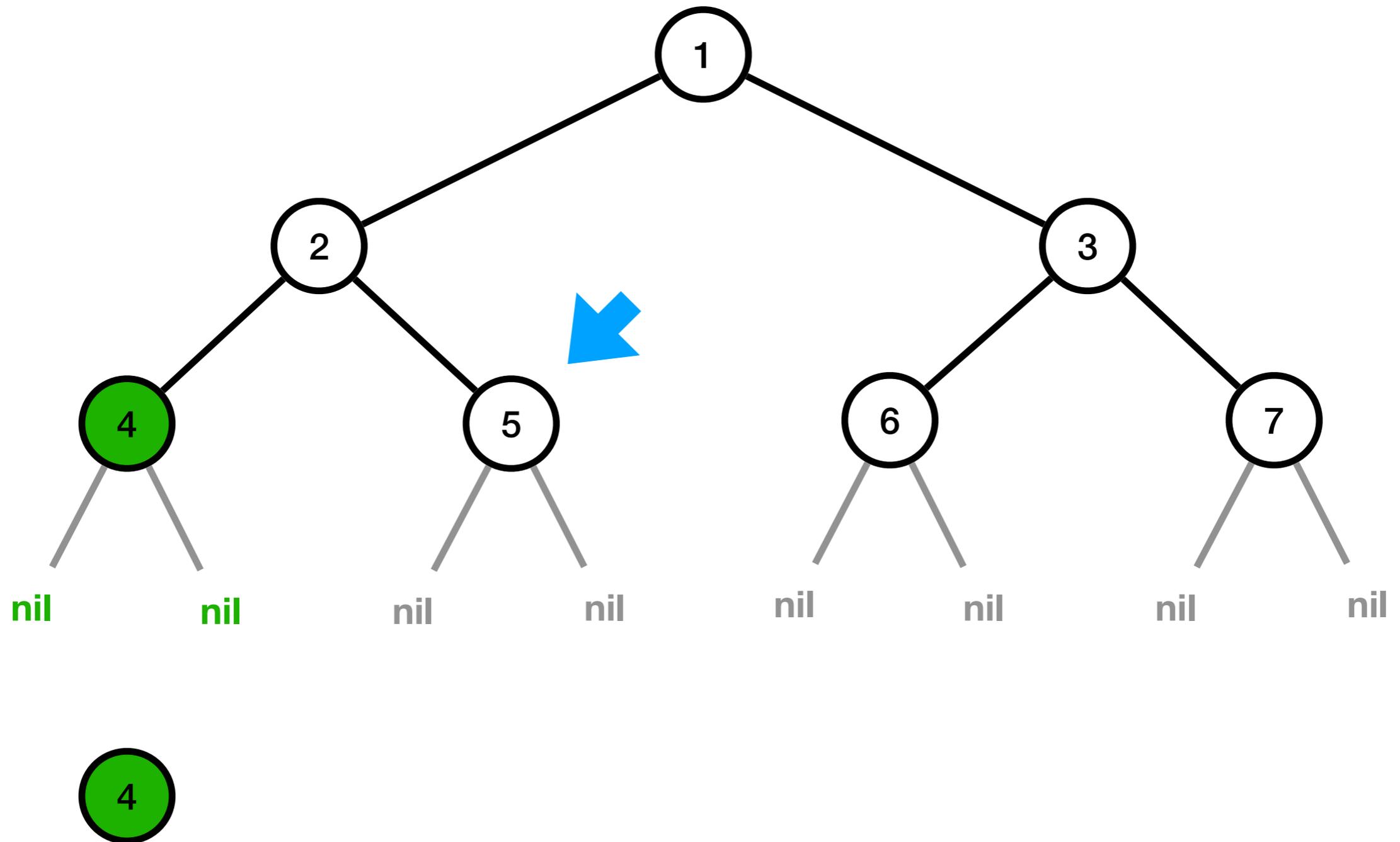
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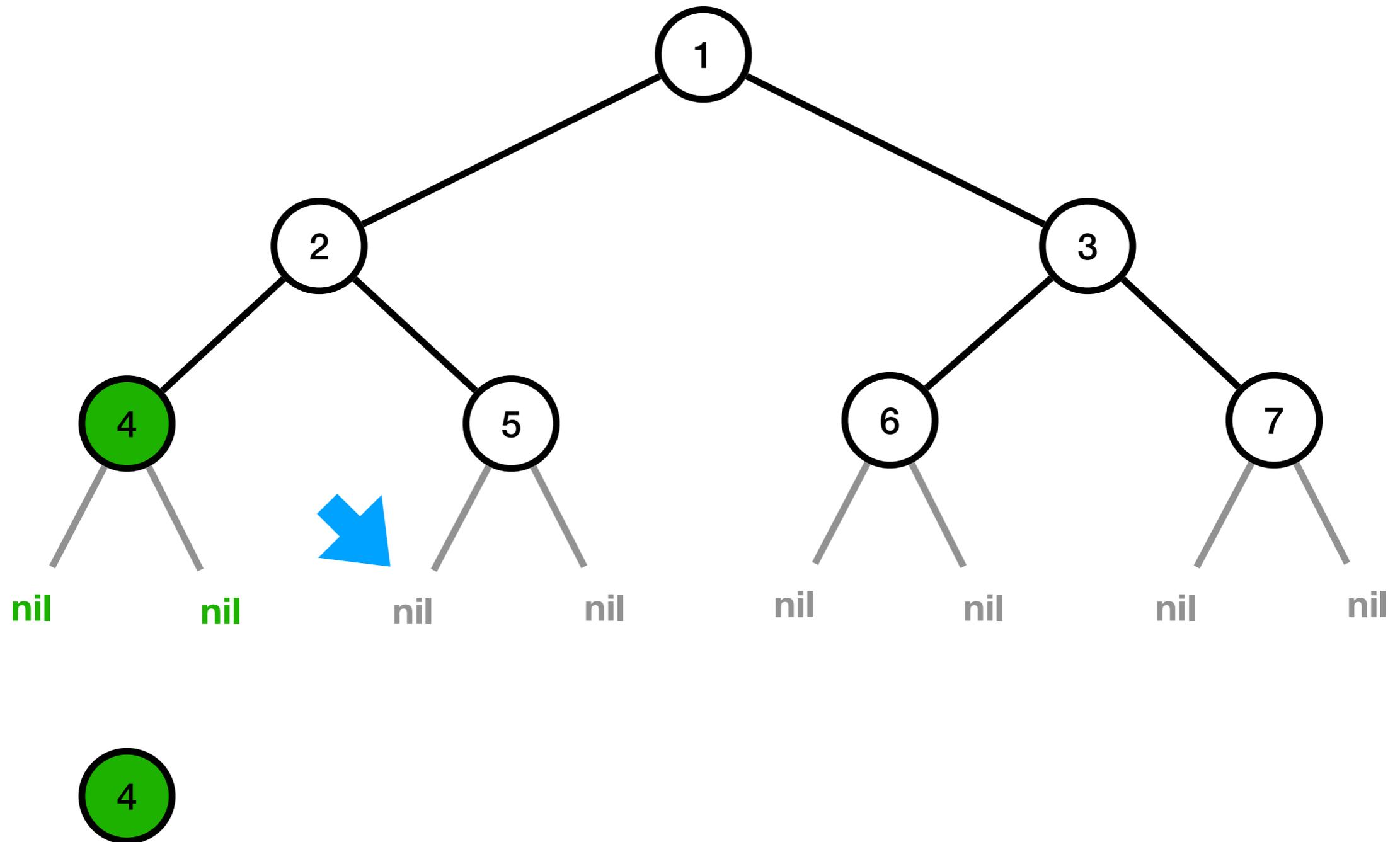
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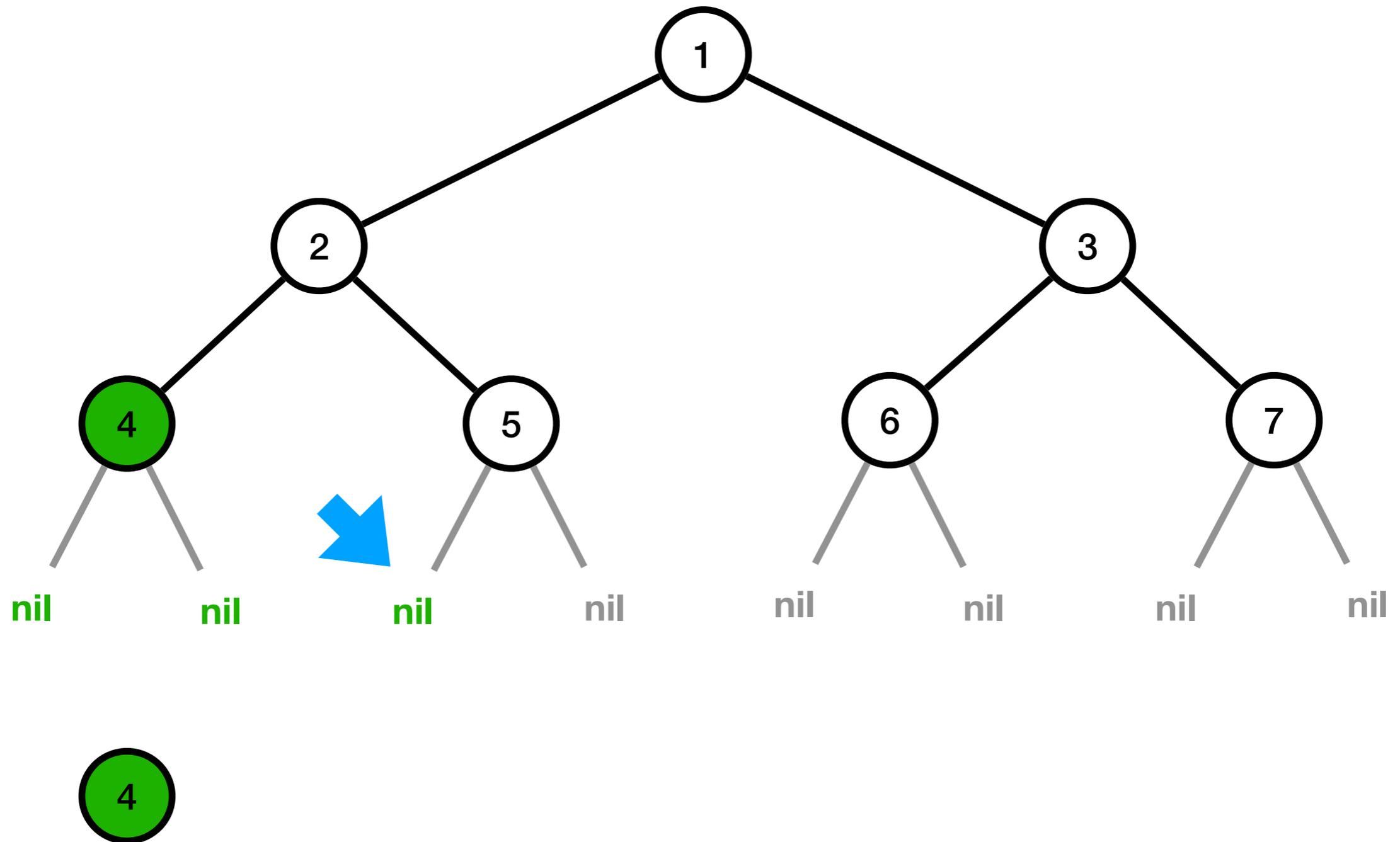
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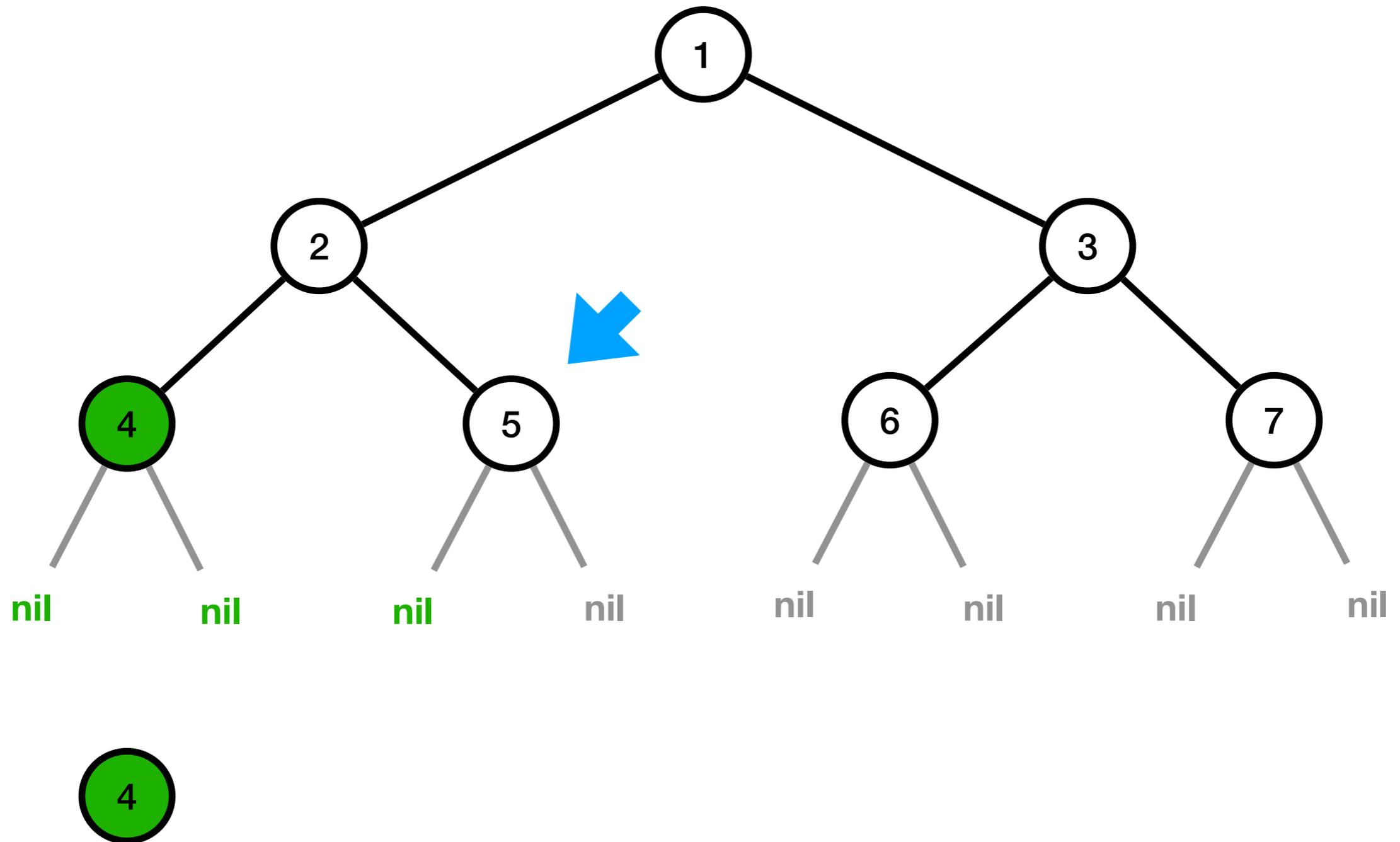
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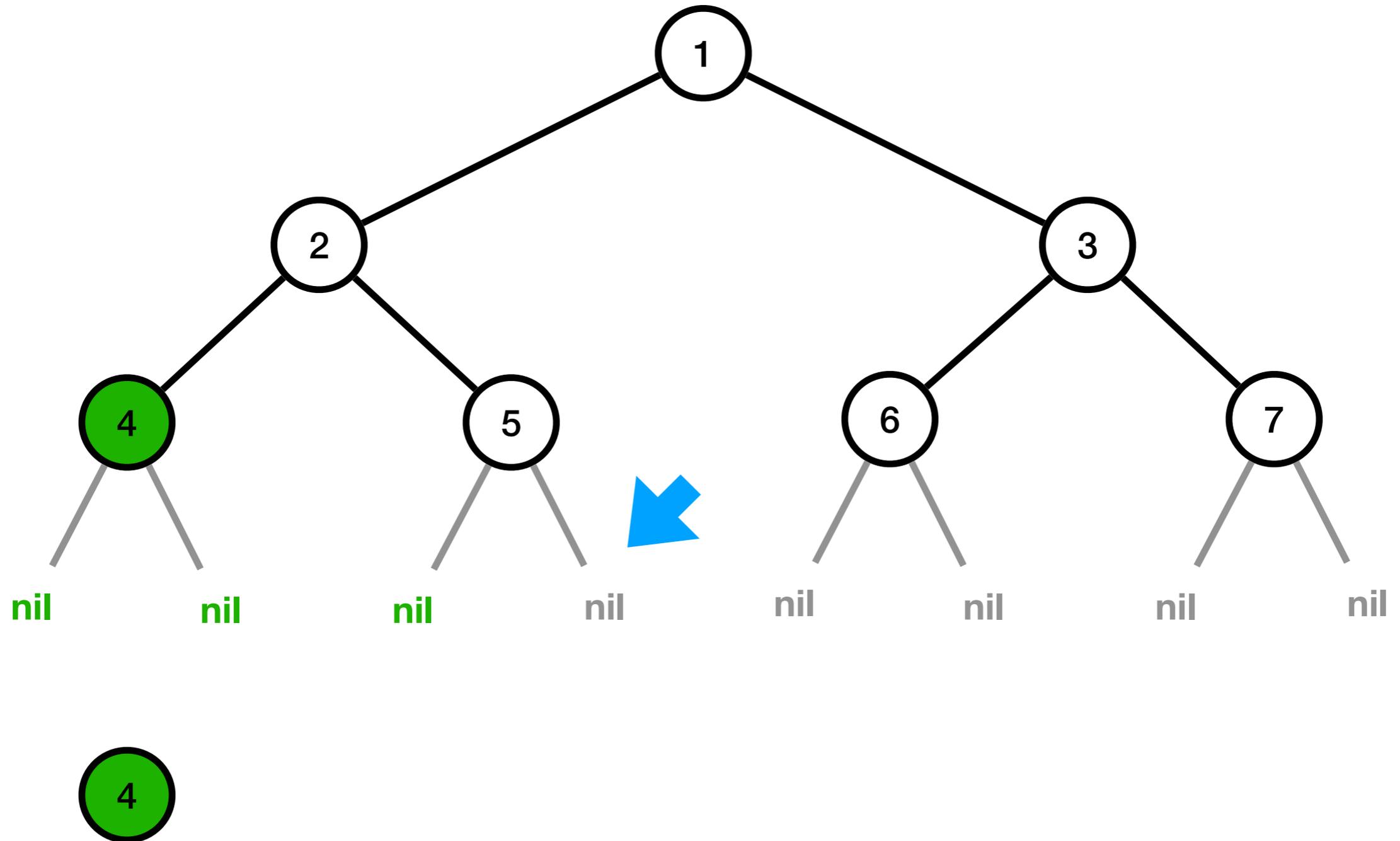
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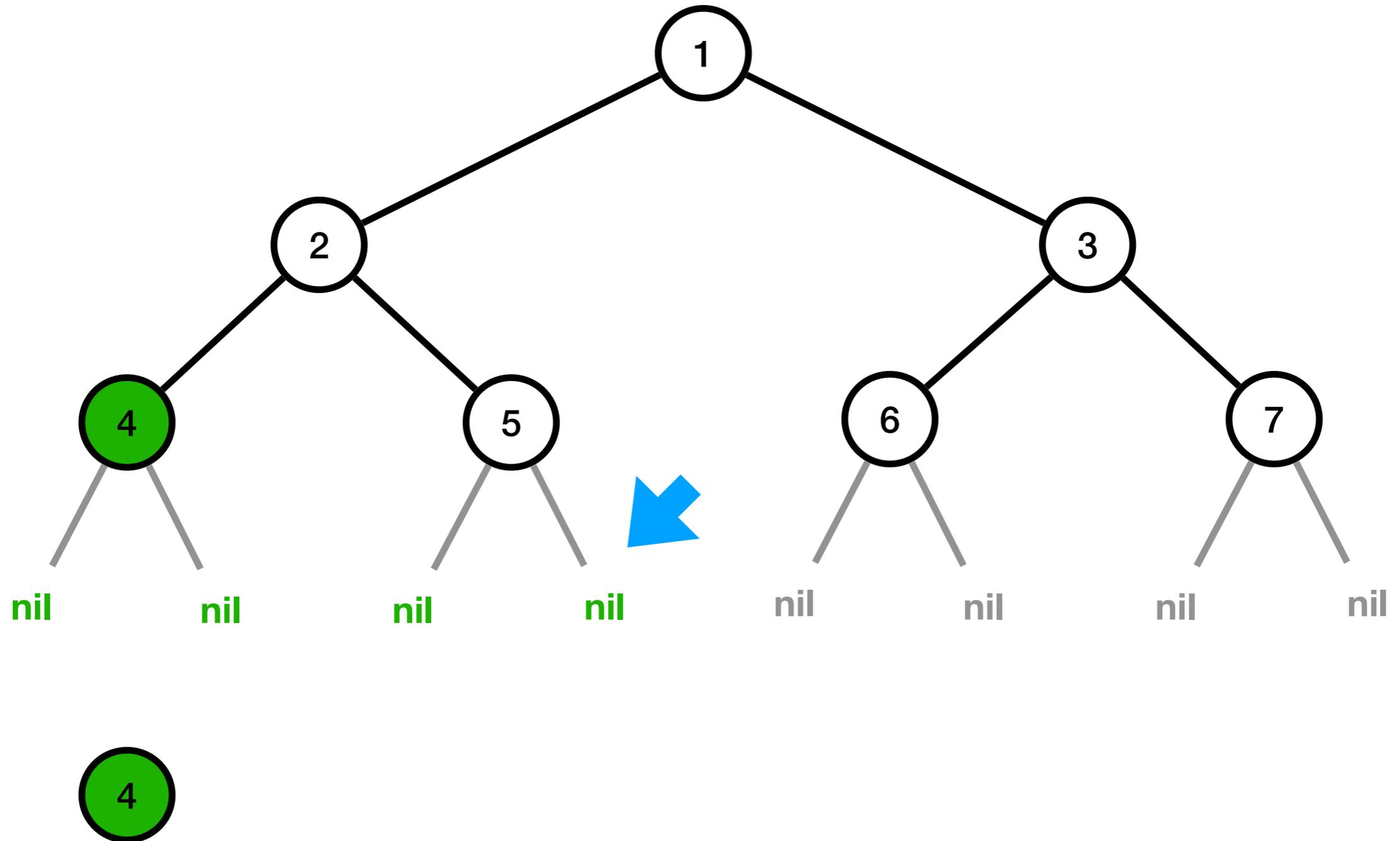
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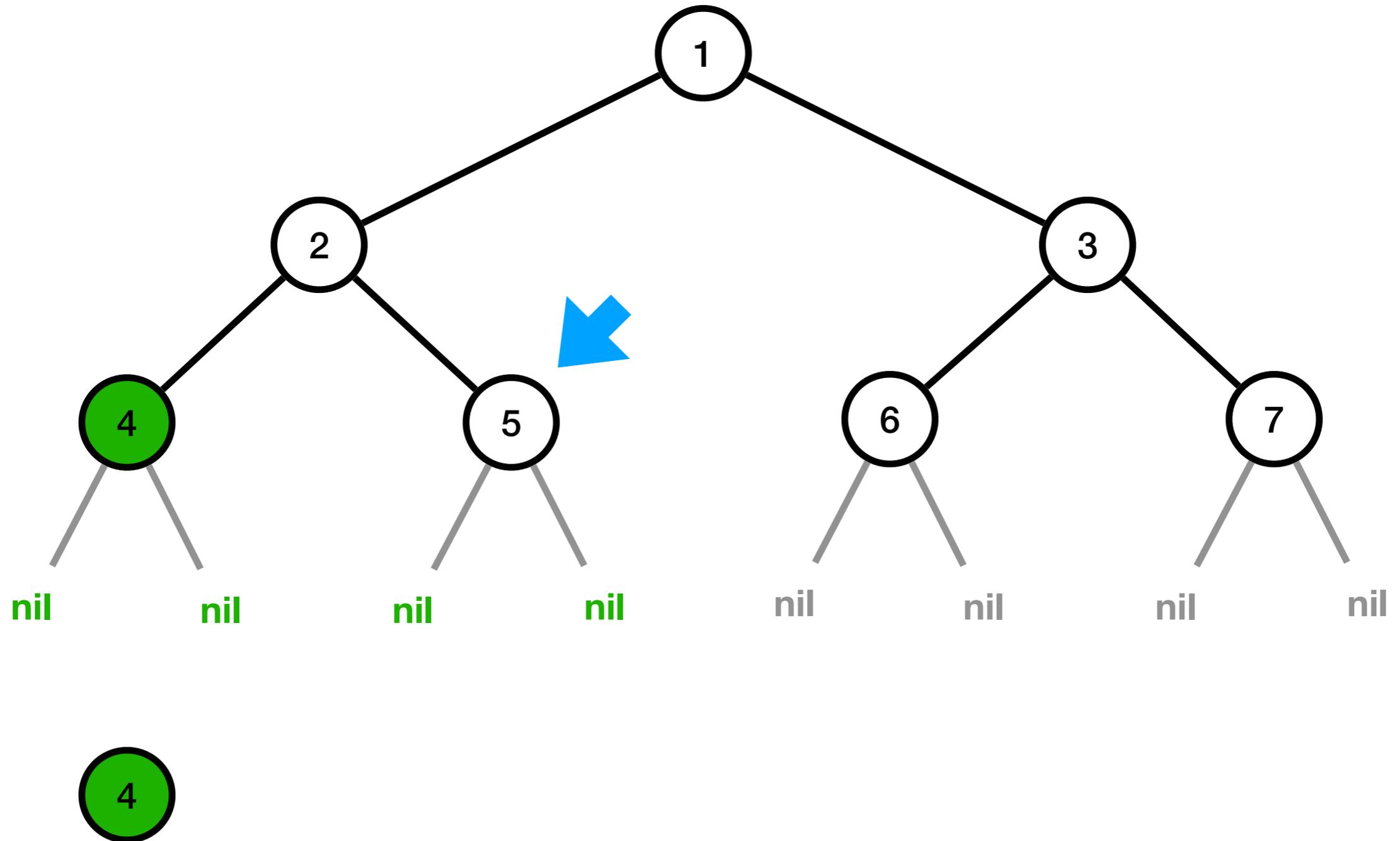
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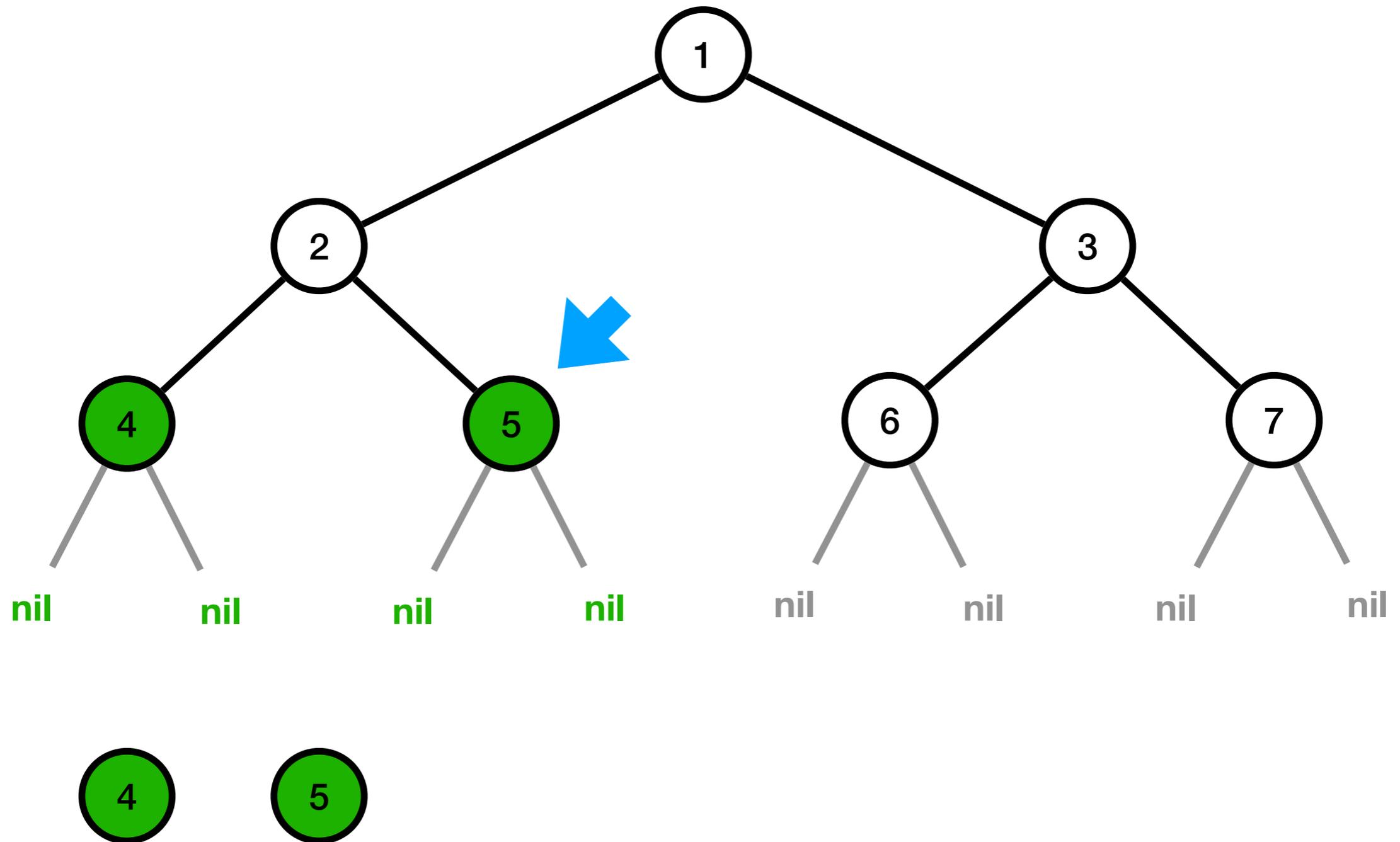
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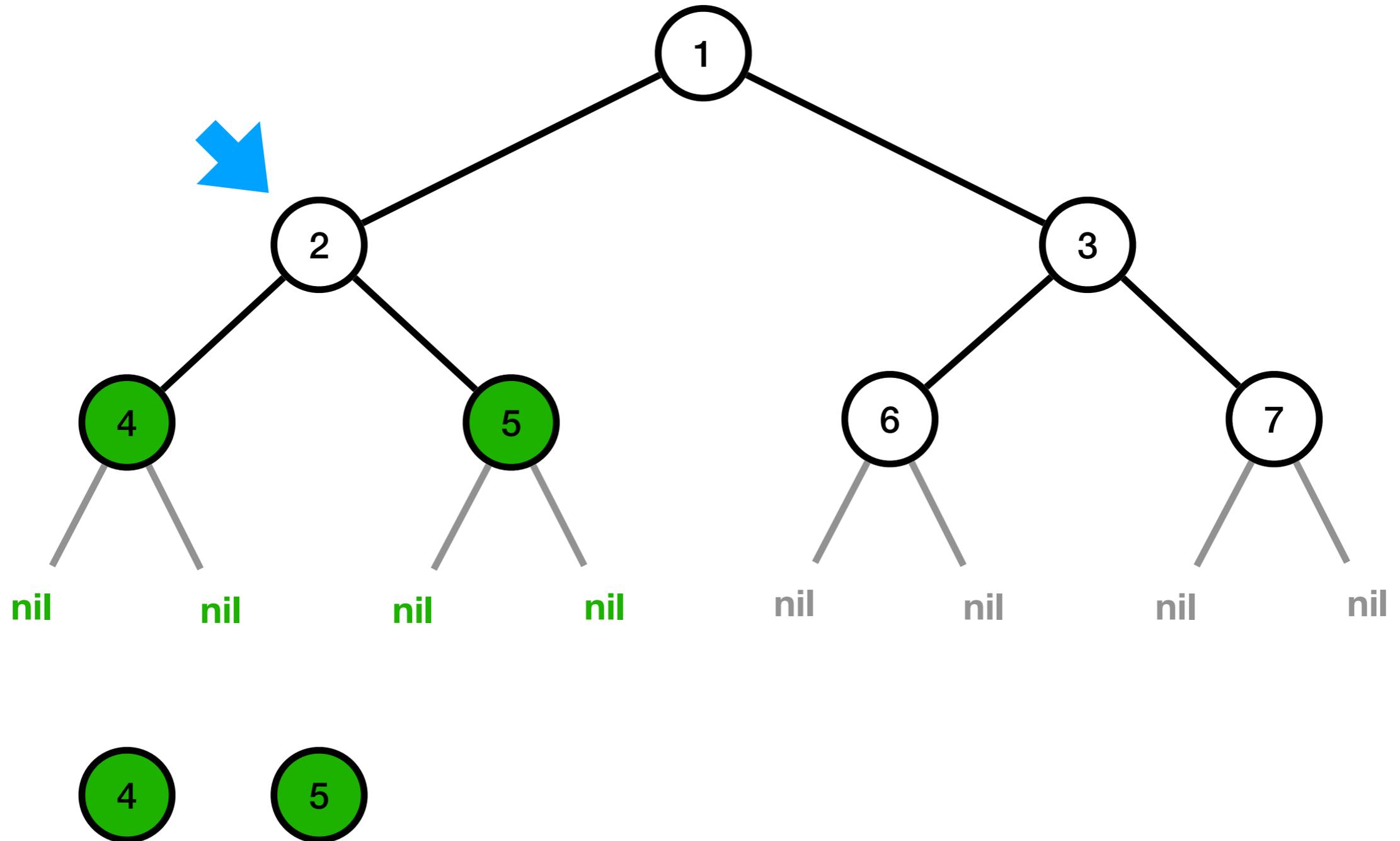
Parcours postfixe



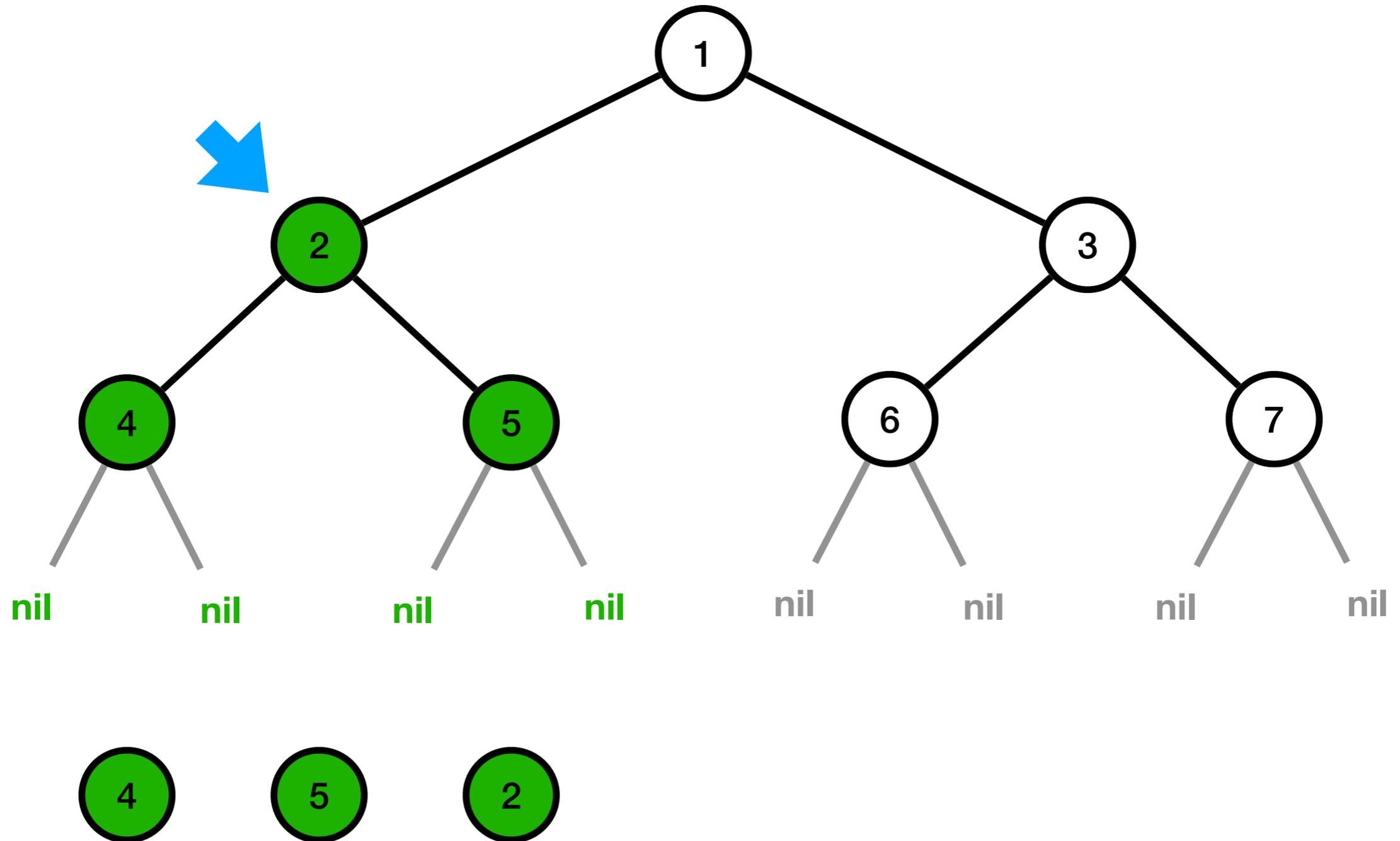
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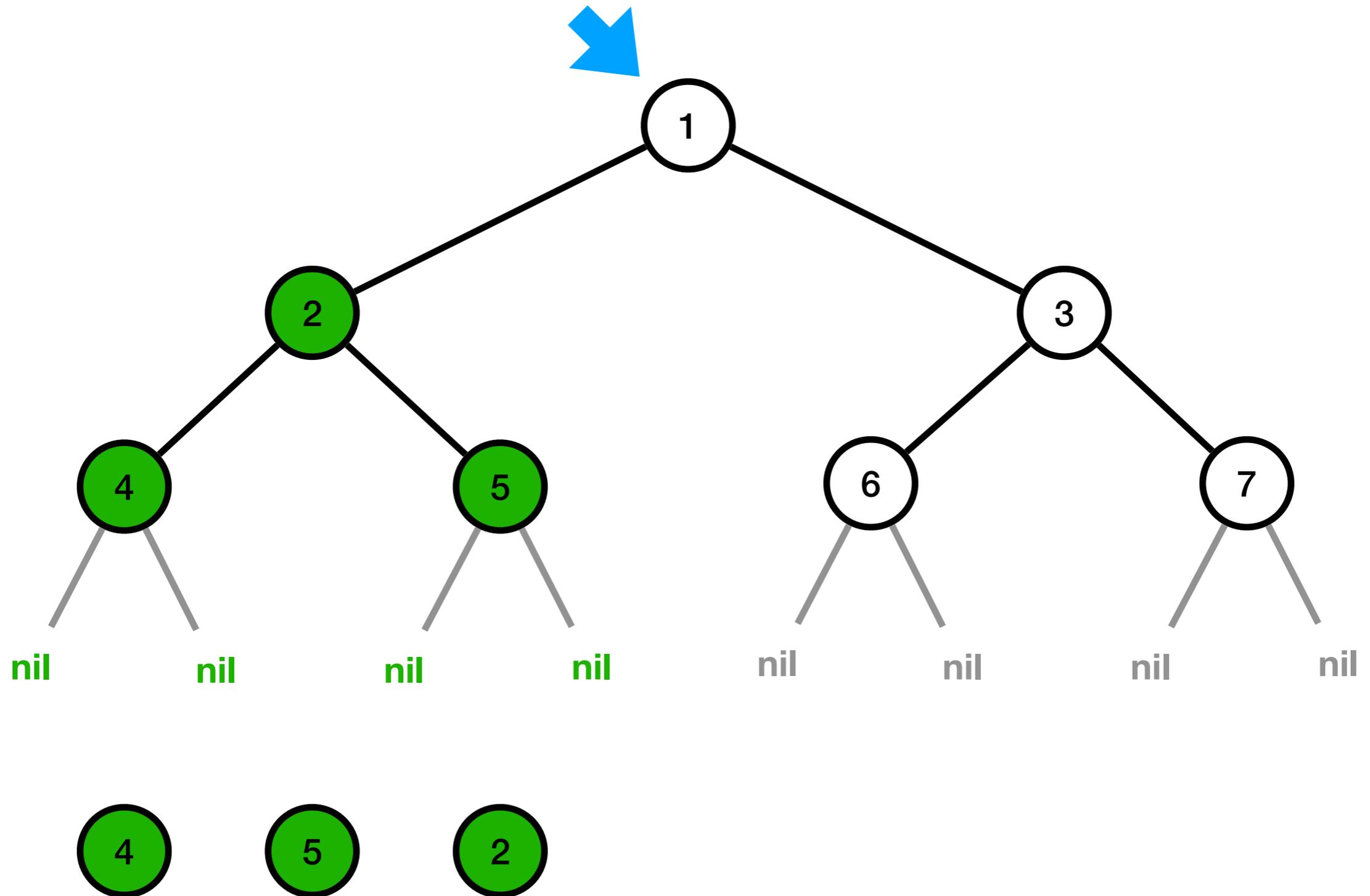
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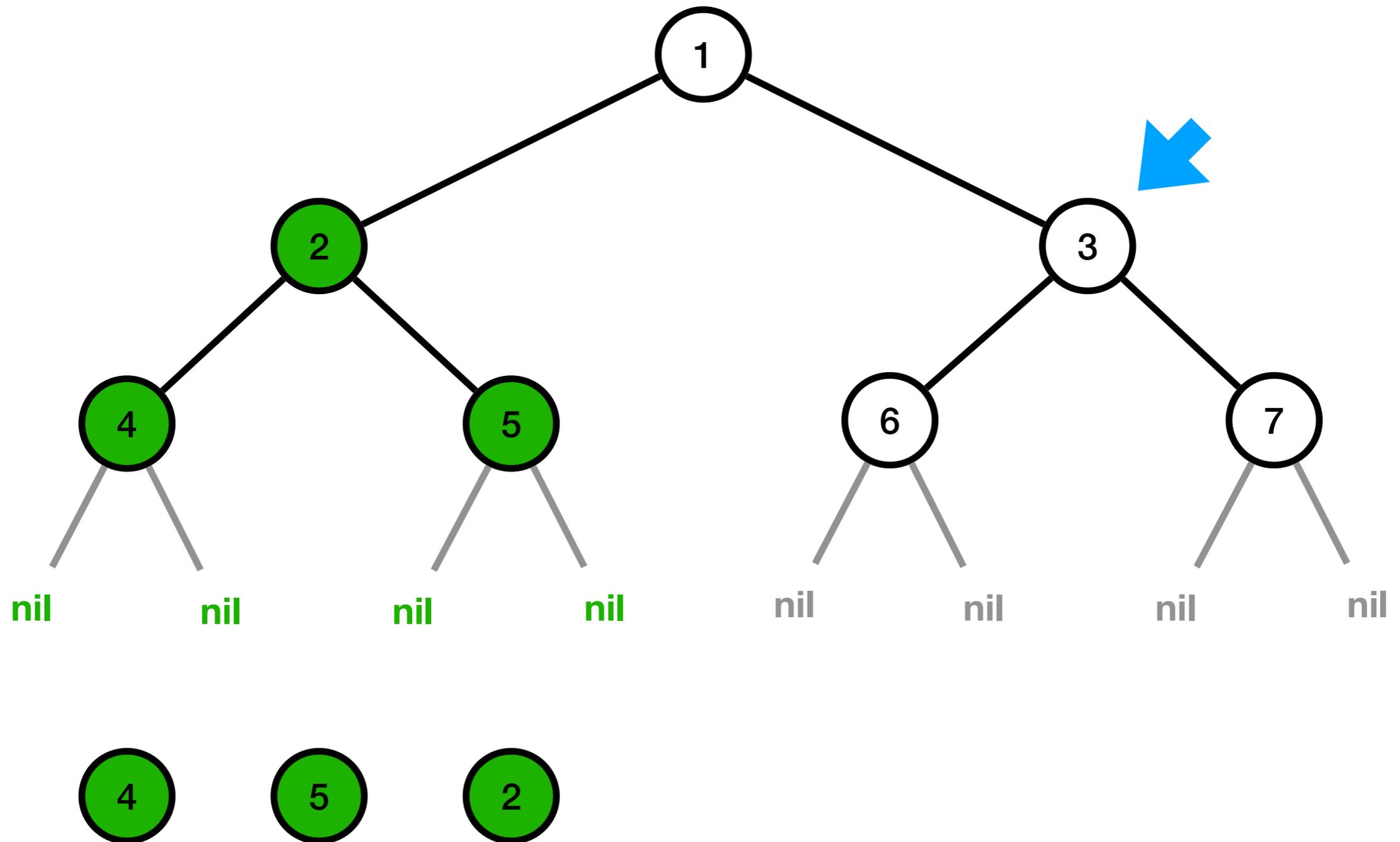
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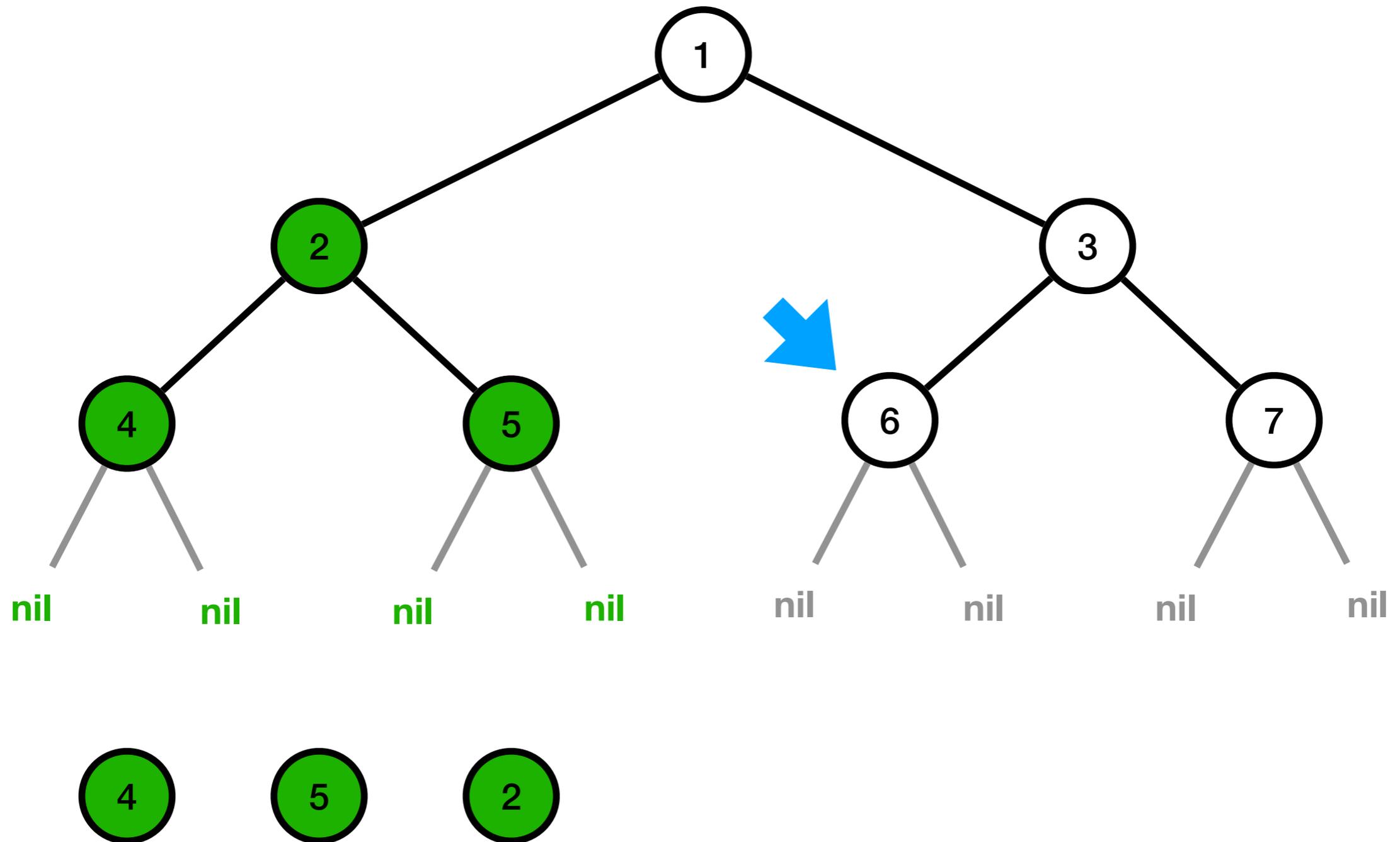
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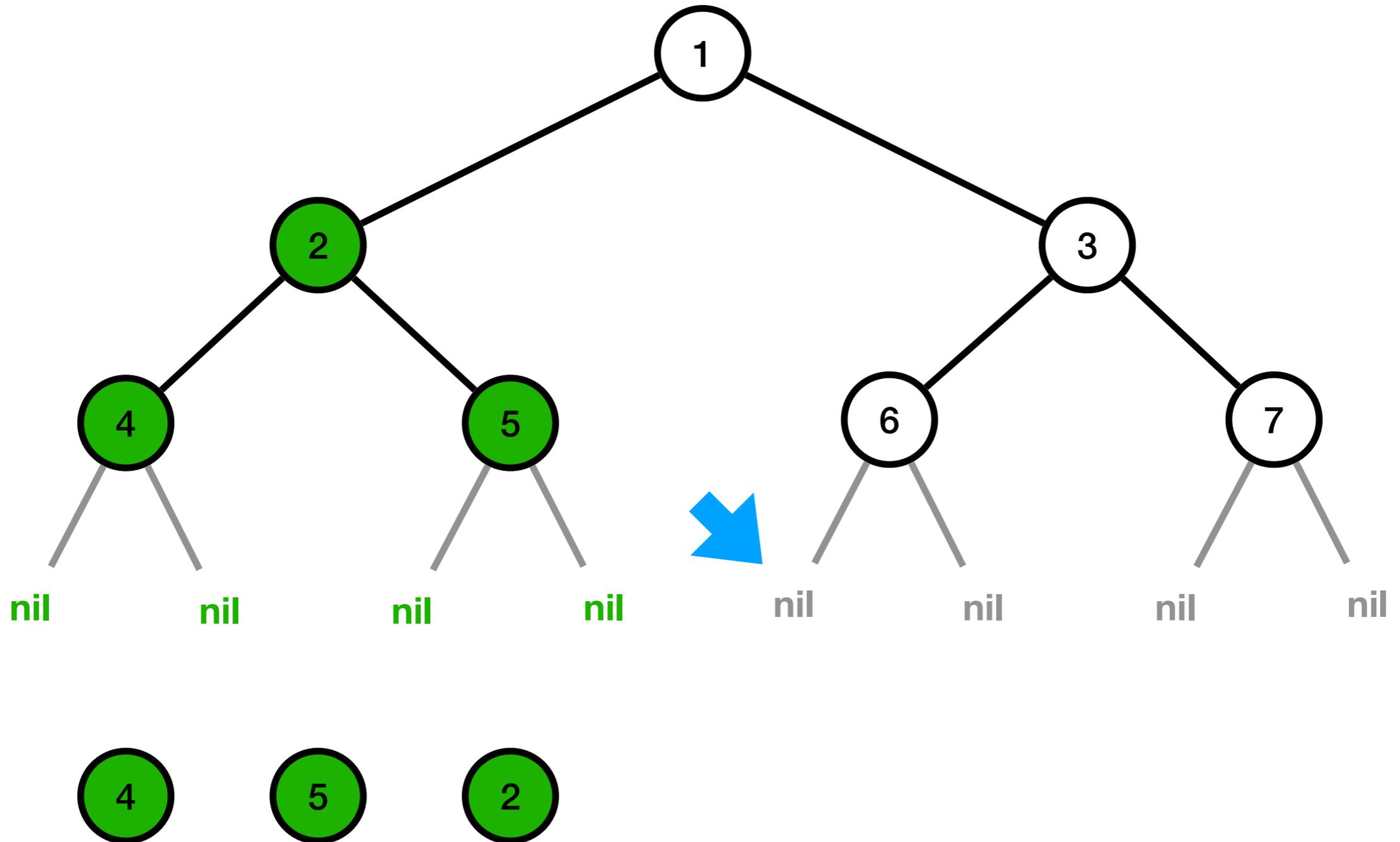
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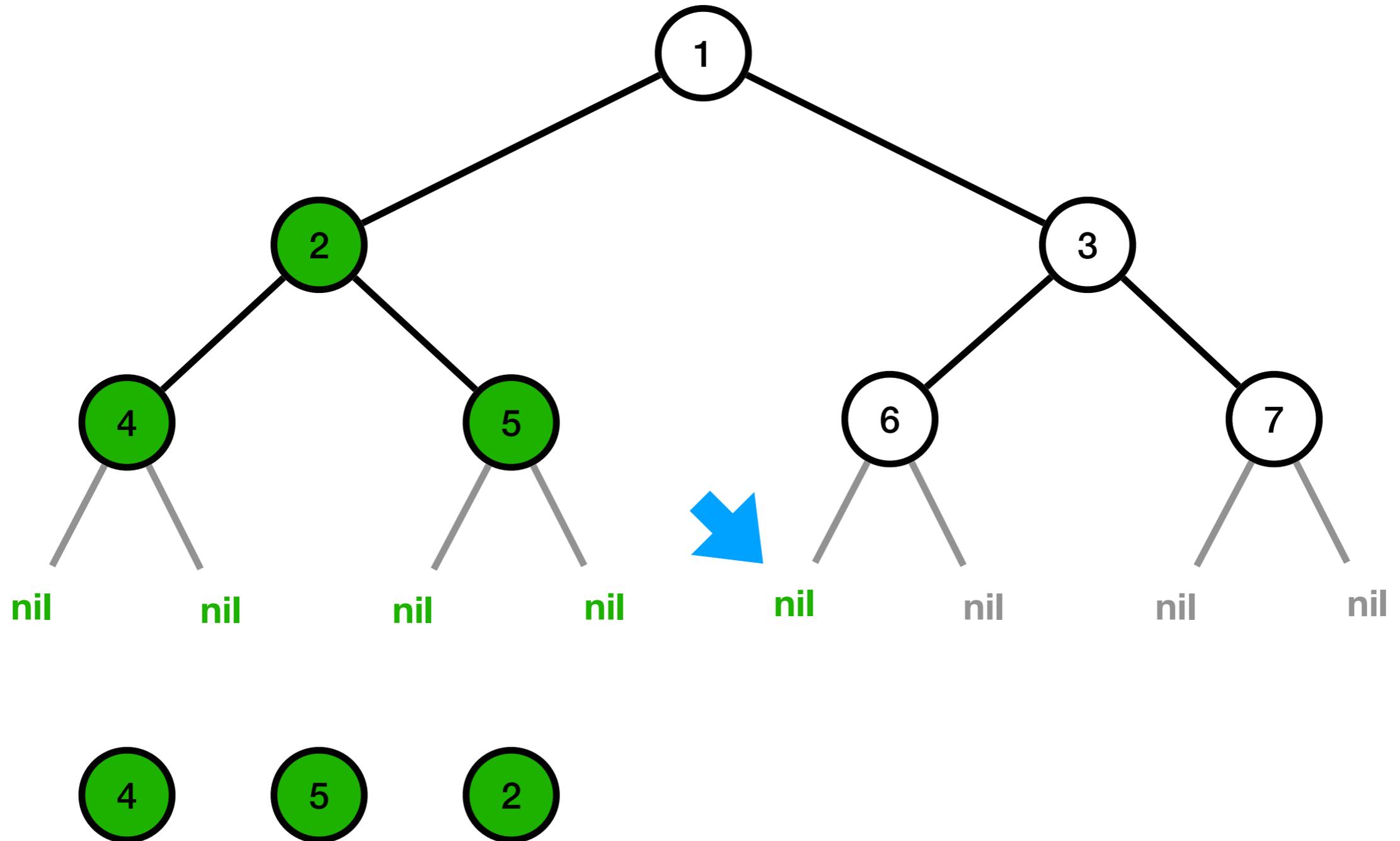
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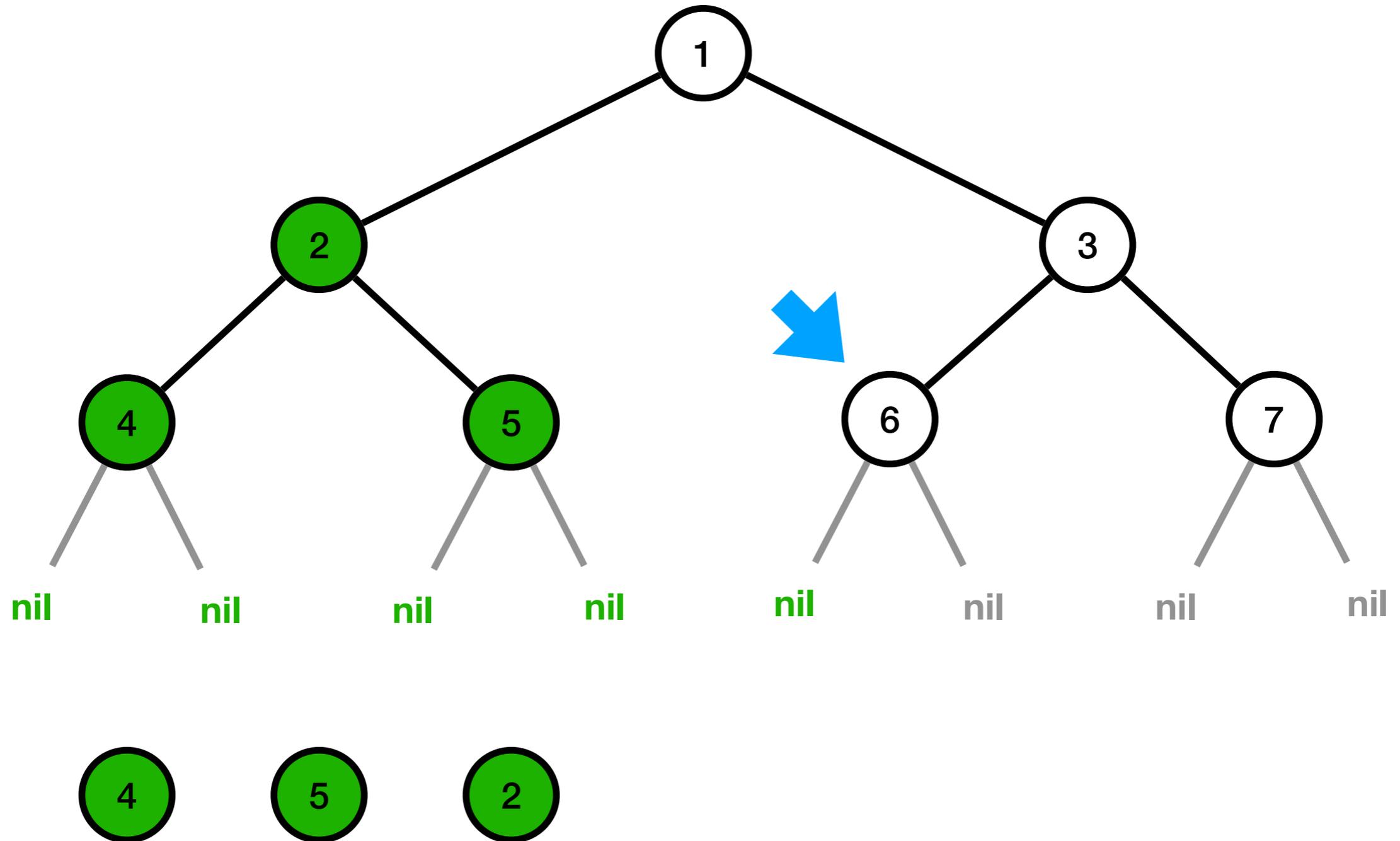
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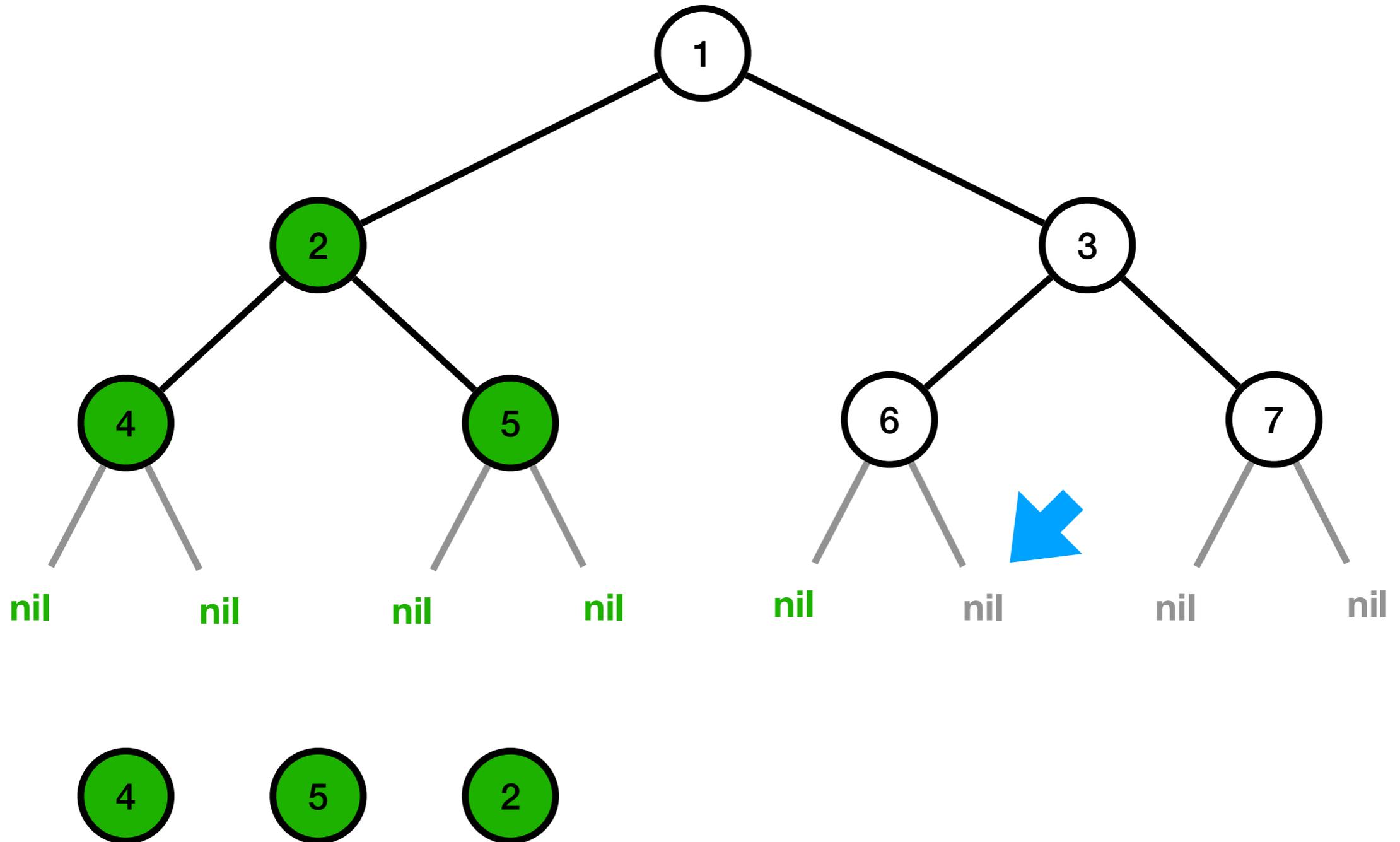
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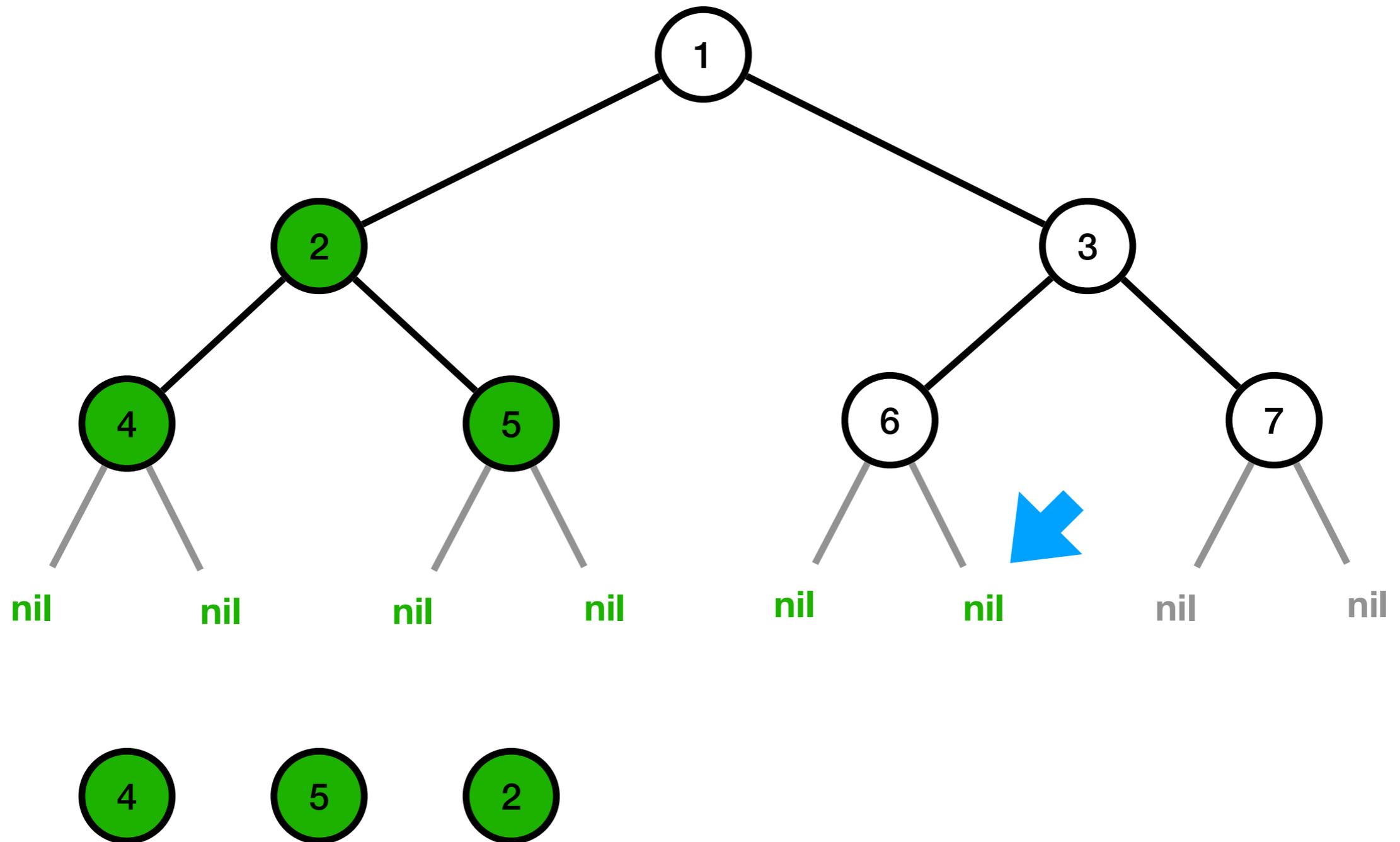
Parcours postfixe



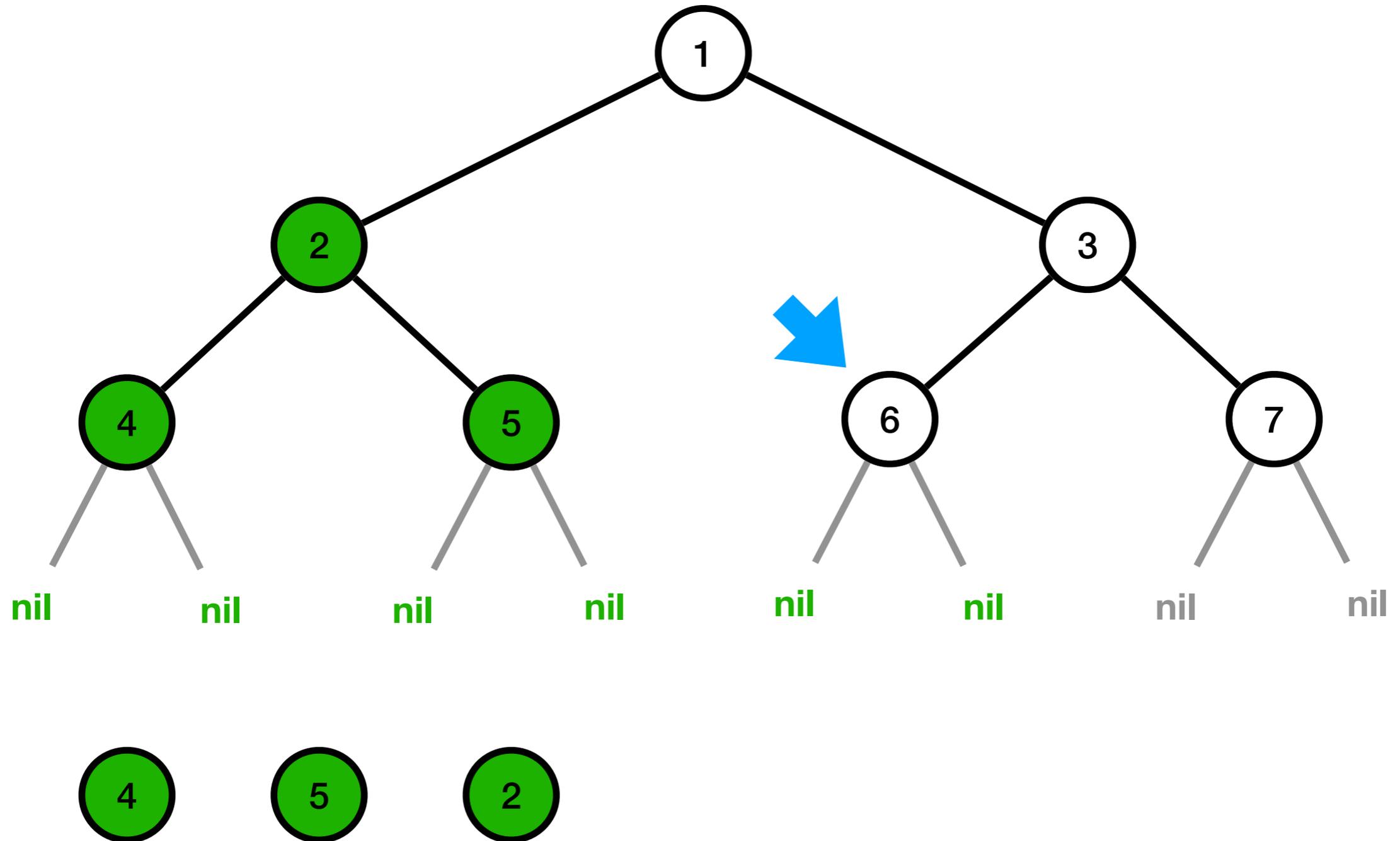
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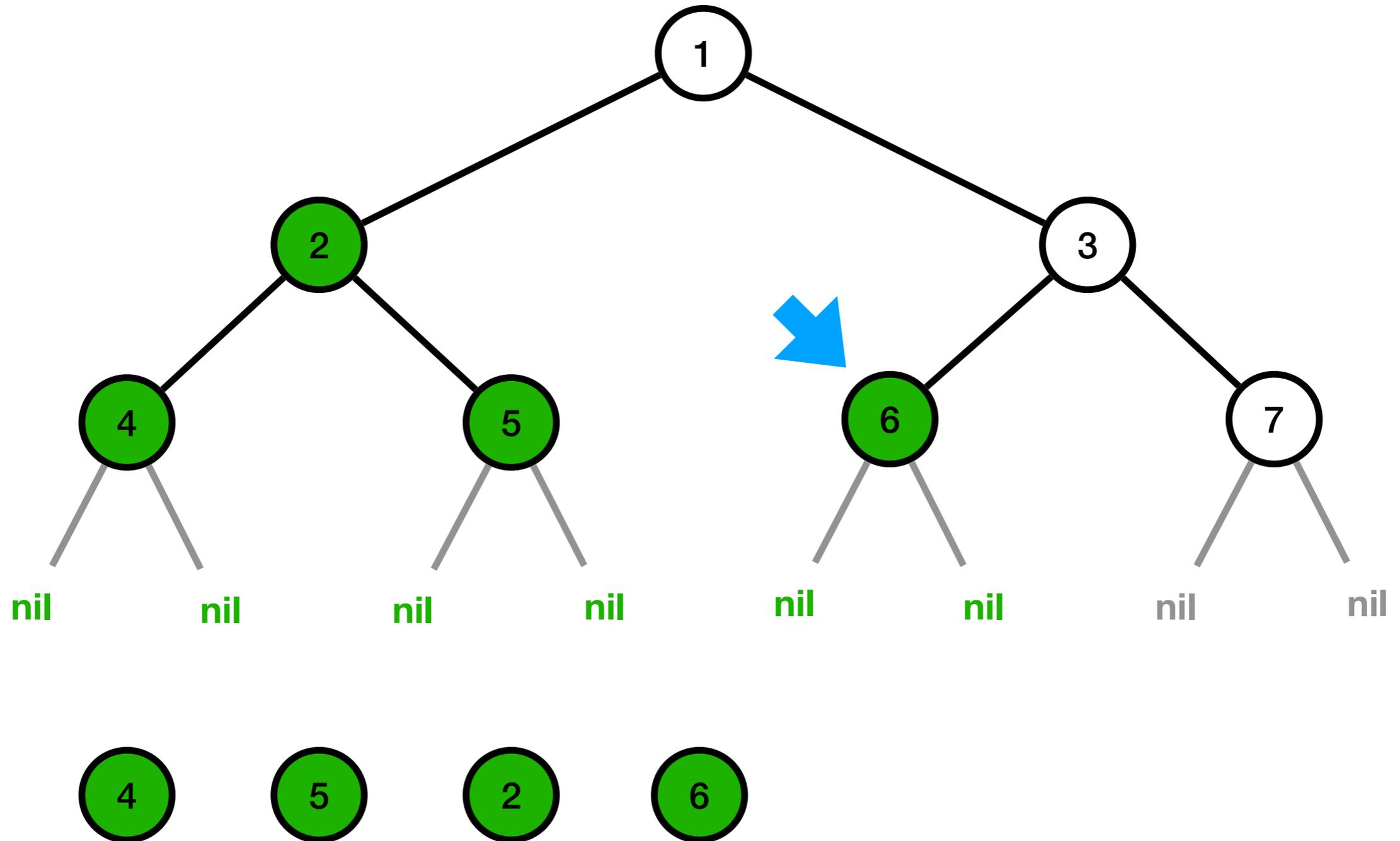
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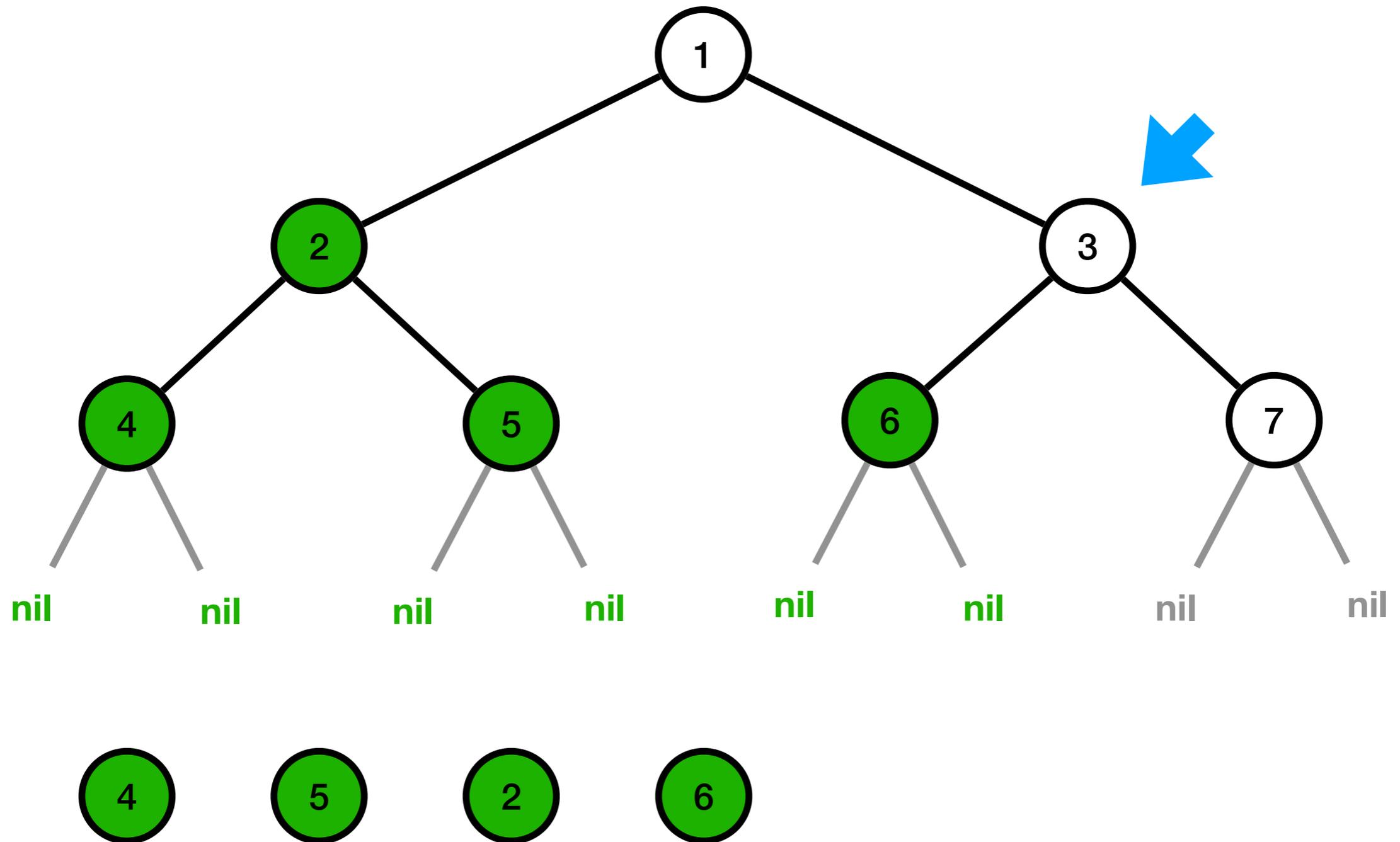
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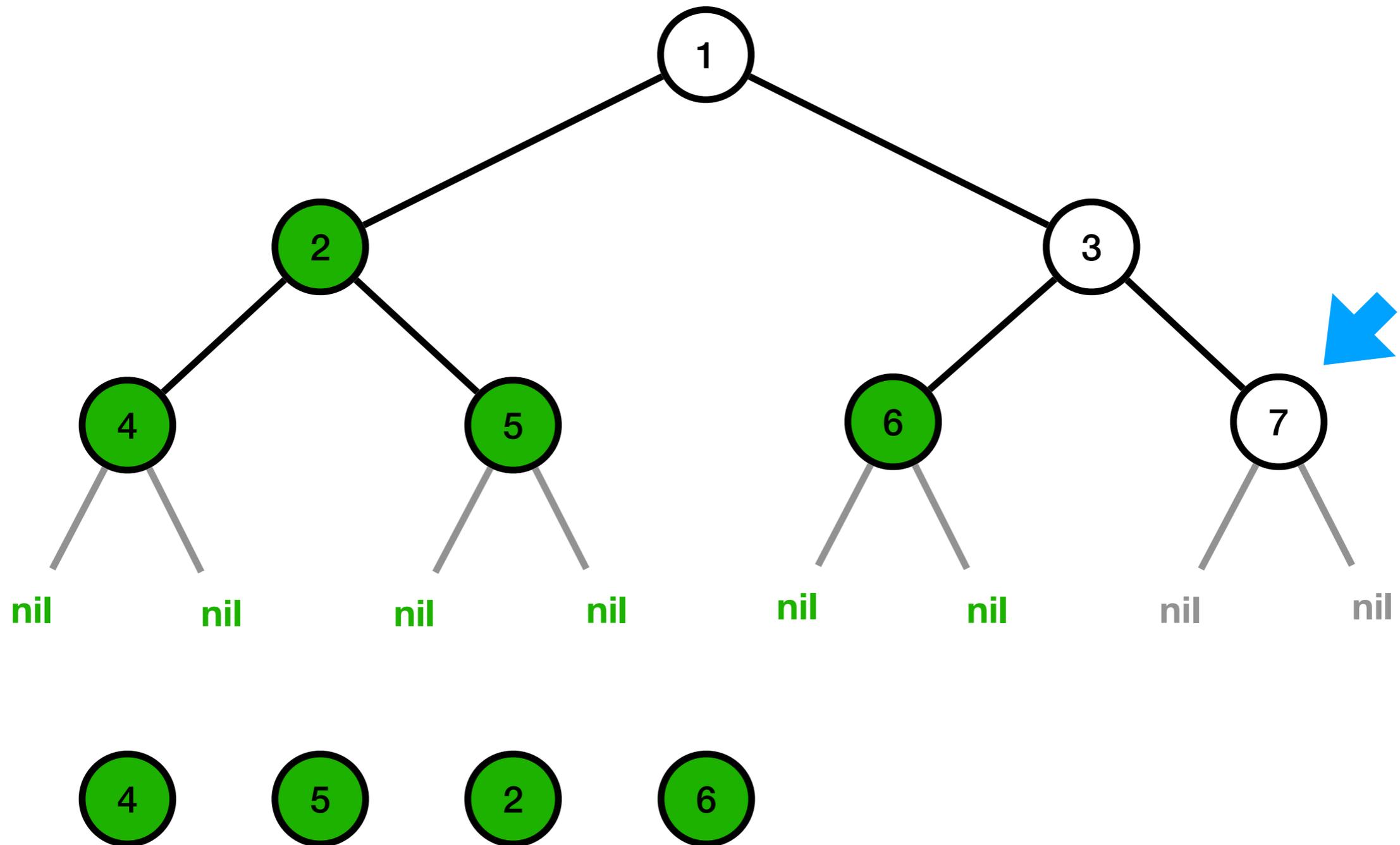
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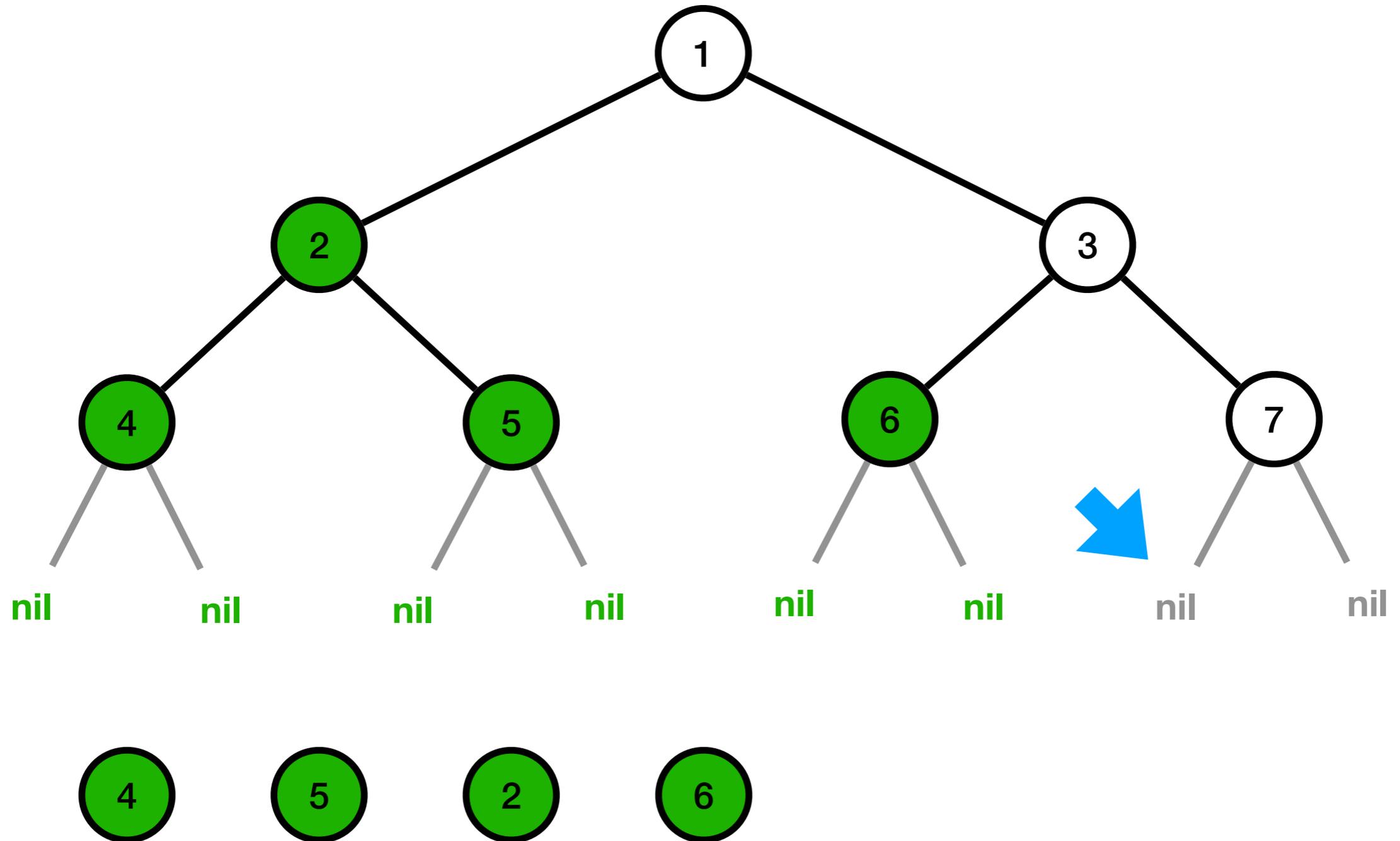
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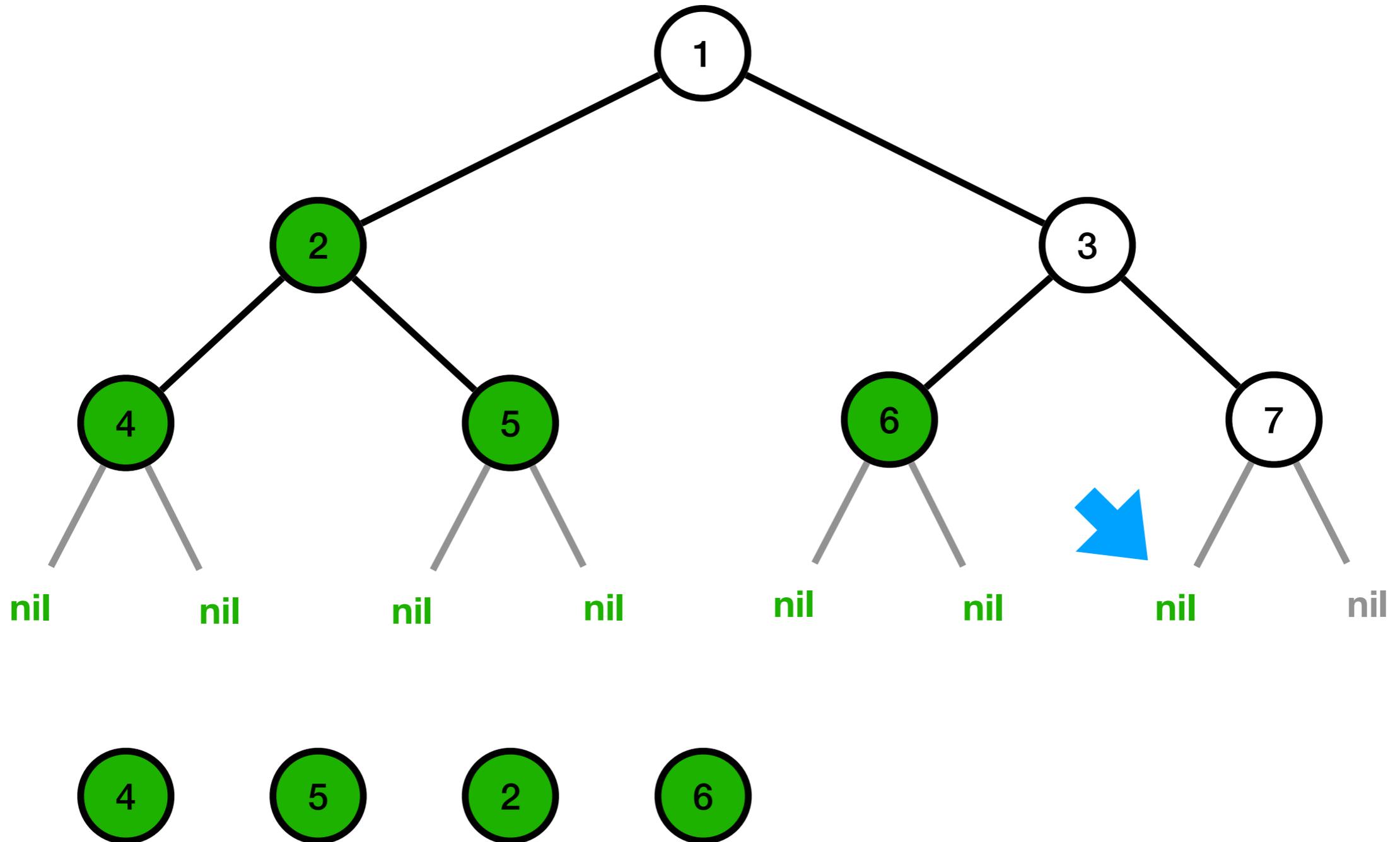
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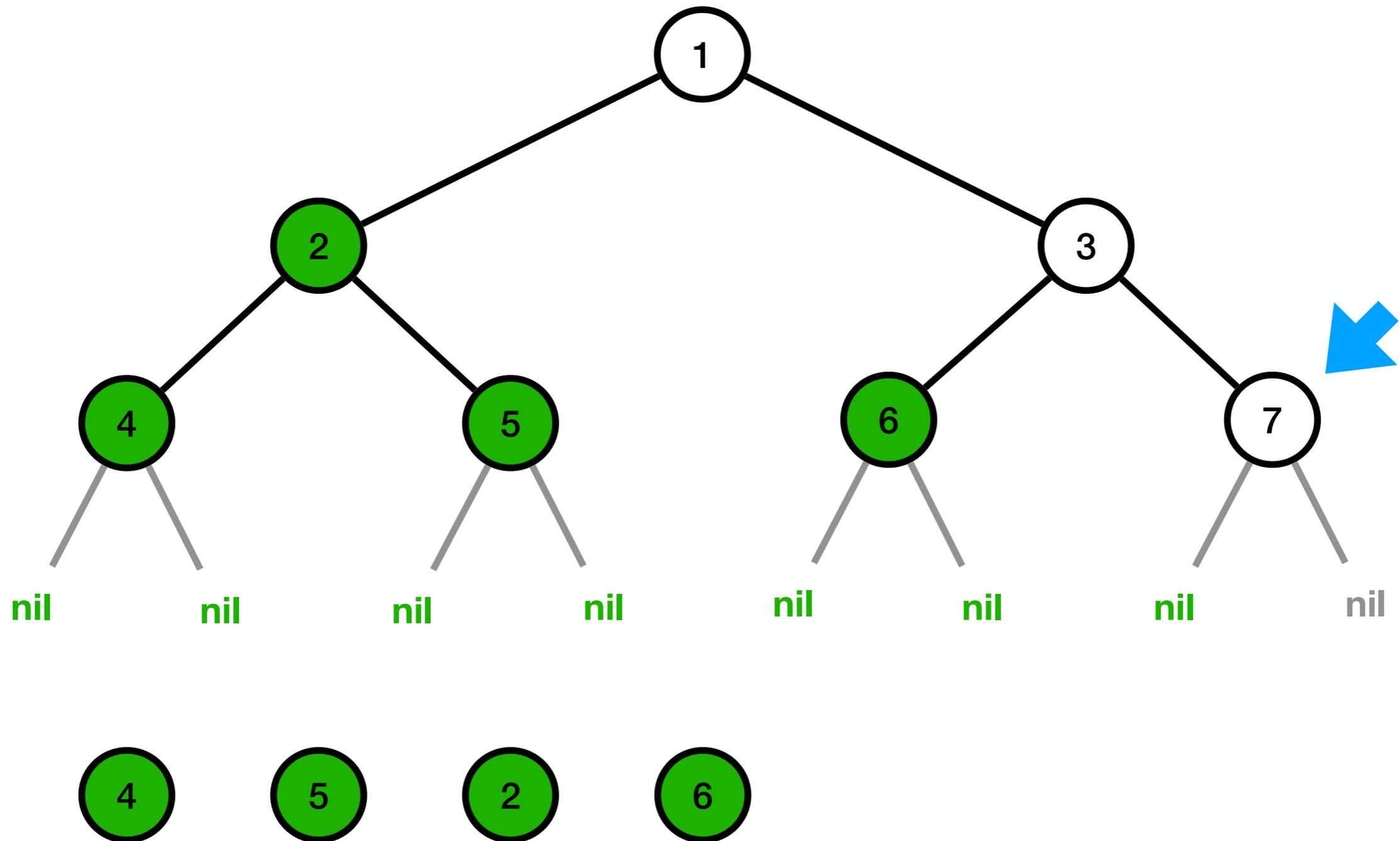
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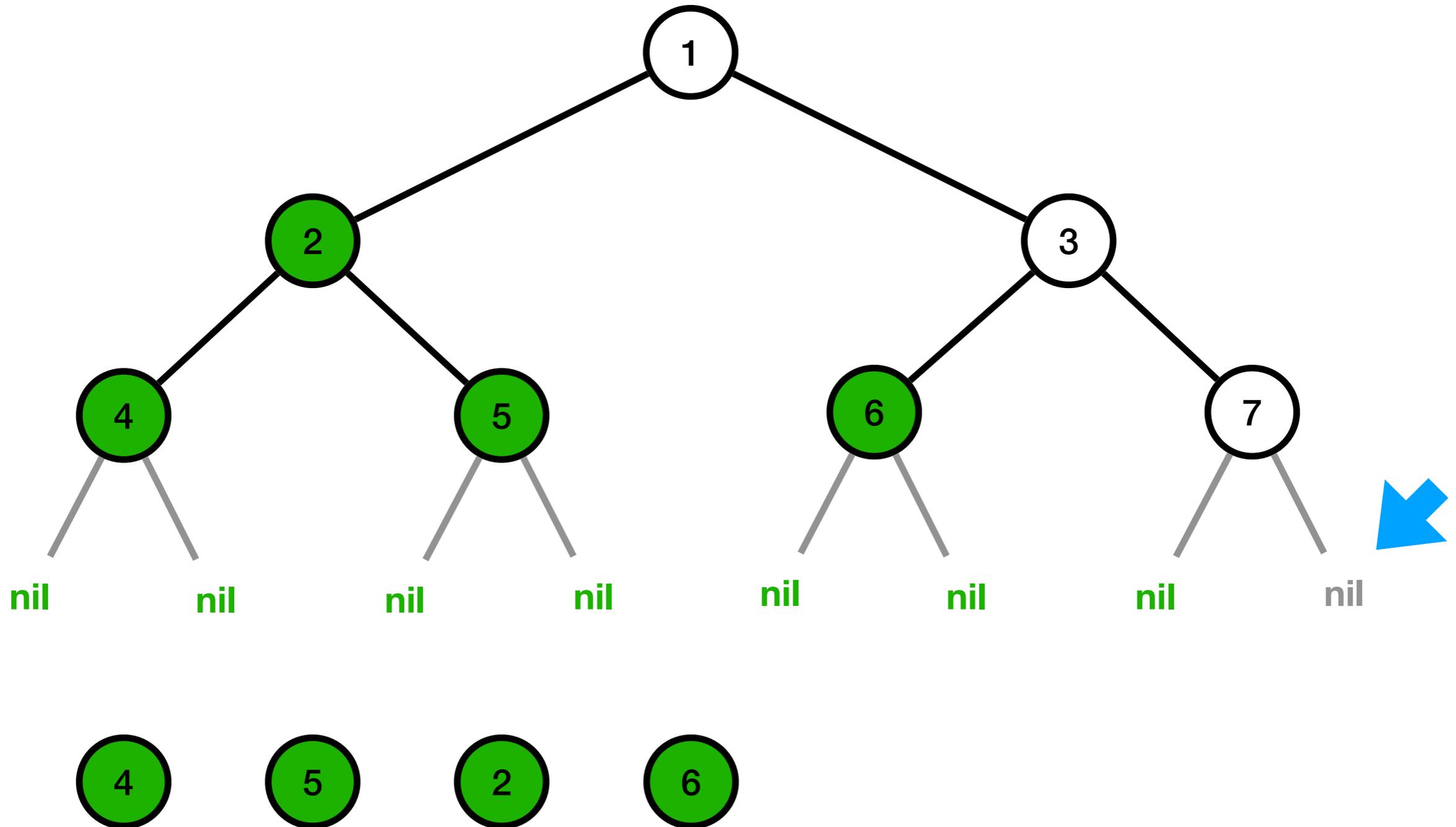
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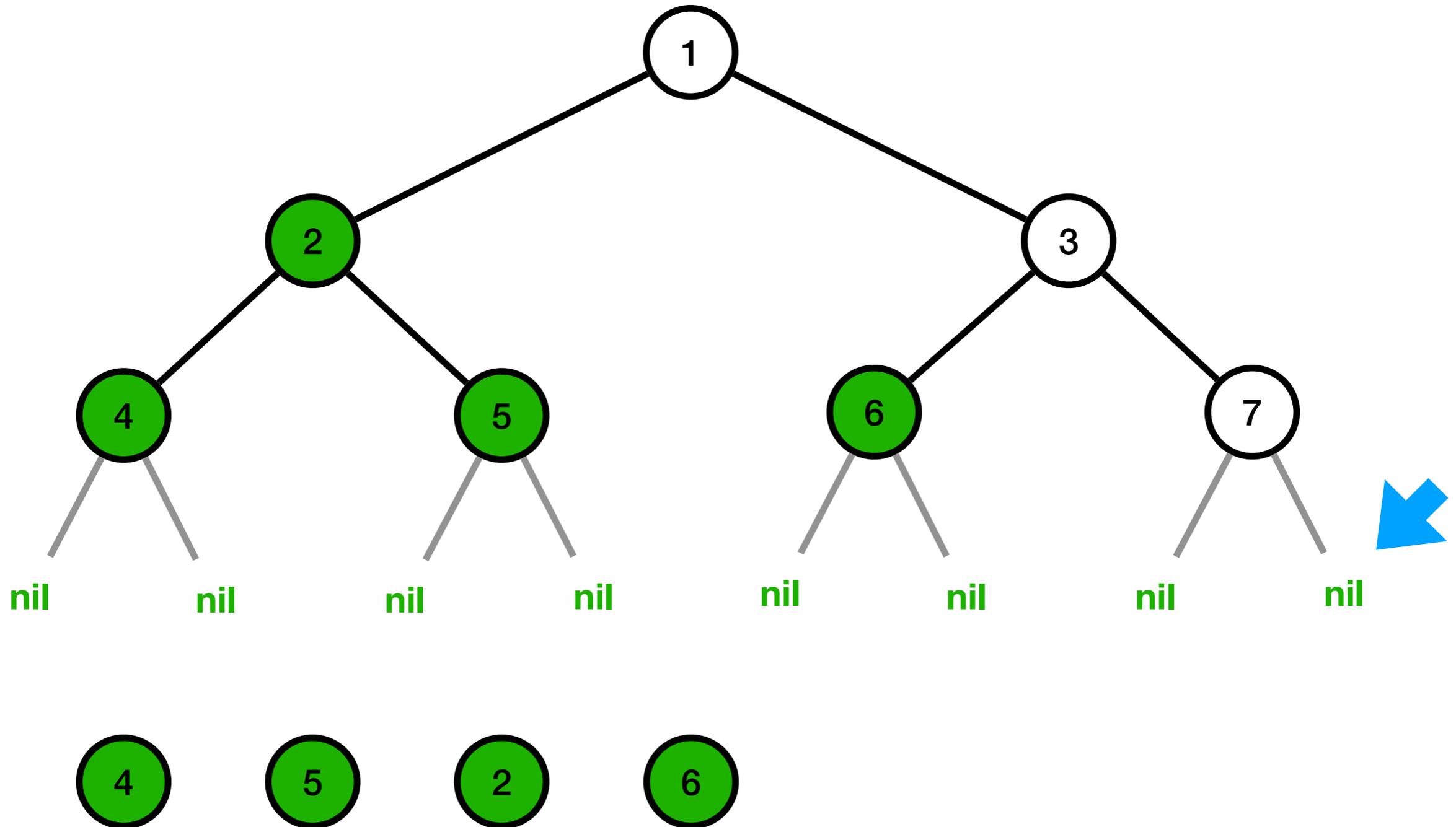
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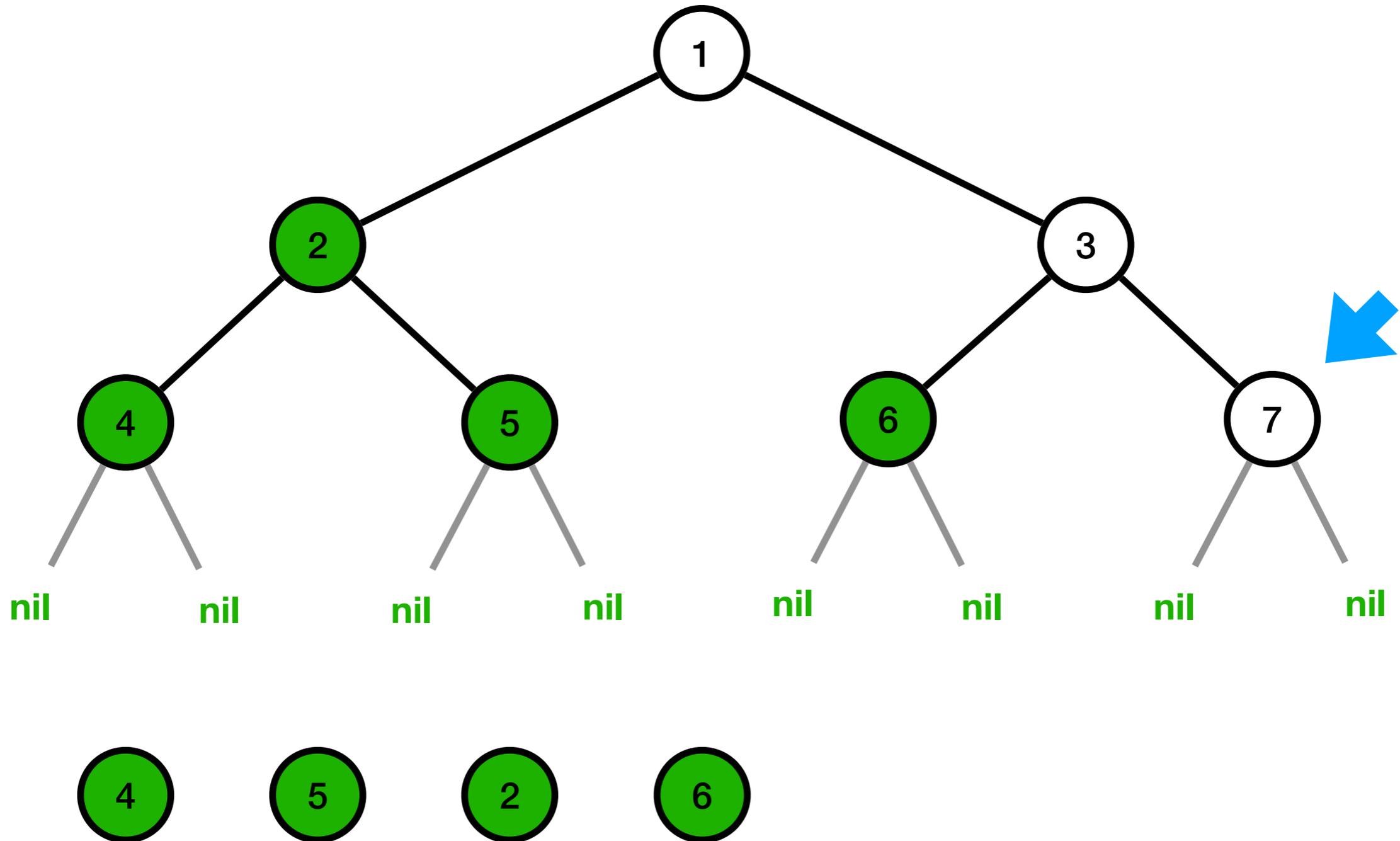
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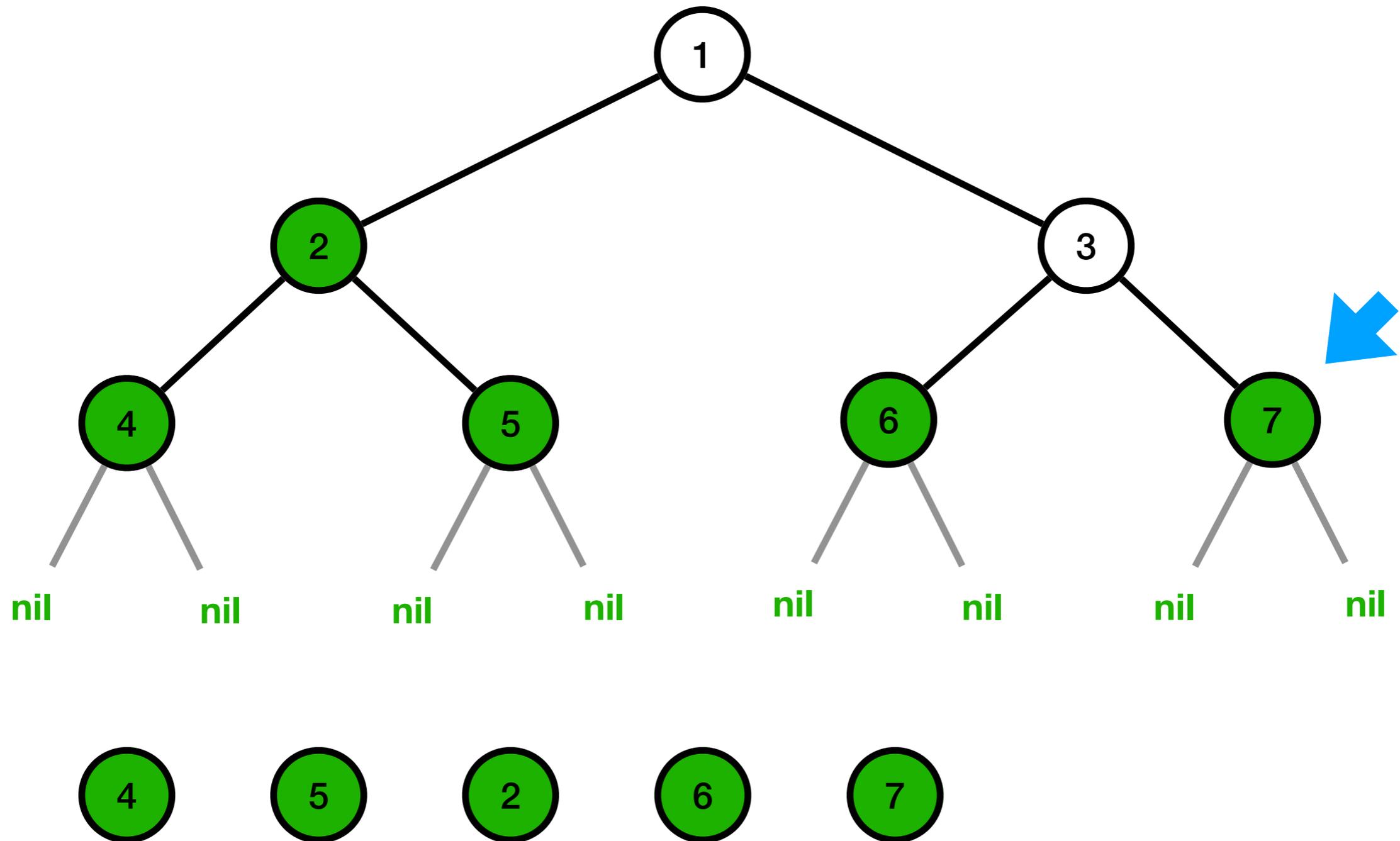
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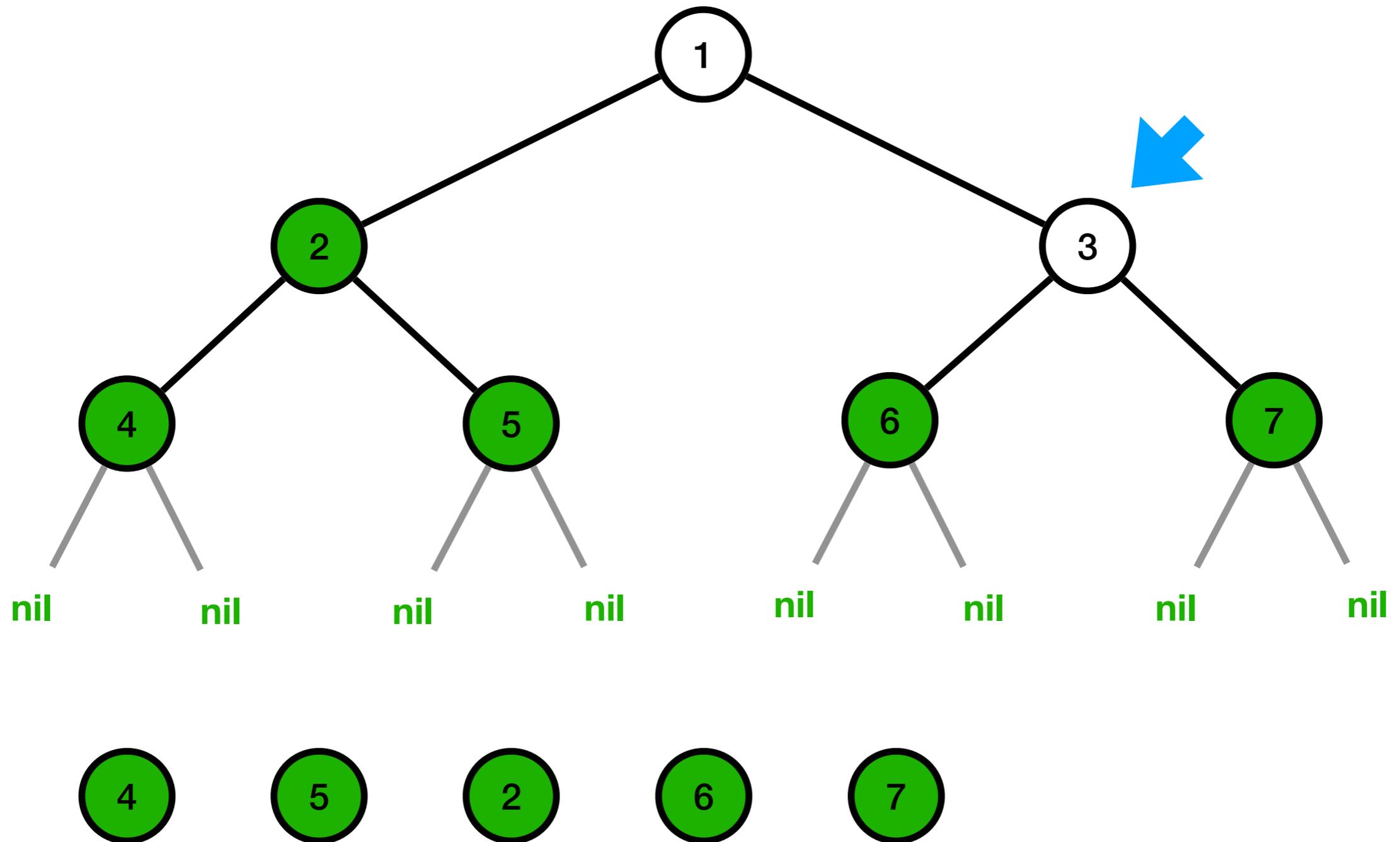
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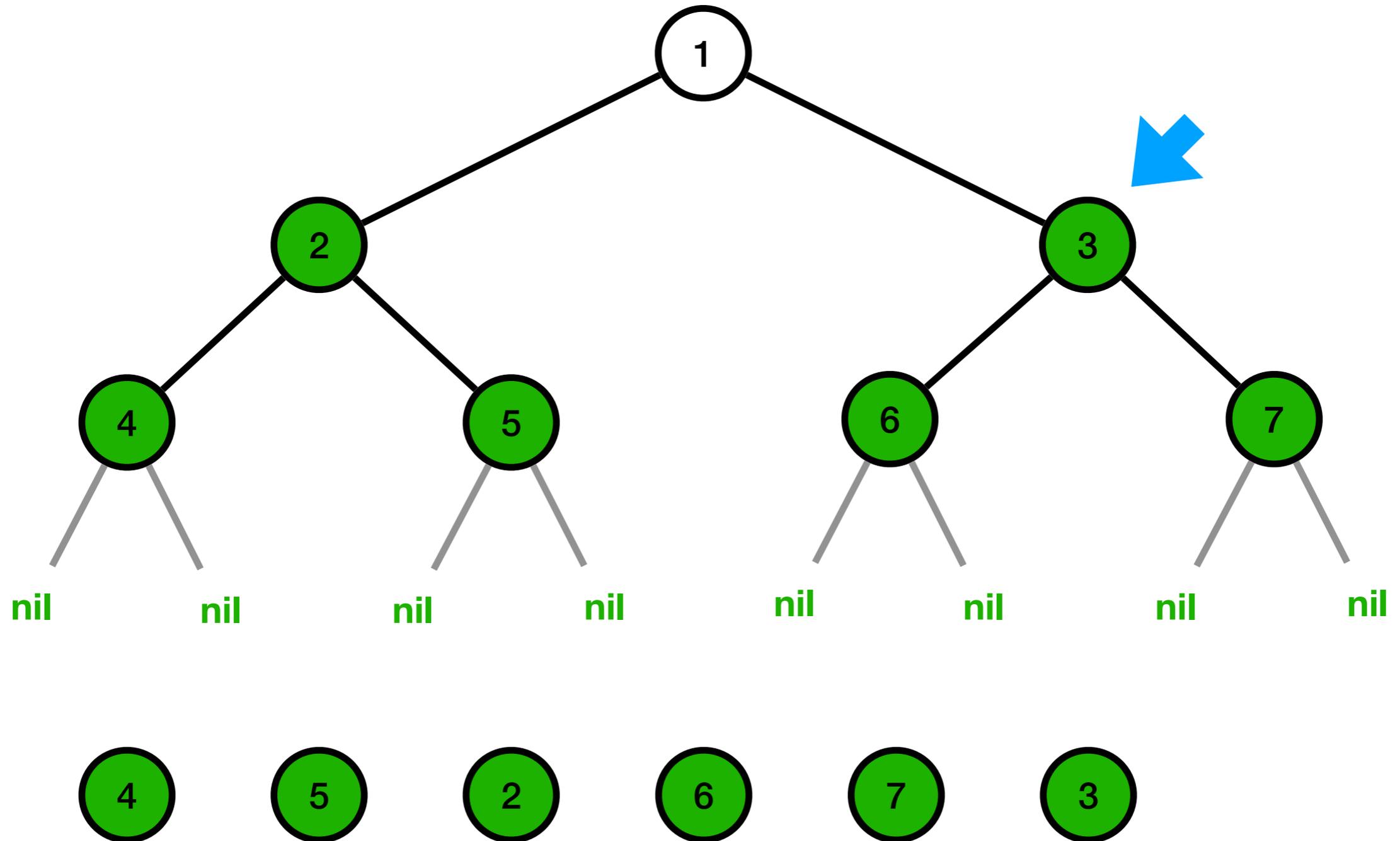
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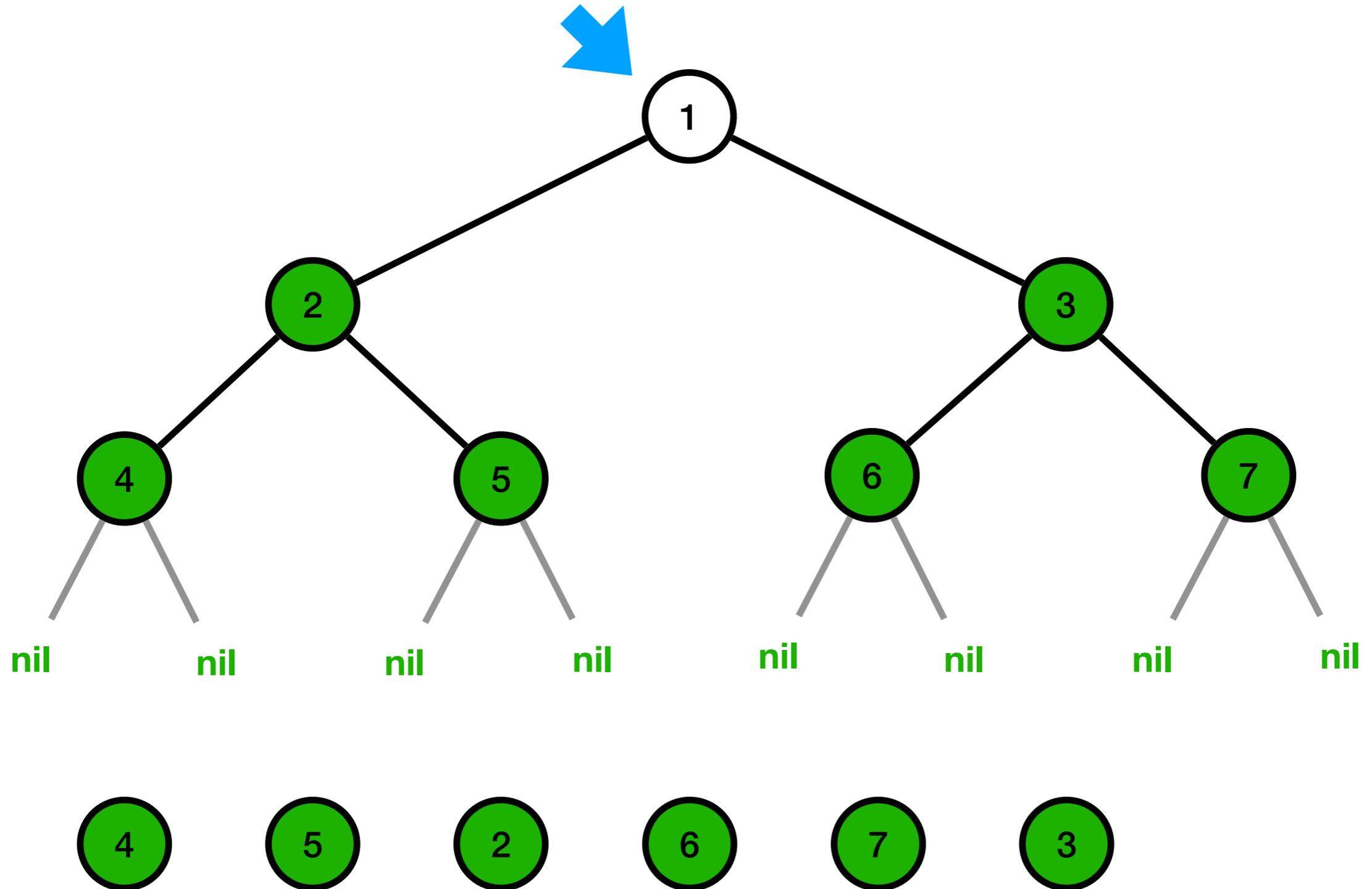
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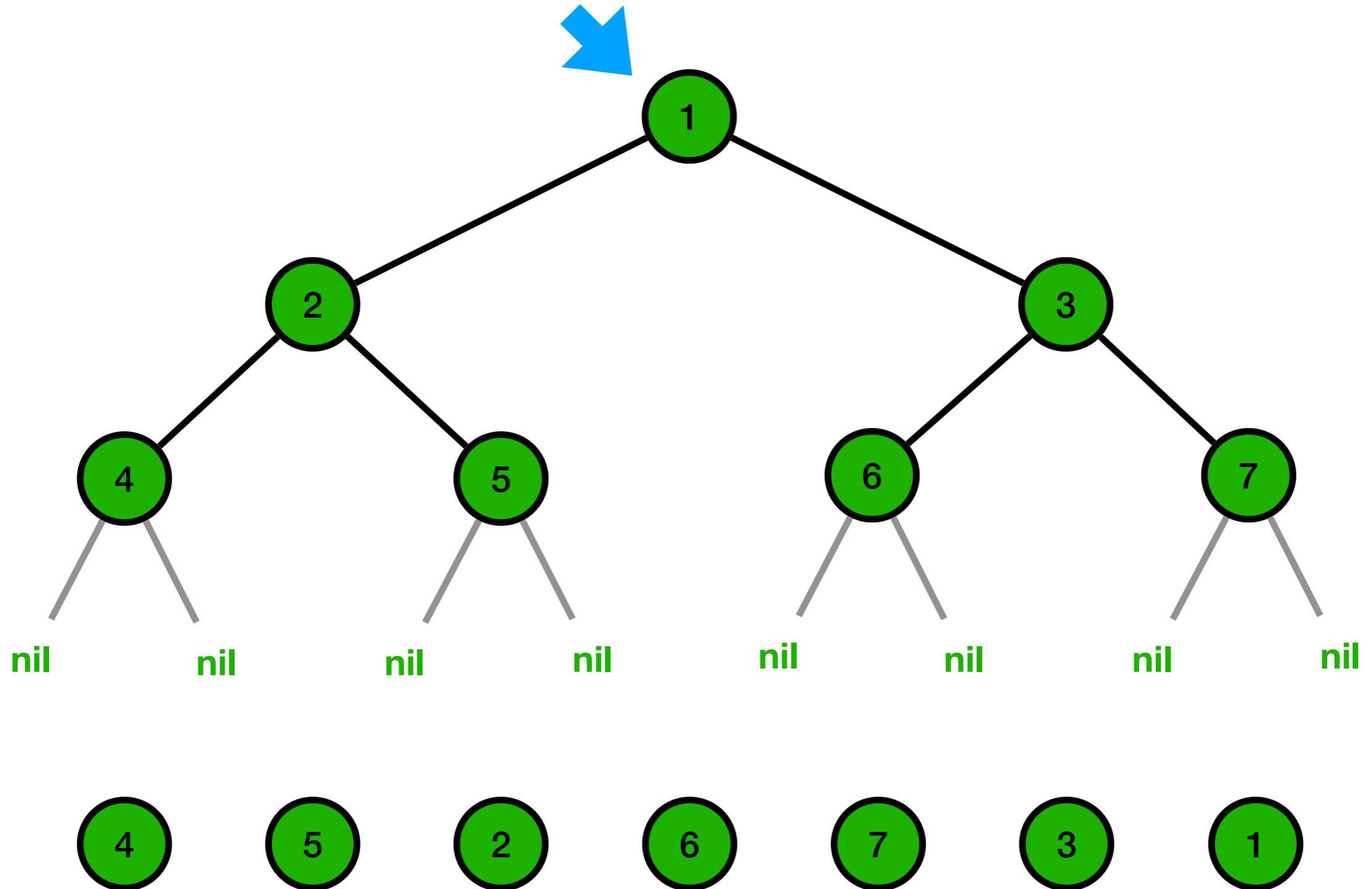
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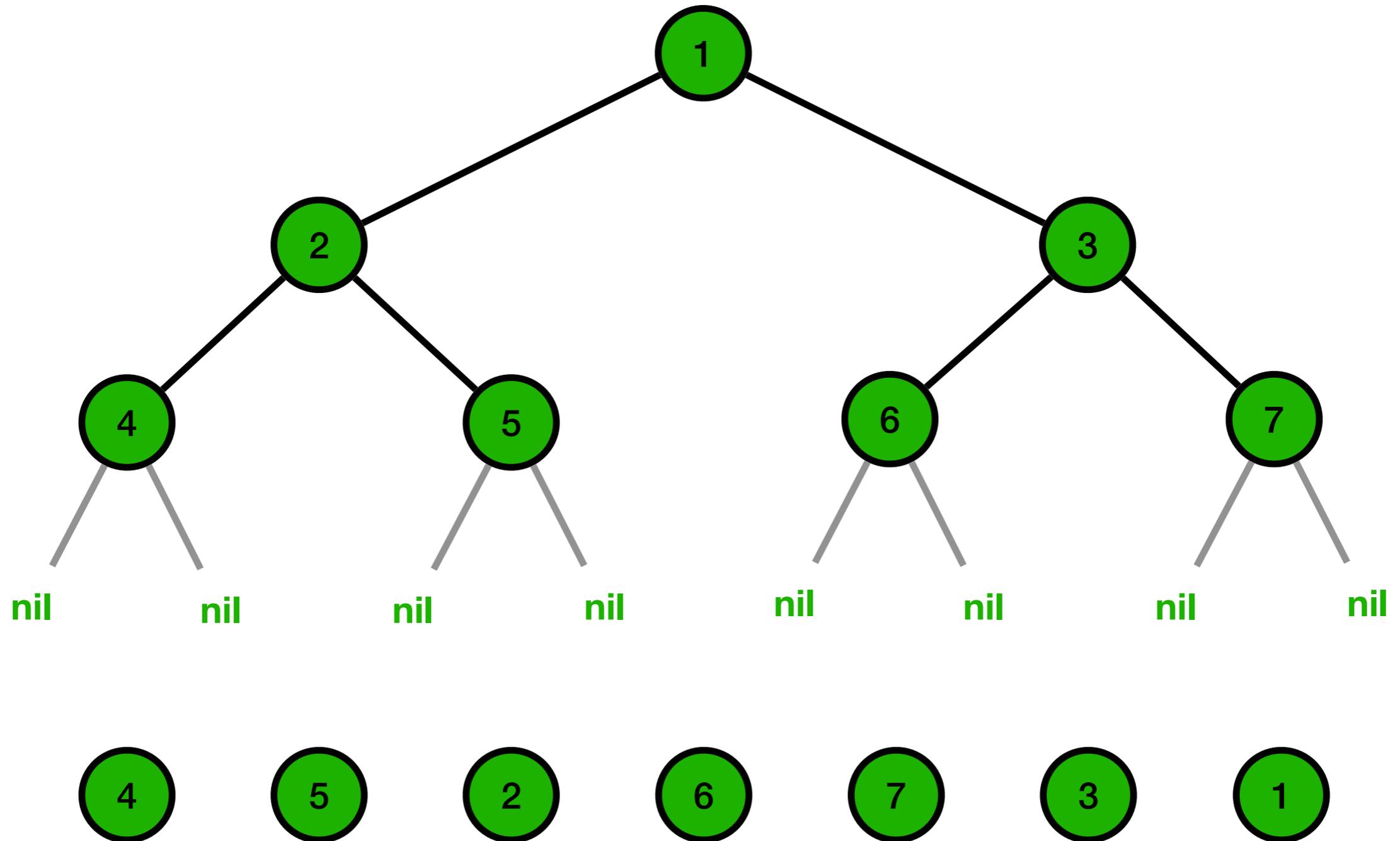
Parcours postfixe



Parcours postfixe



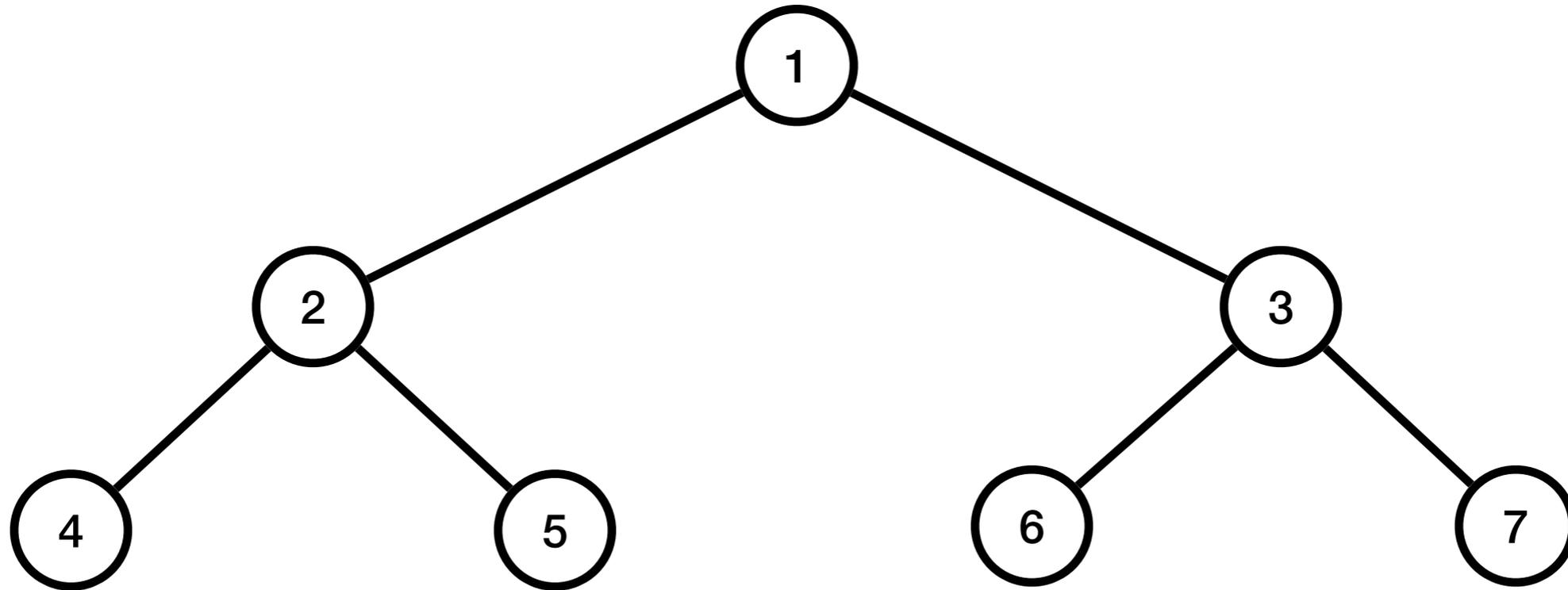
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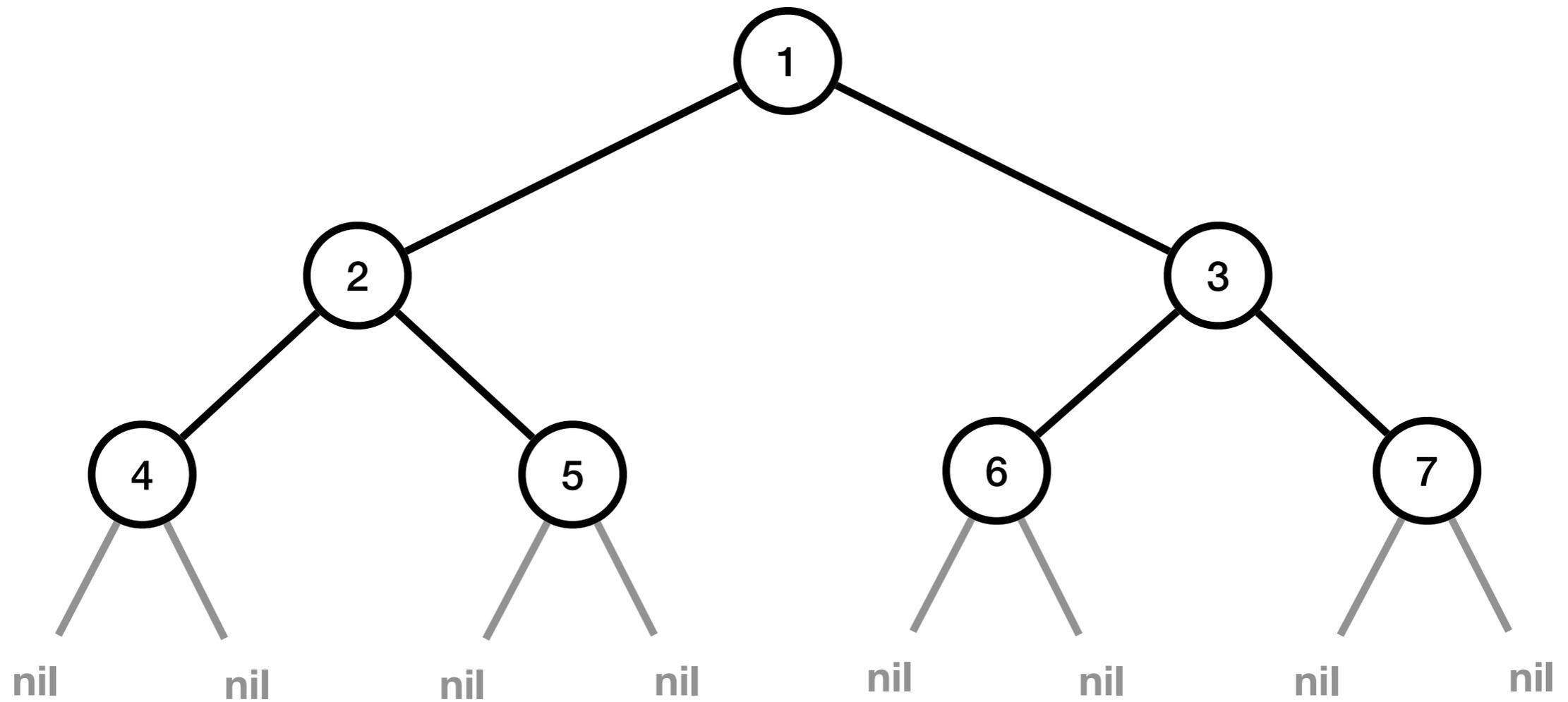
Parcours infixe

```
def parcours_infixe(arbre):  
    if not est_vide(arbre):  
        parcours_infixe(gauche(arbre))  
        print(valeur(arbre))  
        parcours_infixe(droite(arbre))
```

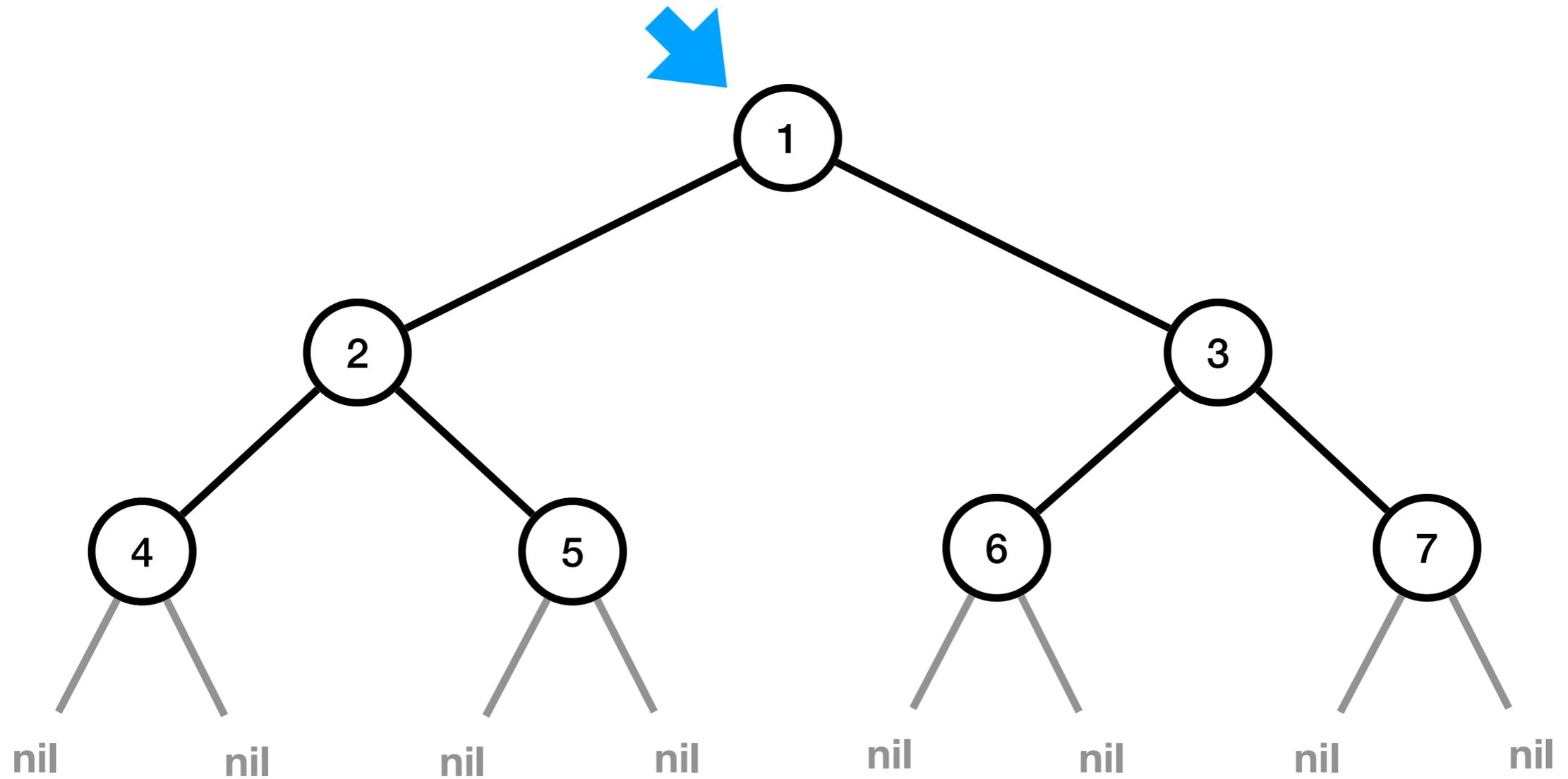
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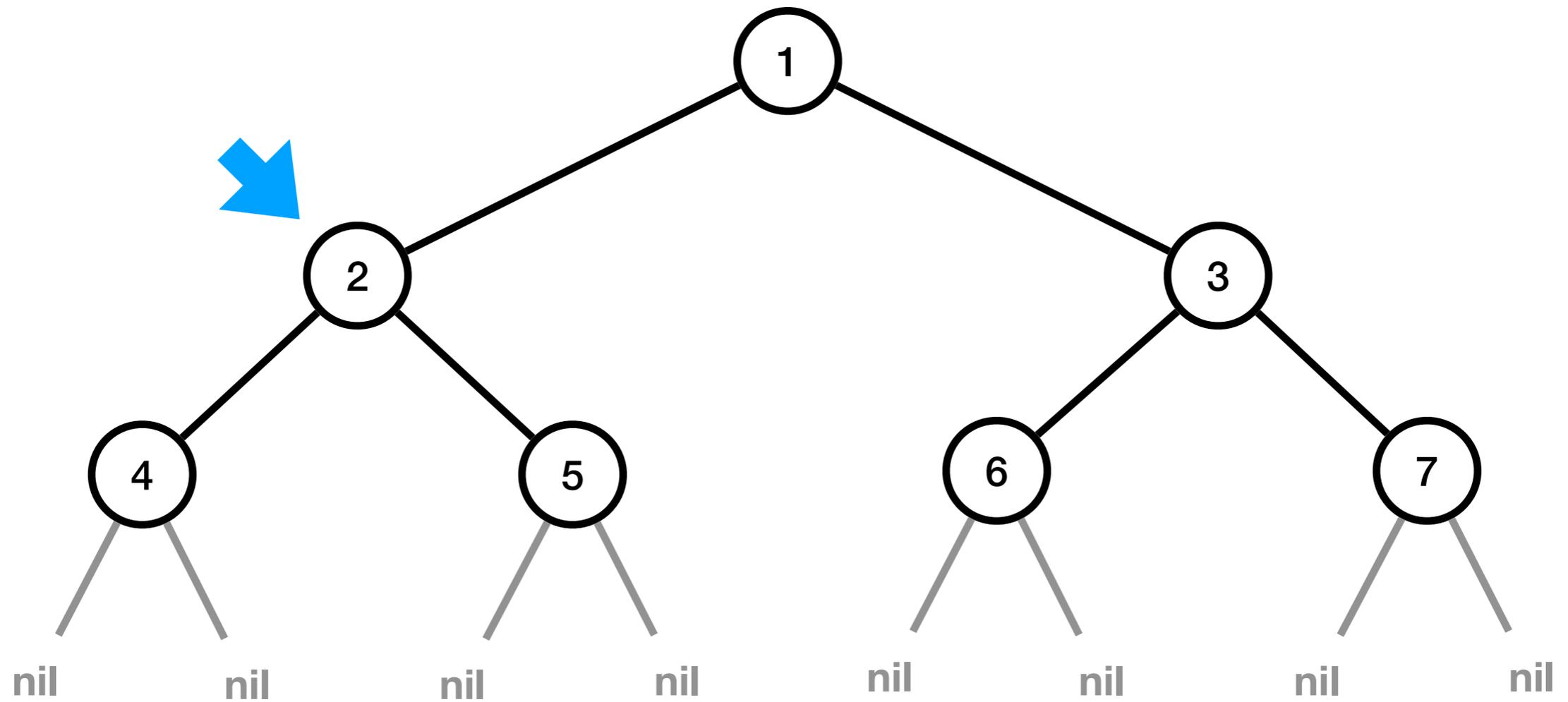
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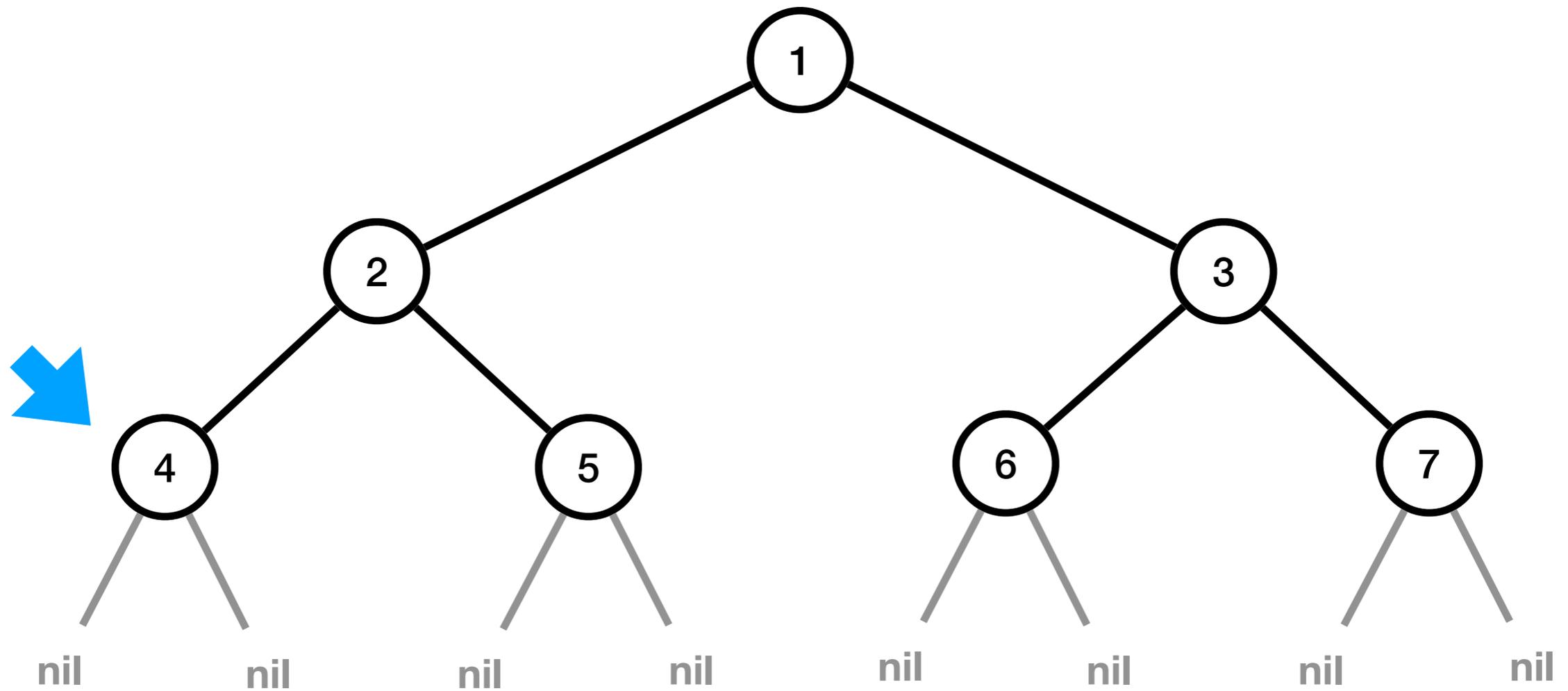
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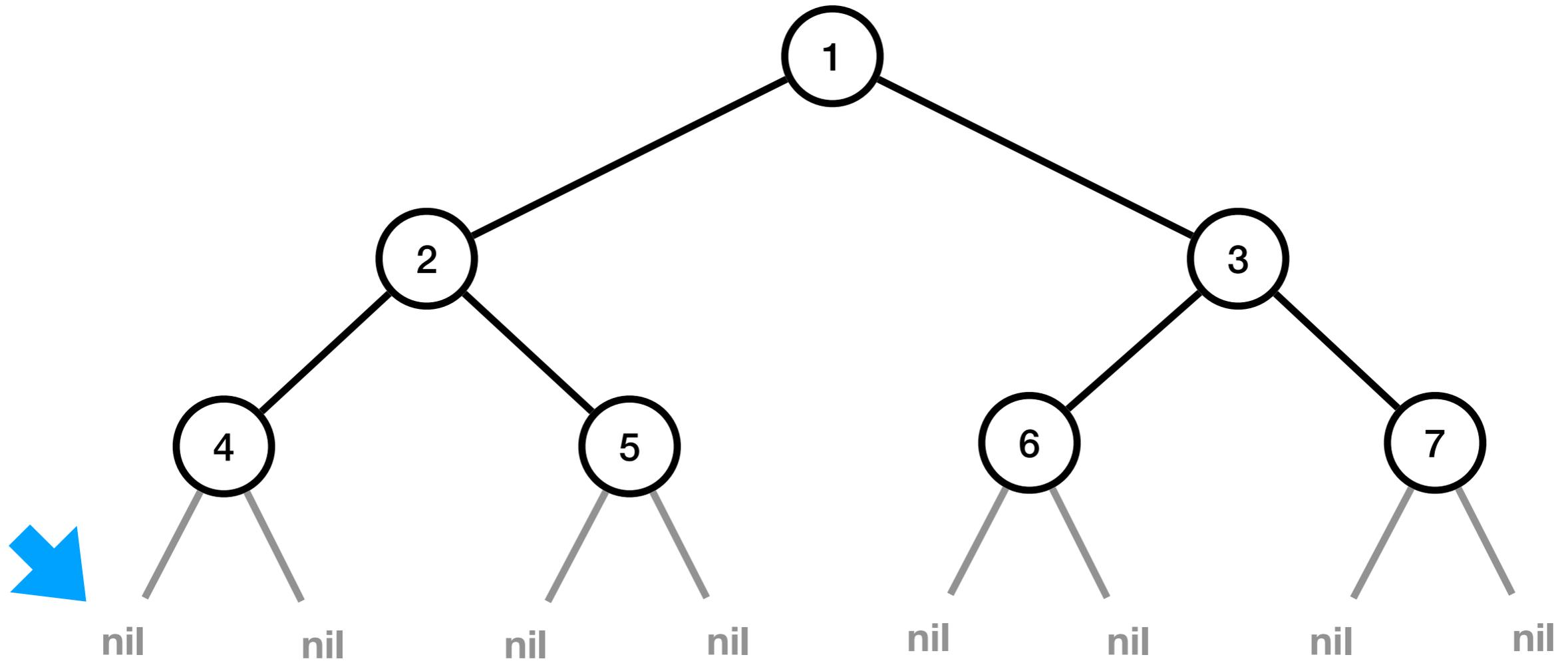
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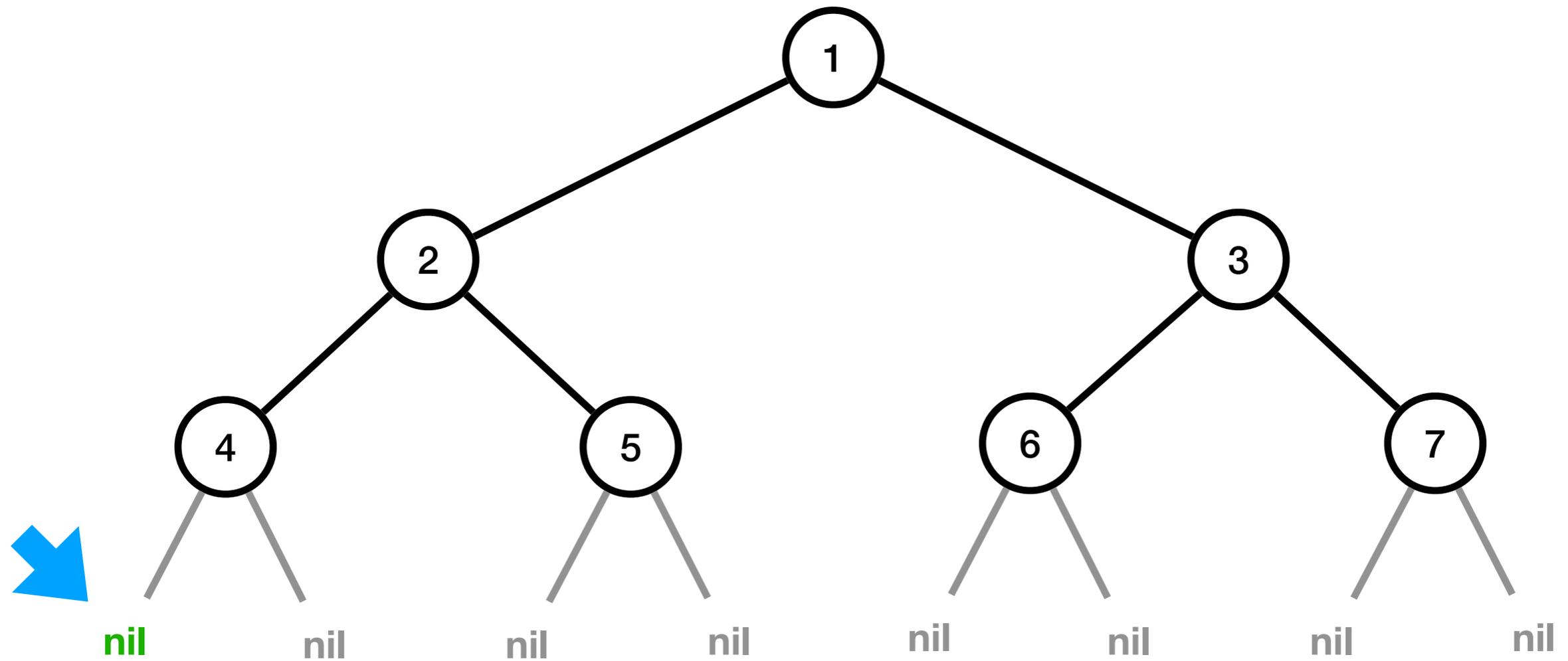
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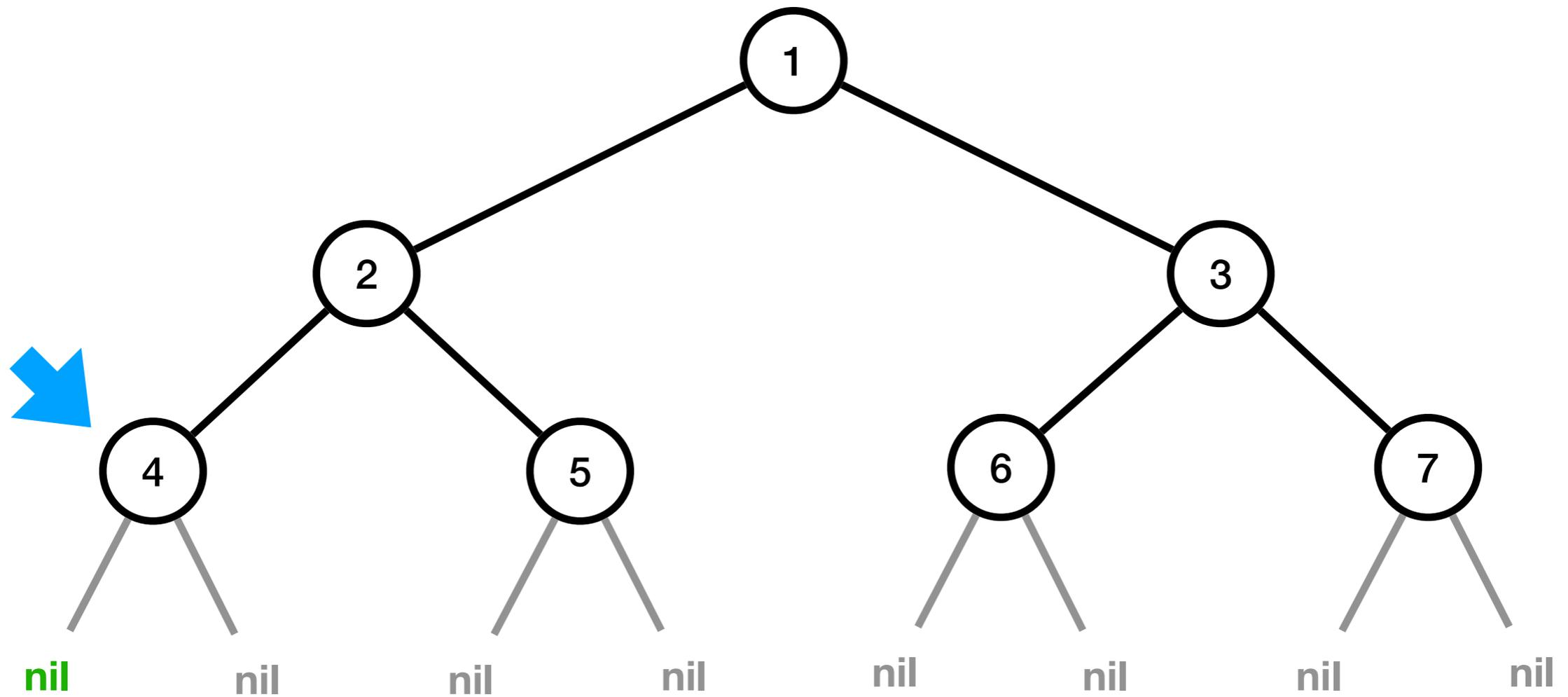
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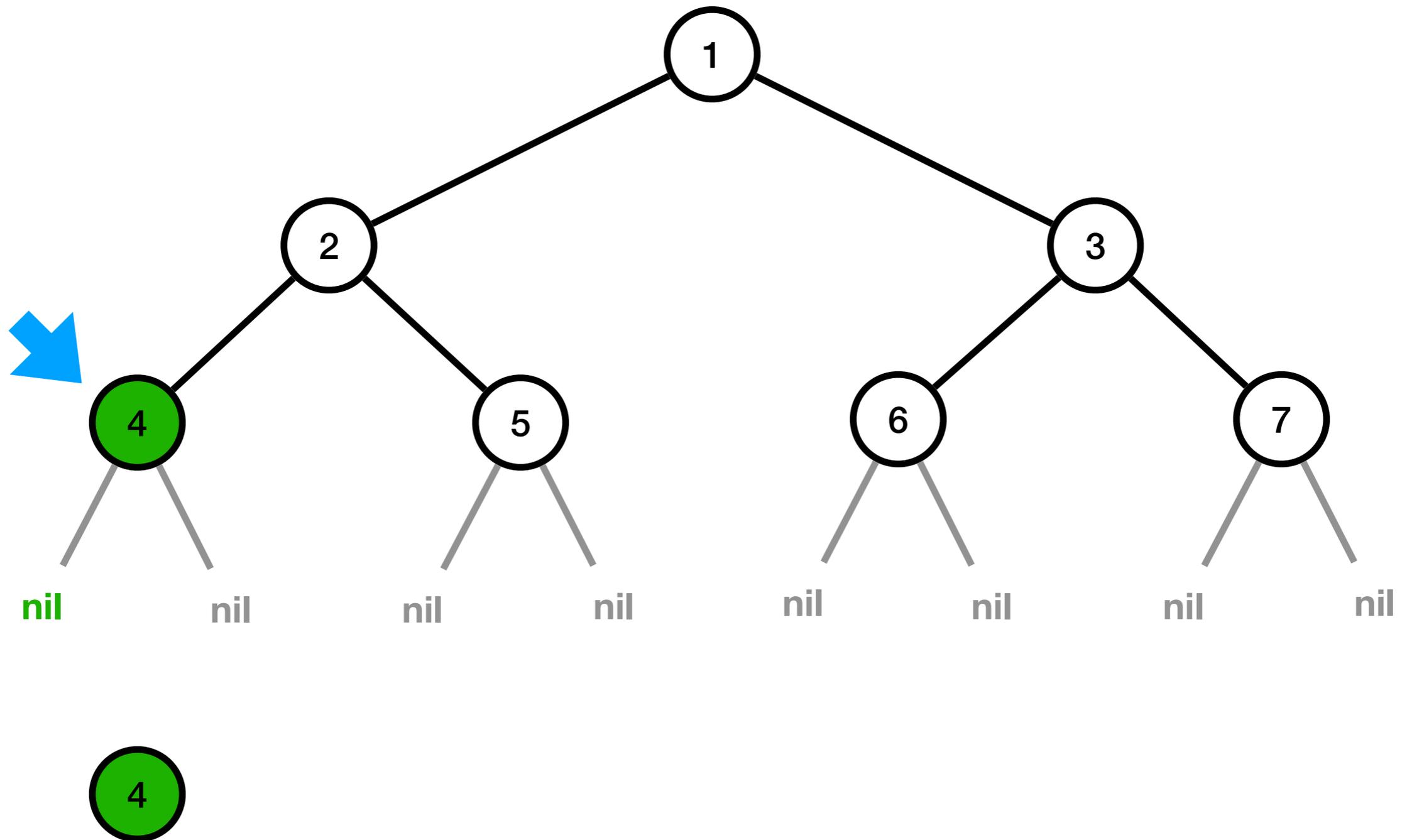
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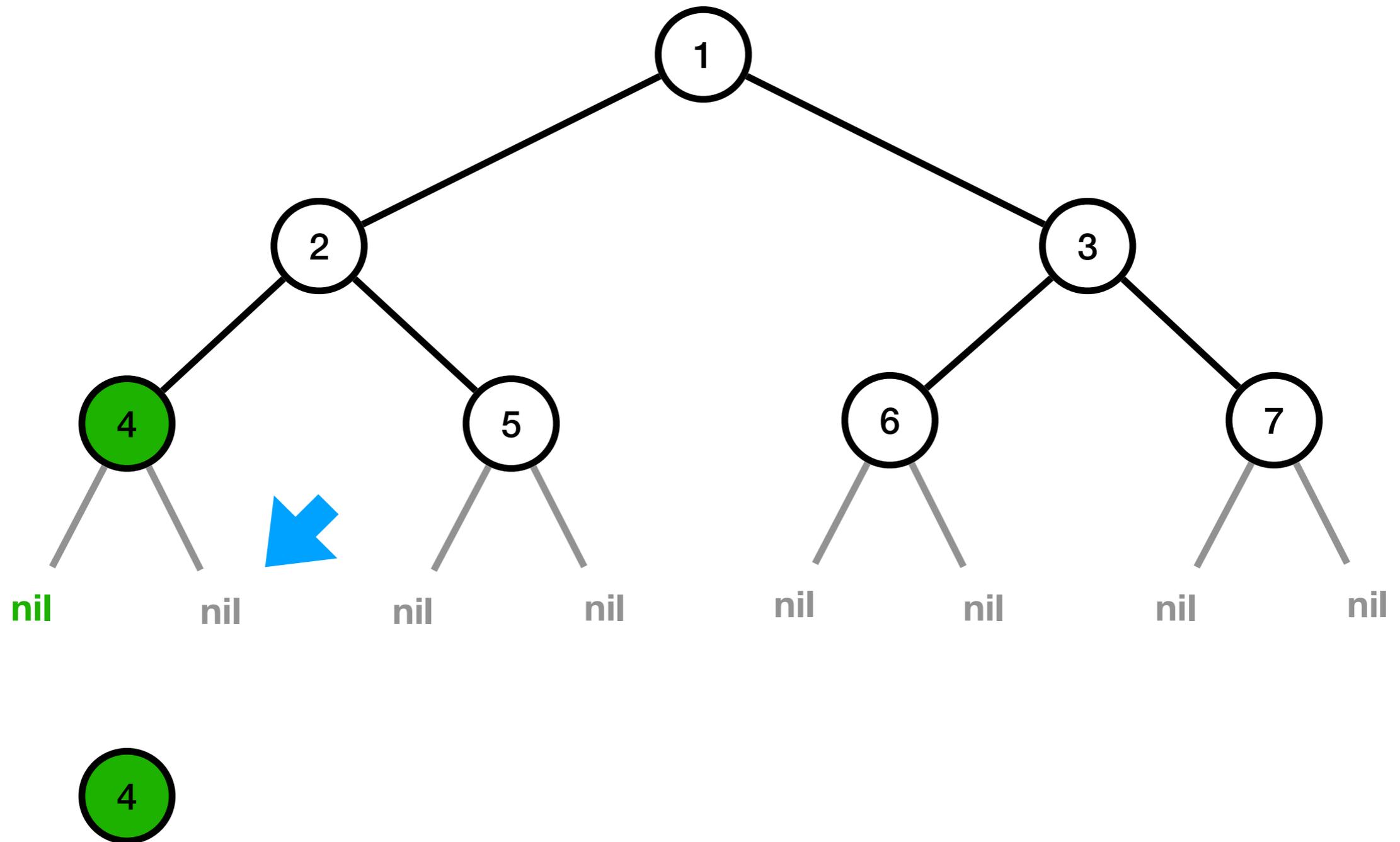
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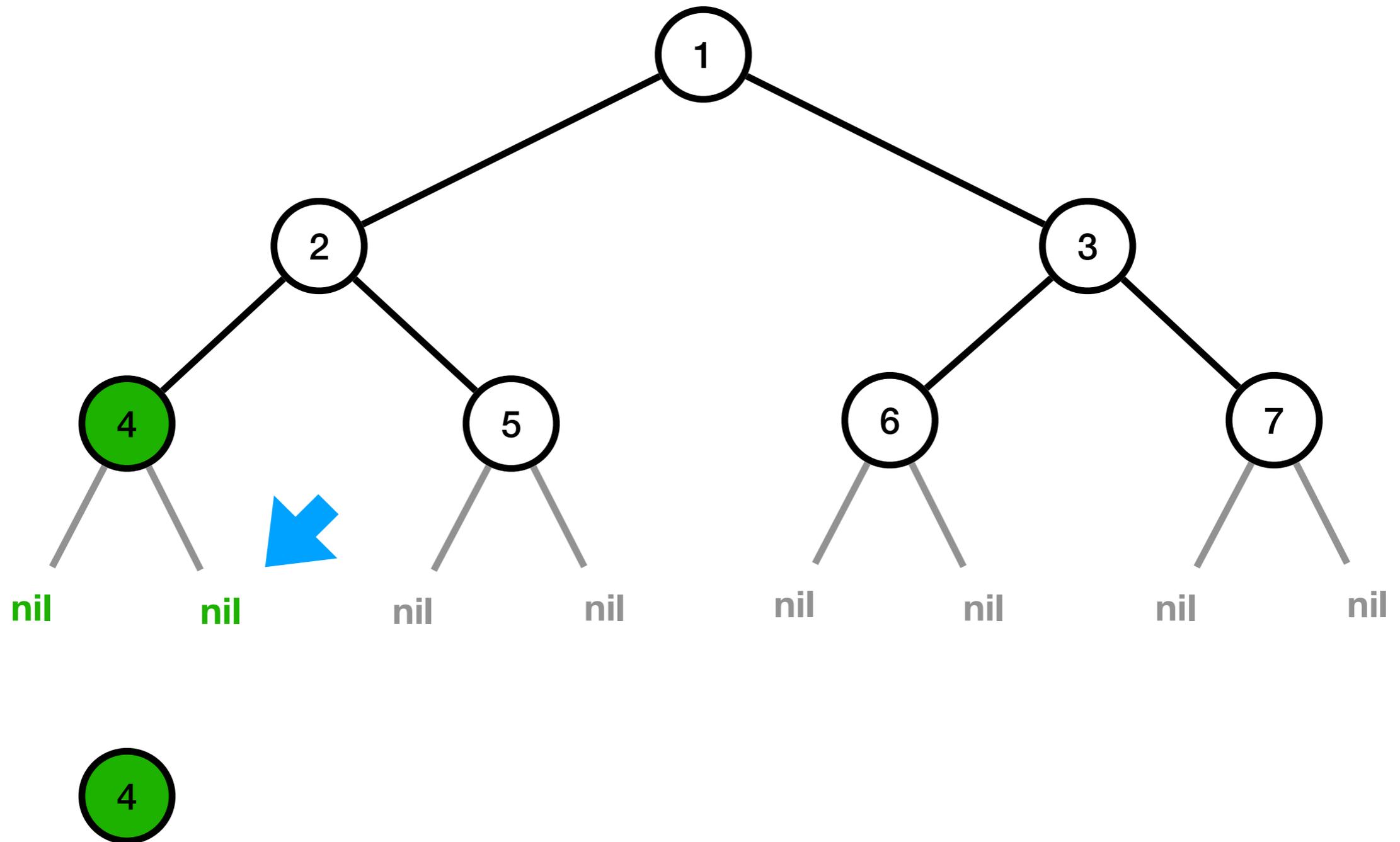
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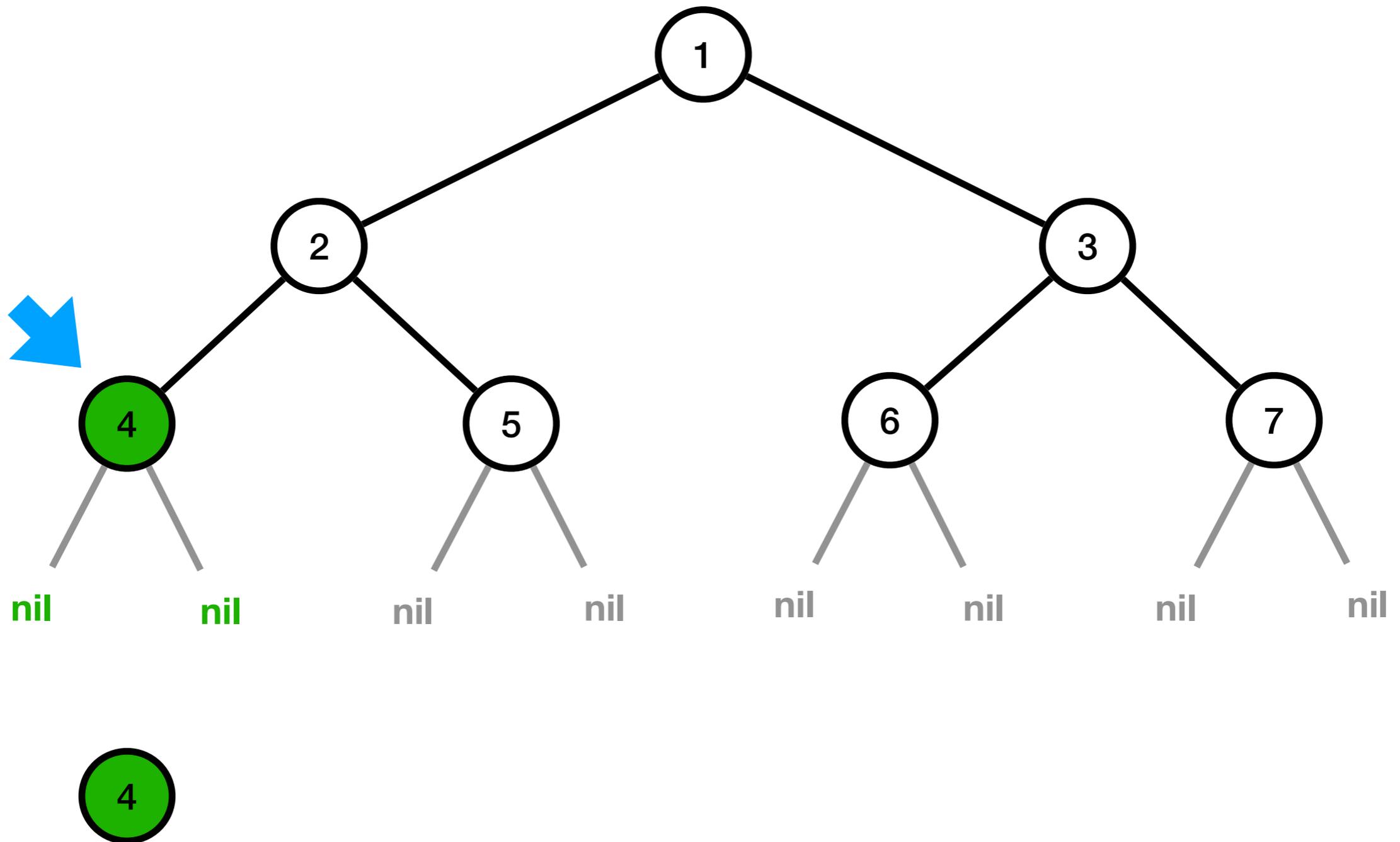
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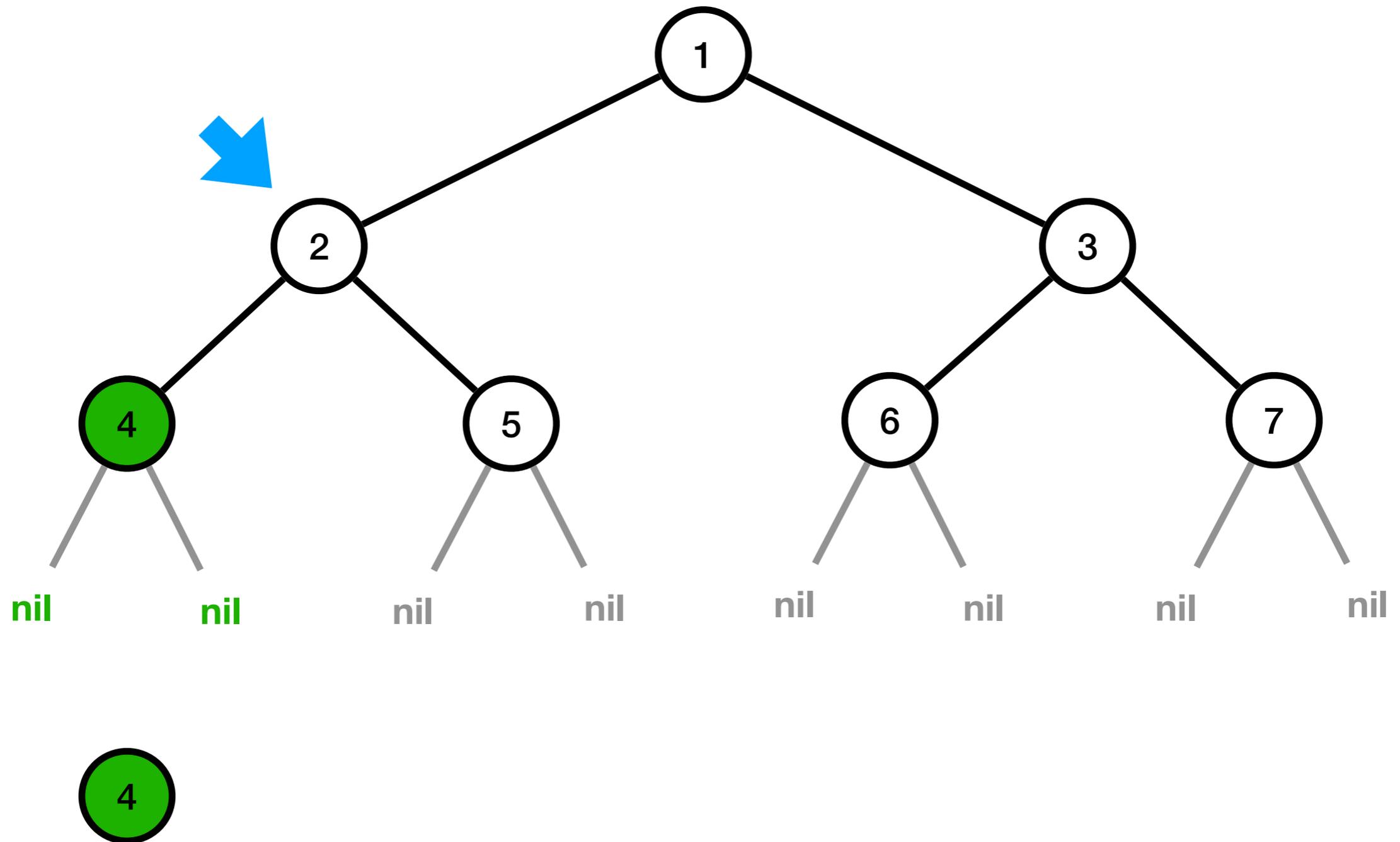
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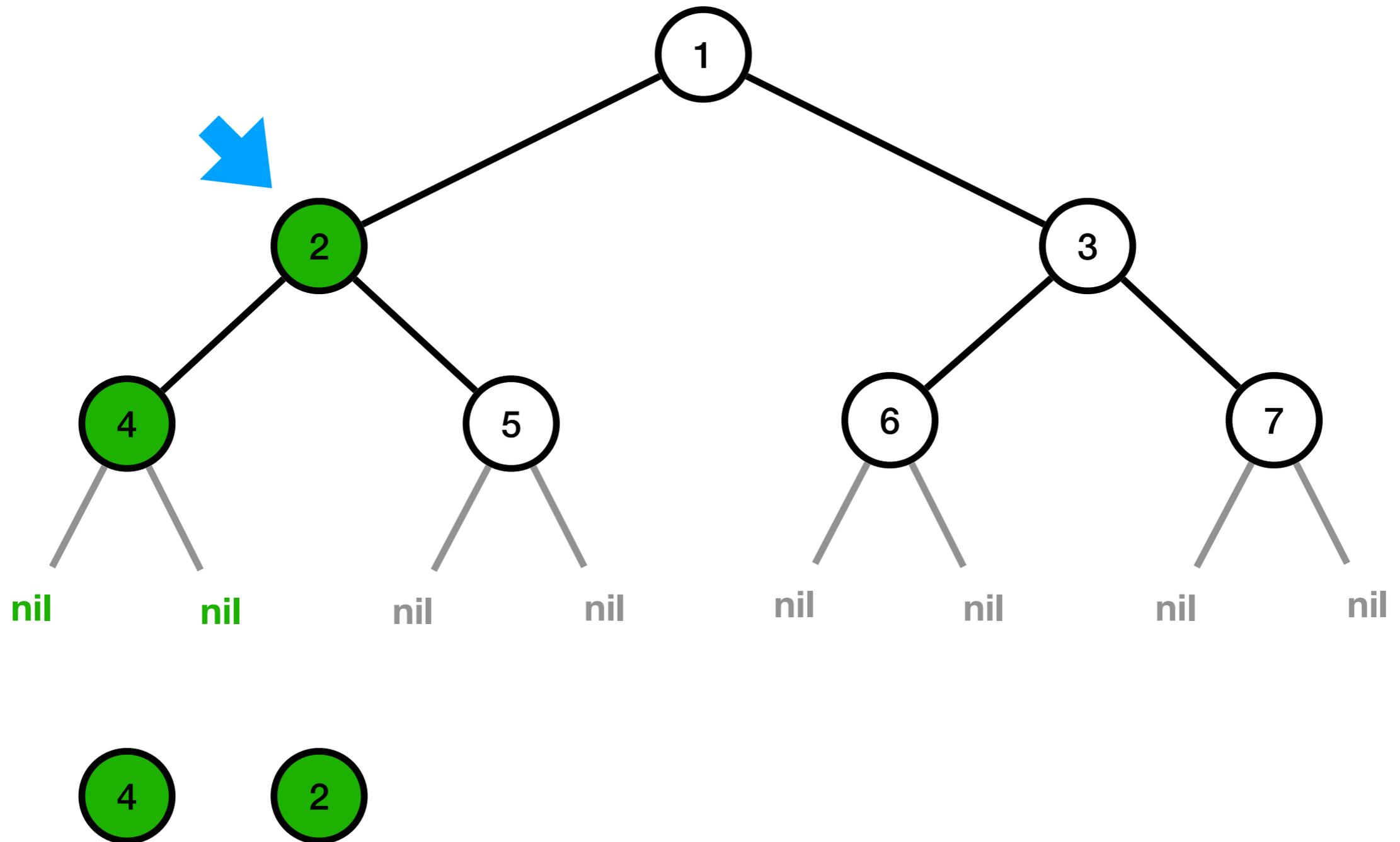
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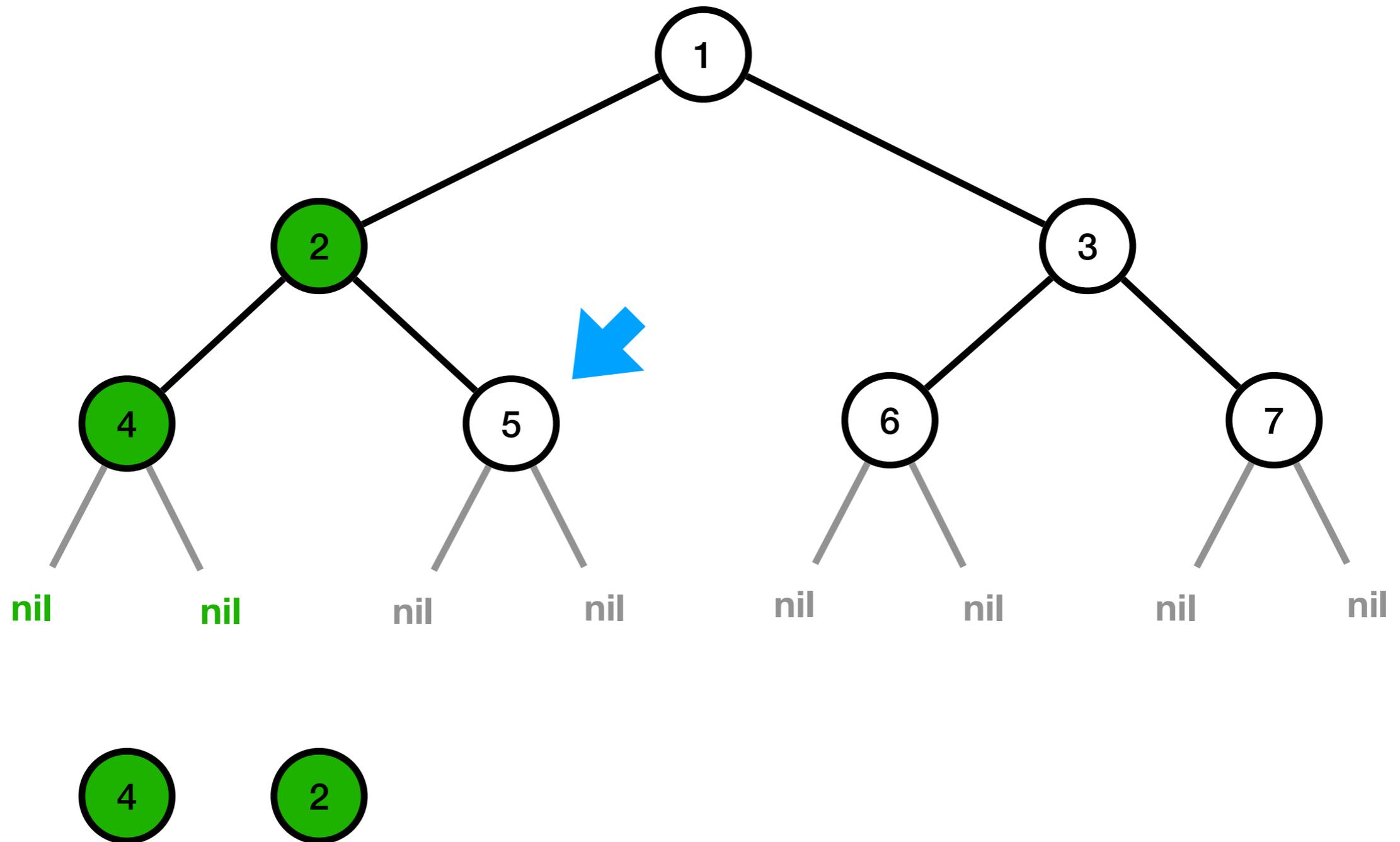
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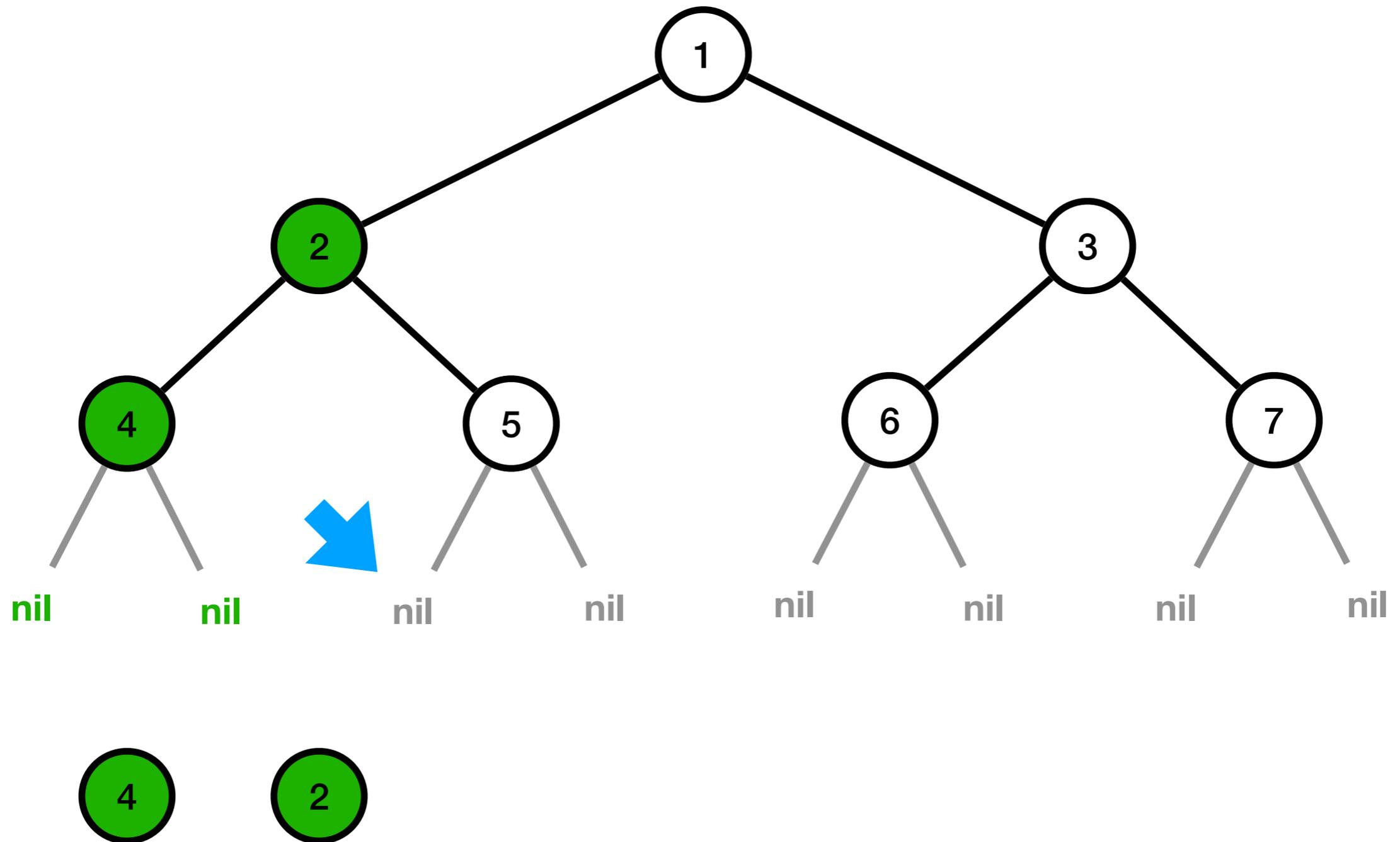
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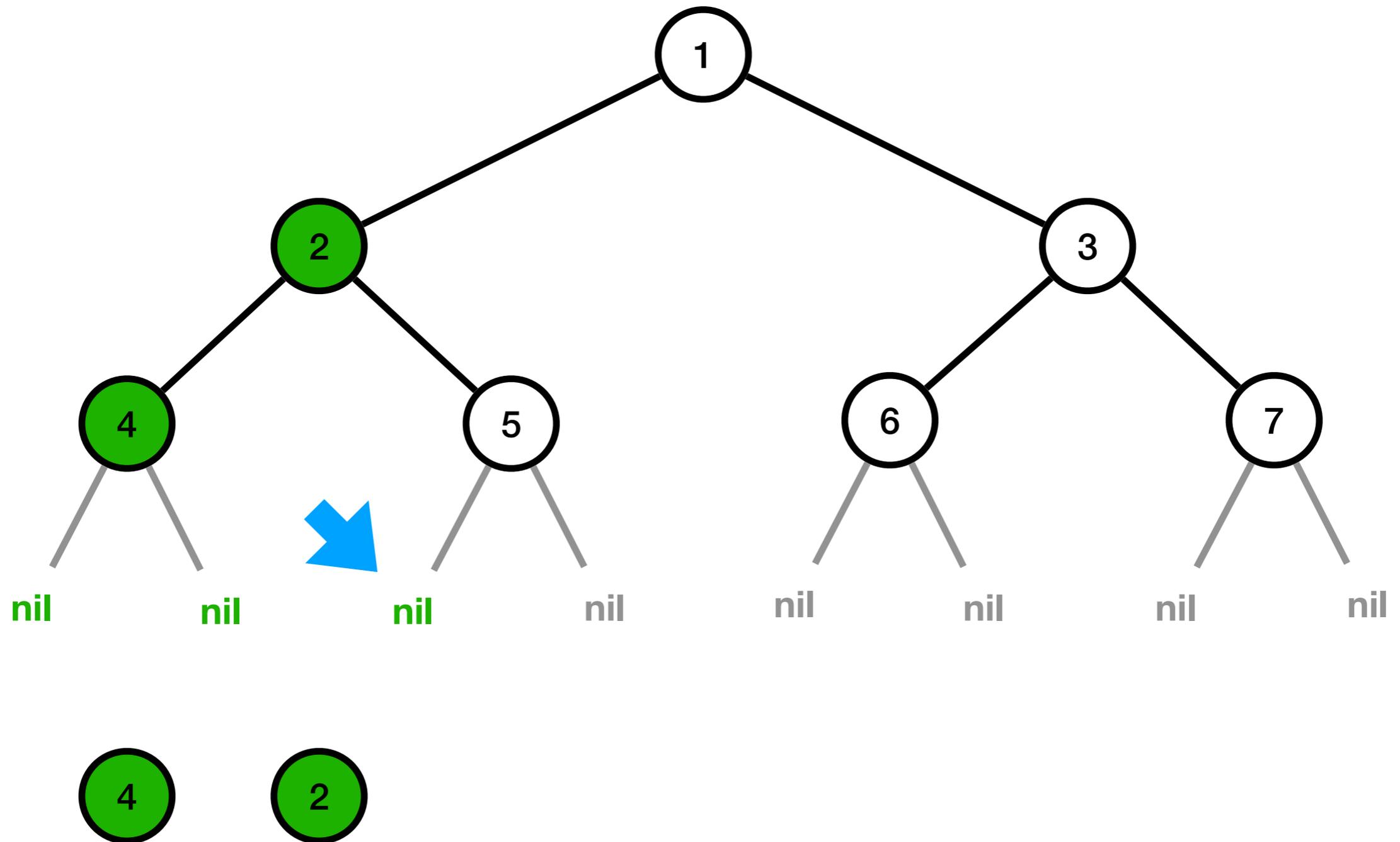
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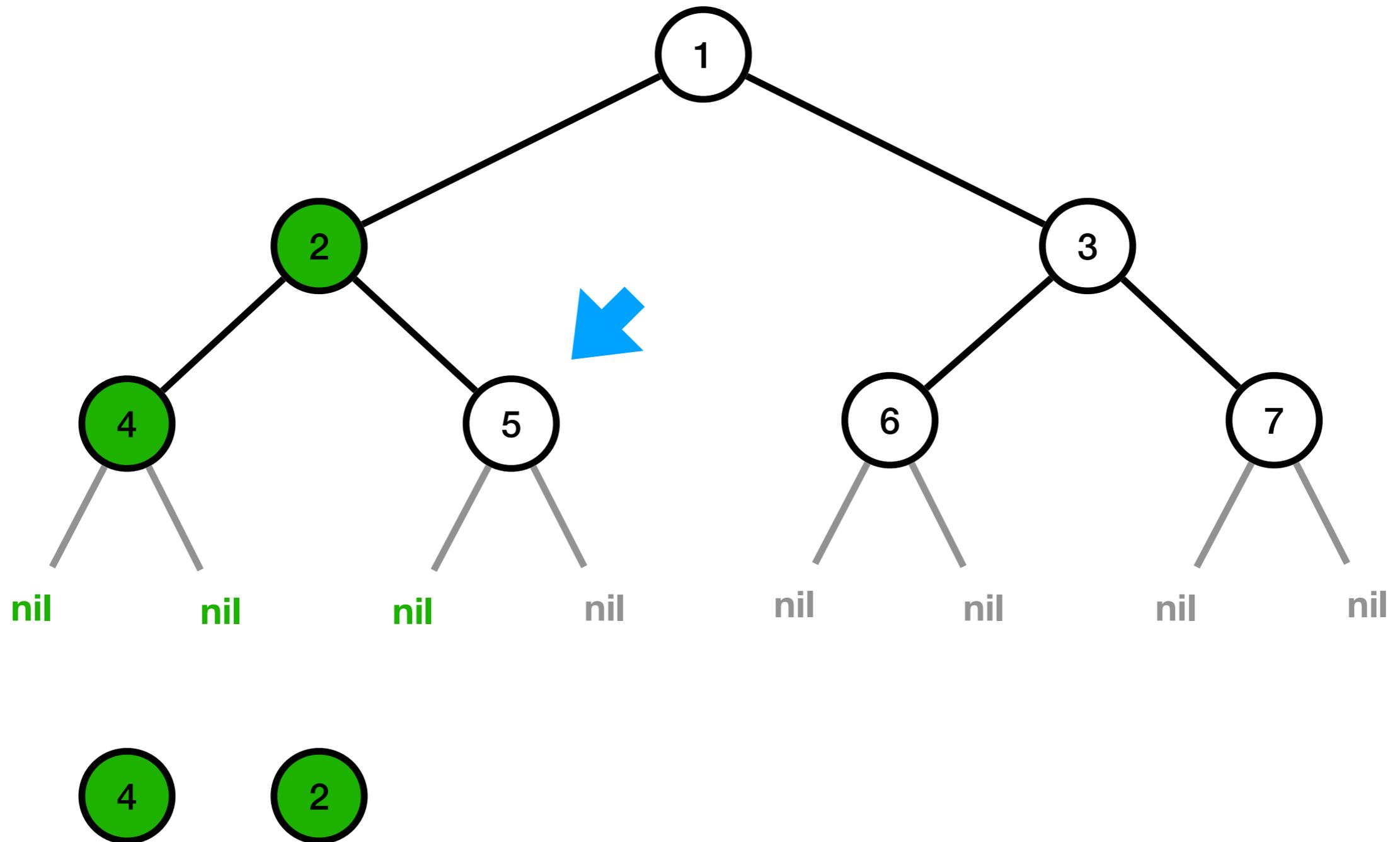
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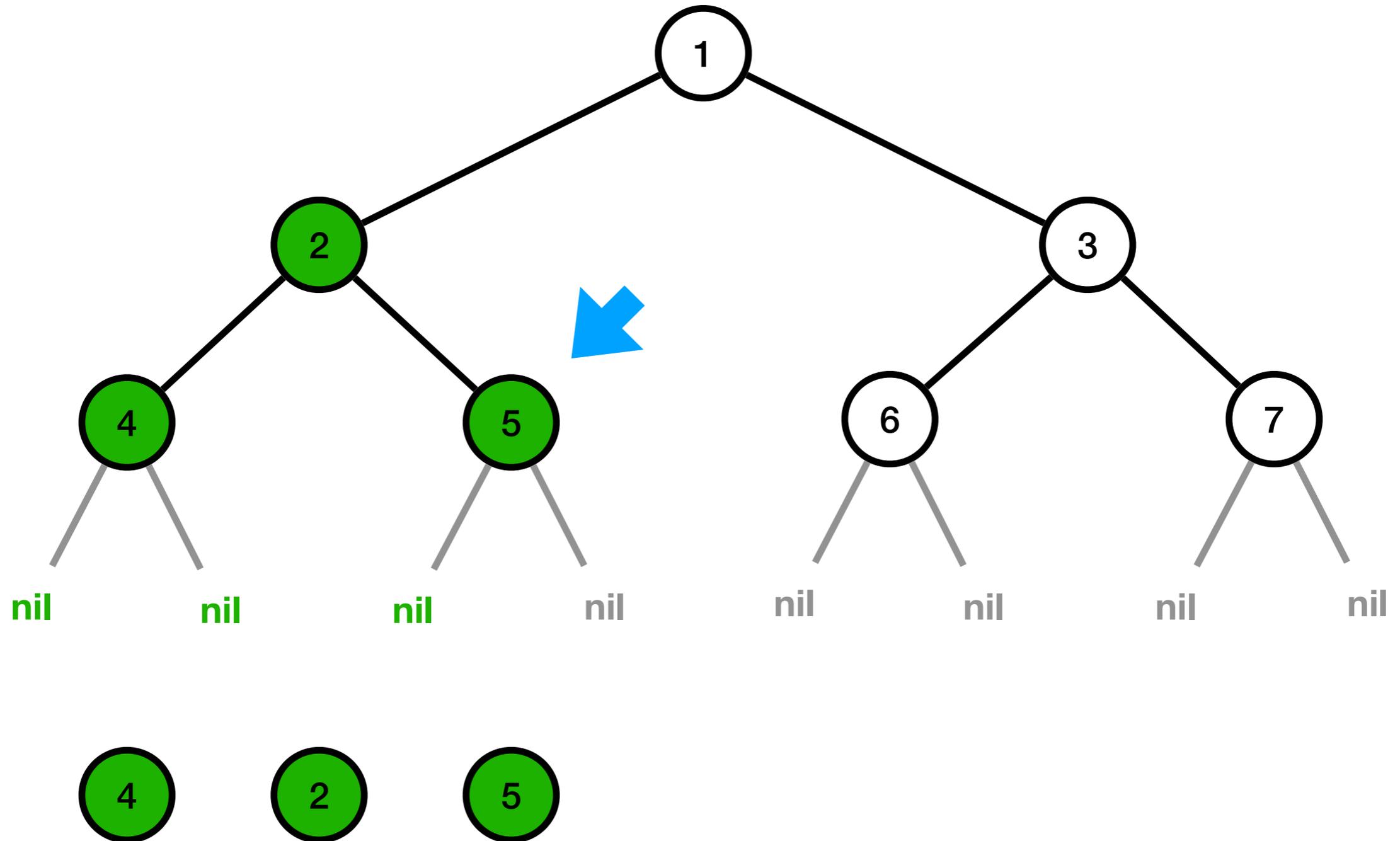
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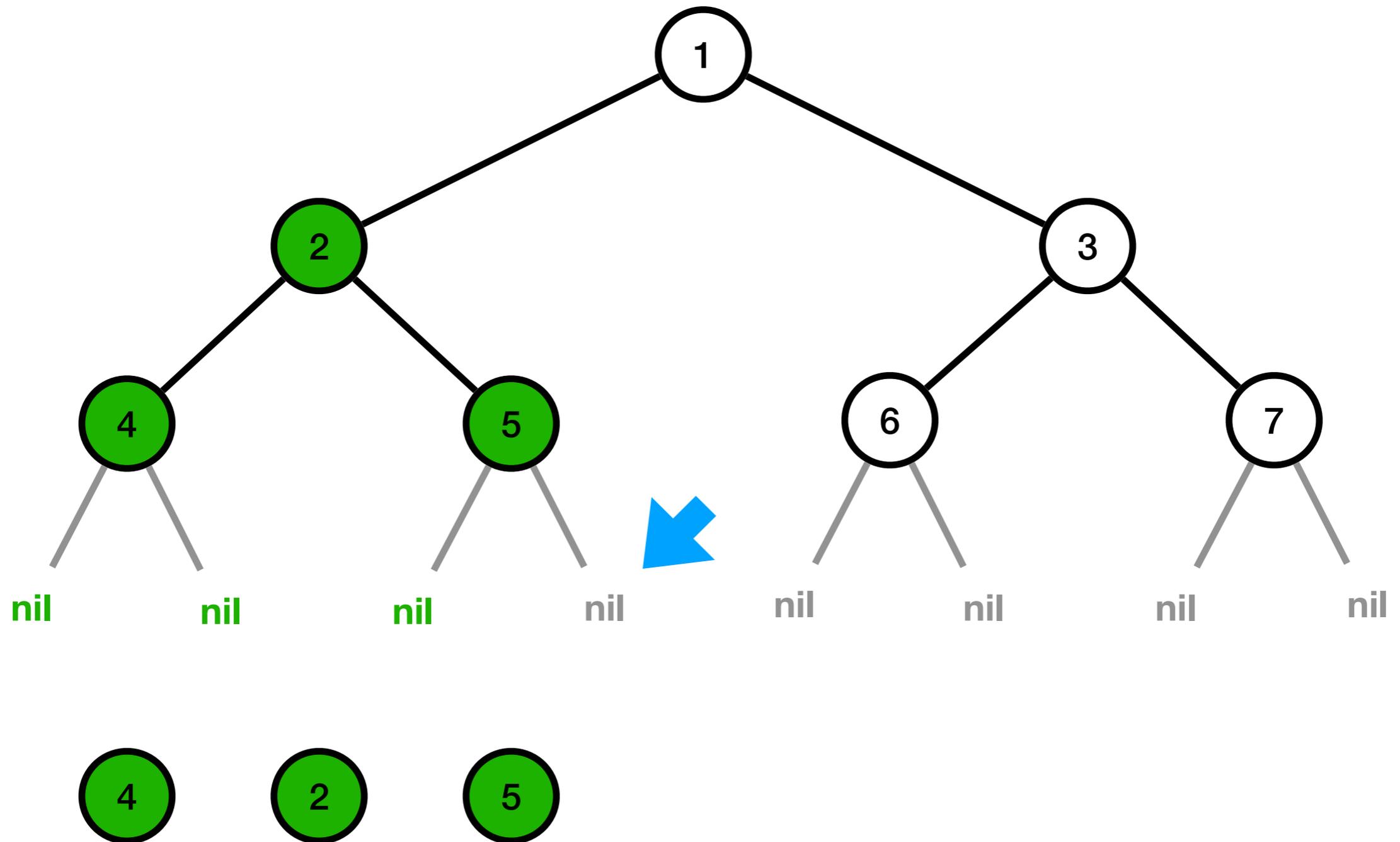
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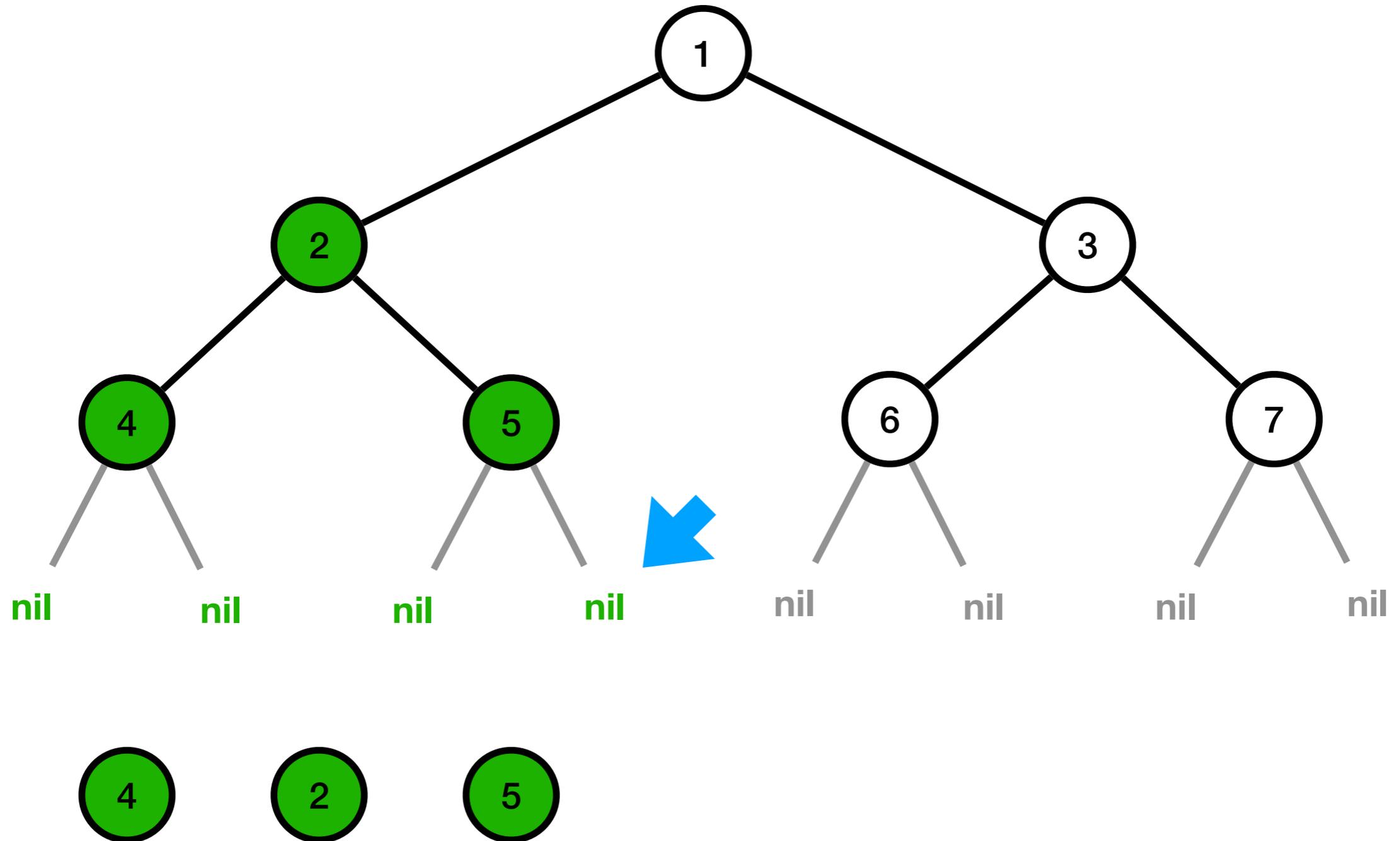
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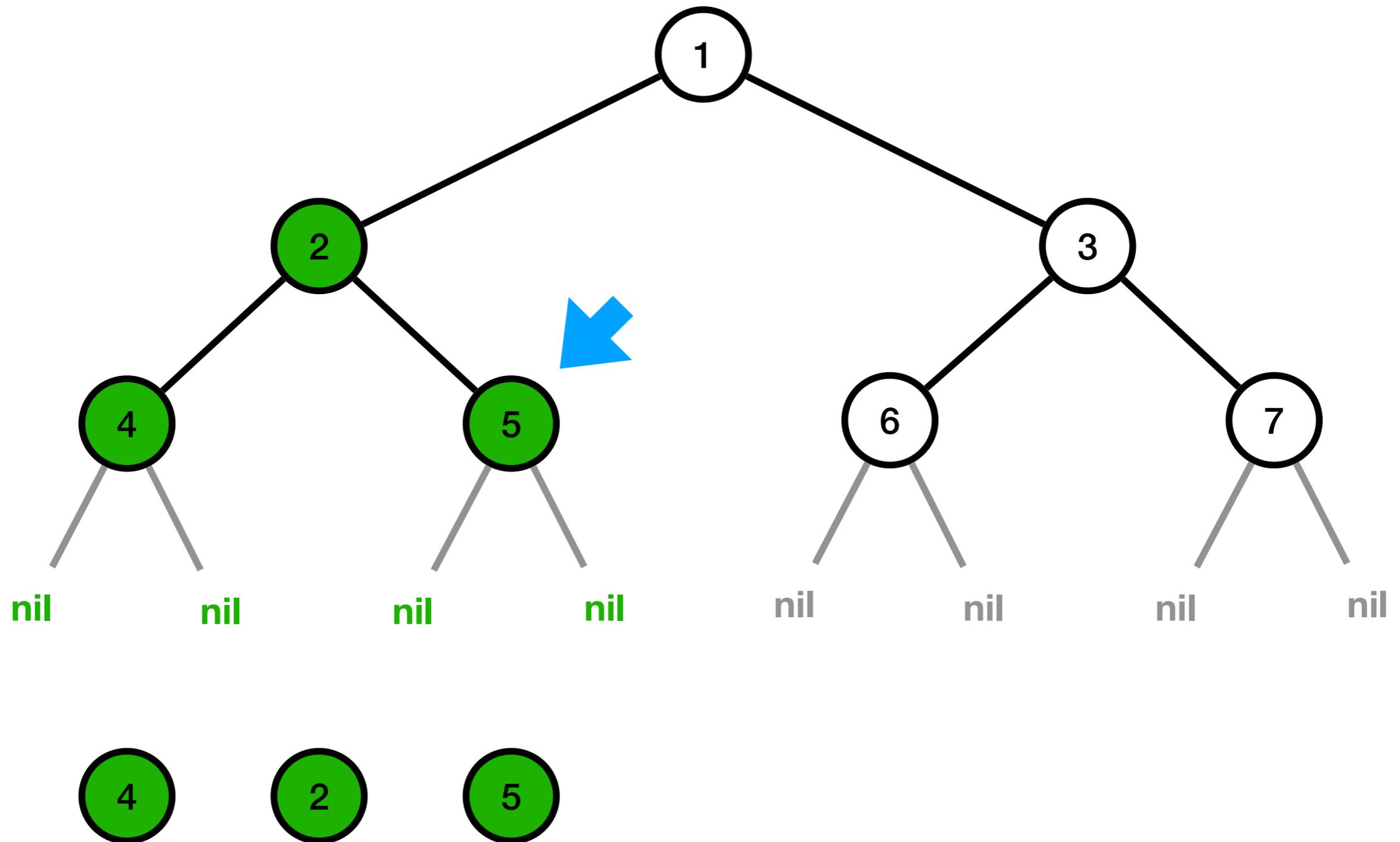
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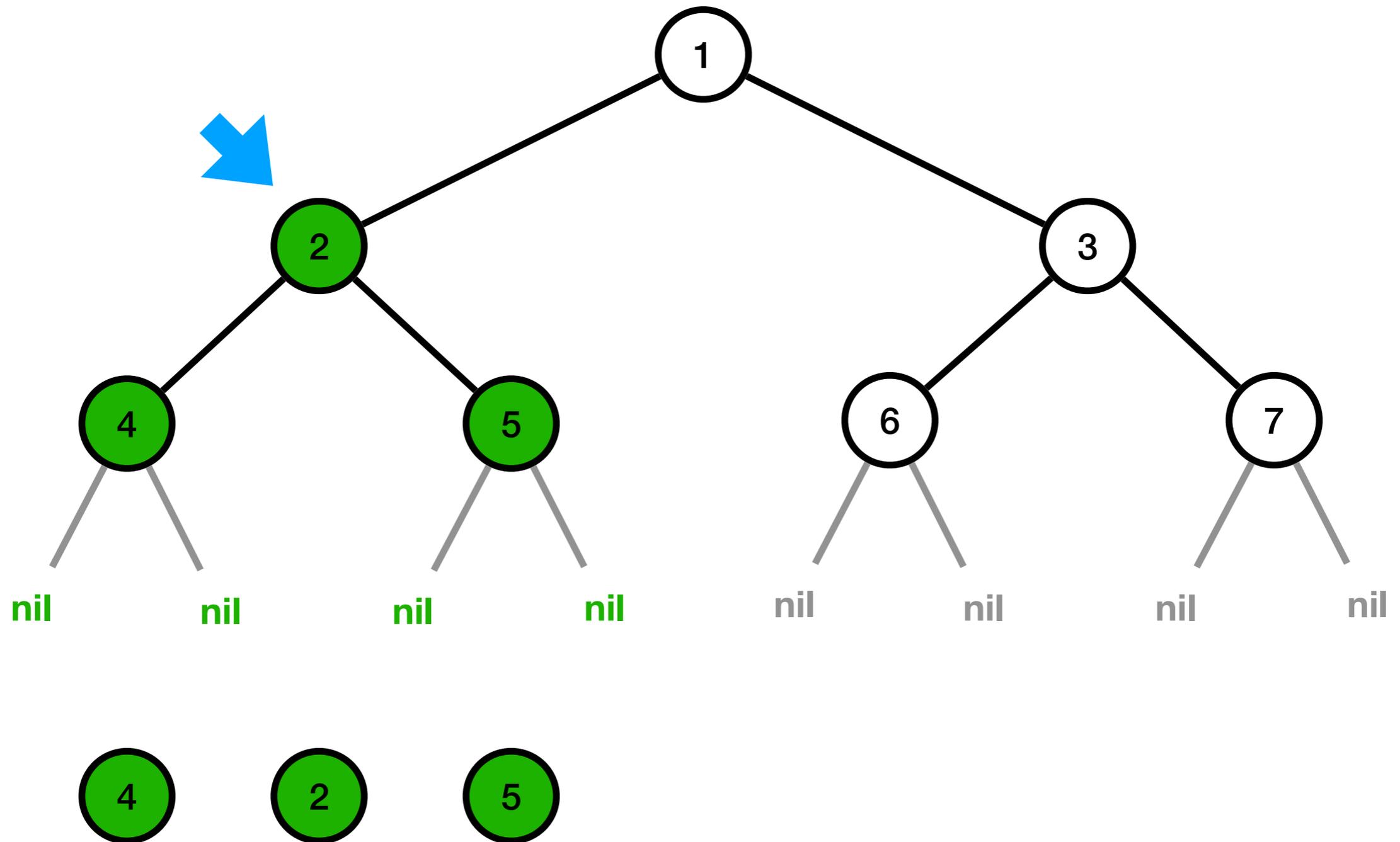
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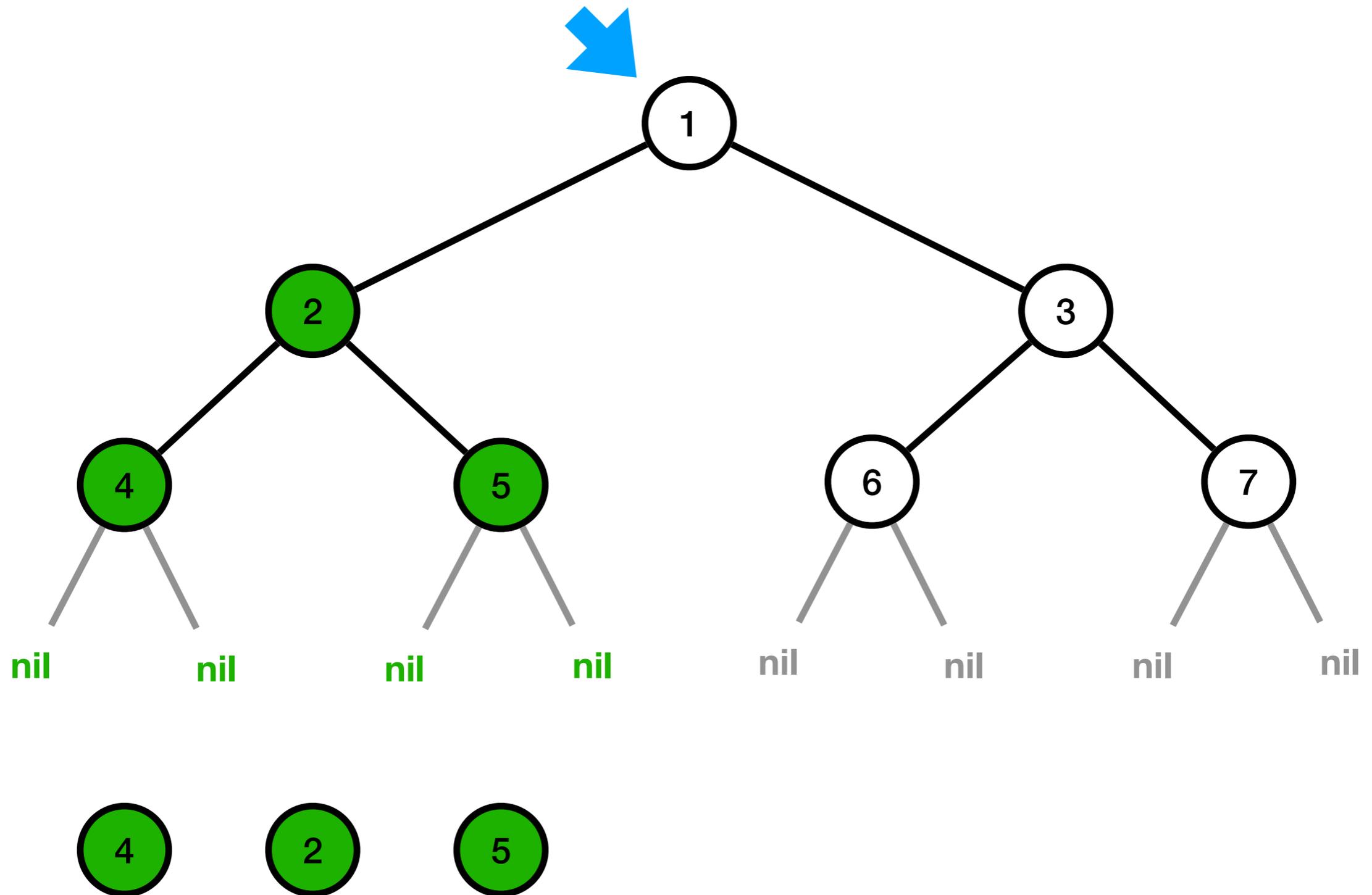
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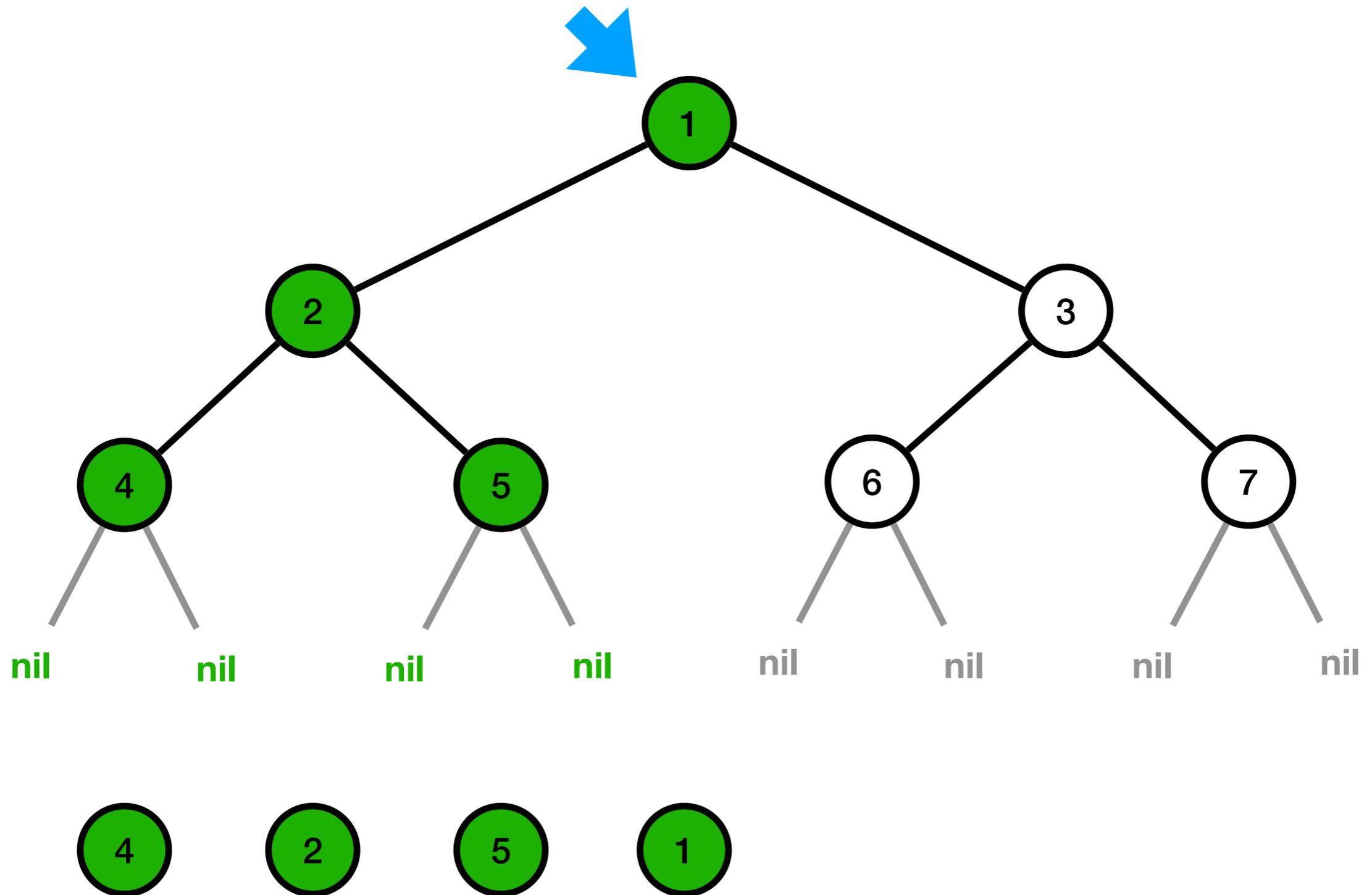
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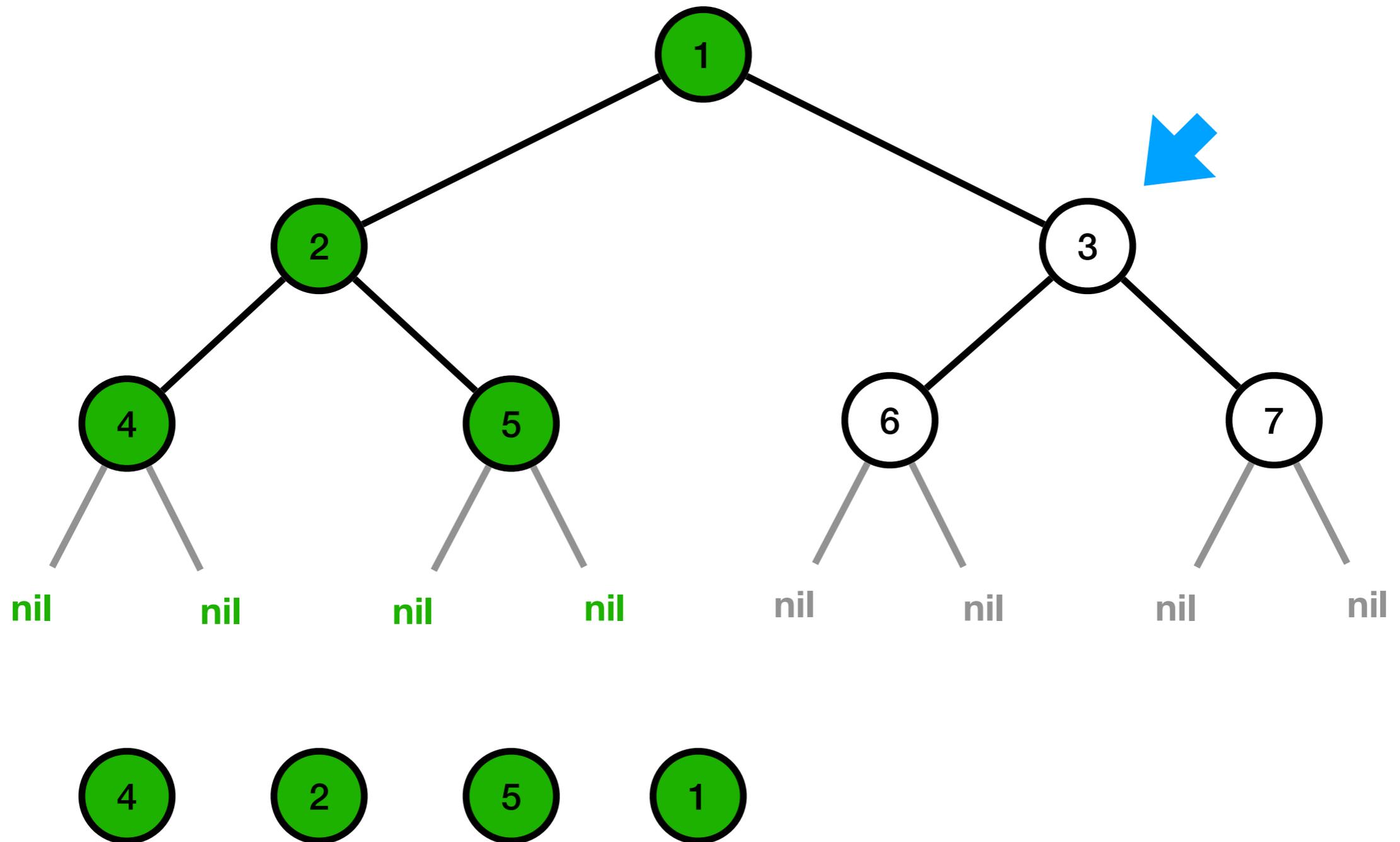
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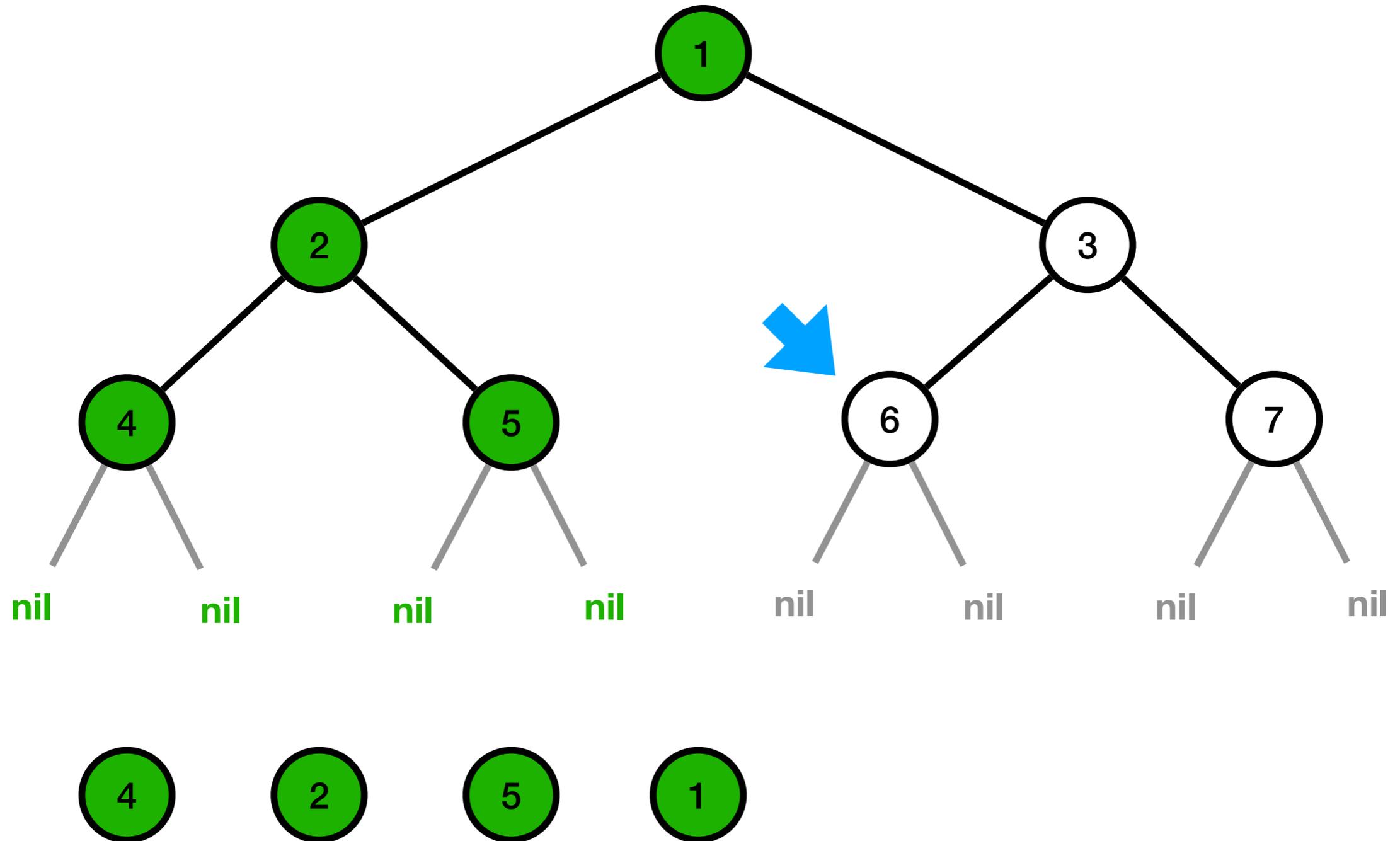
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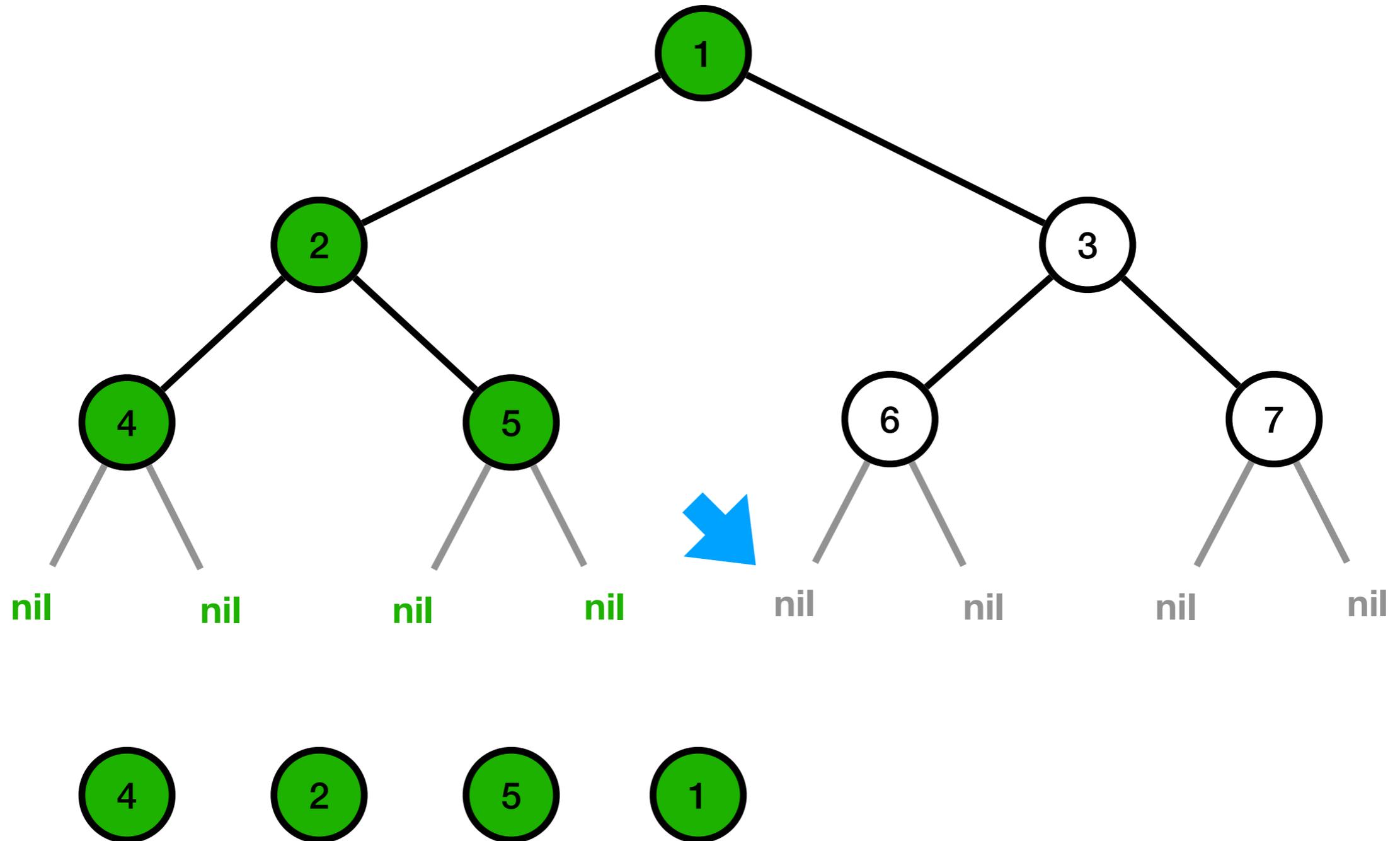
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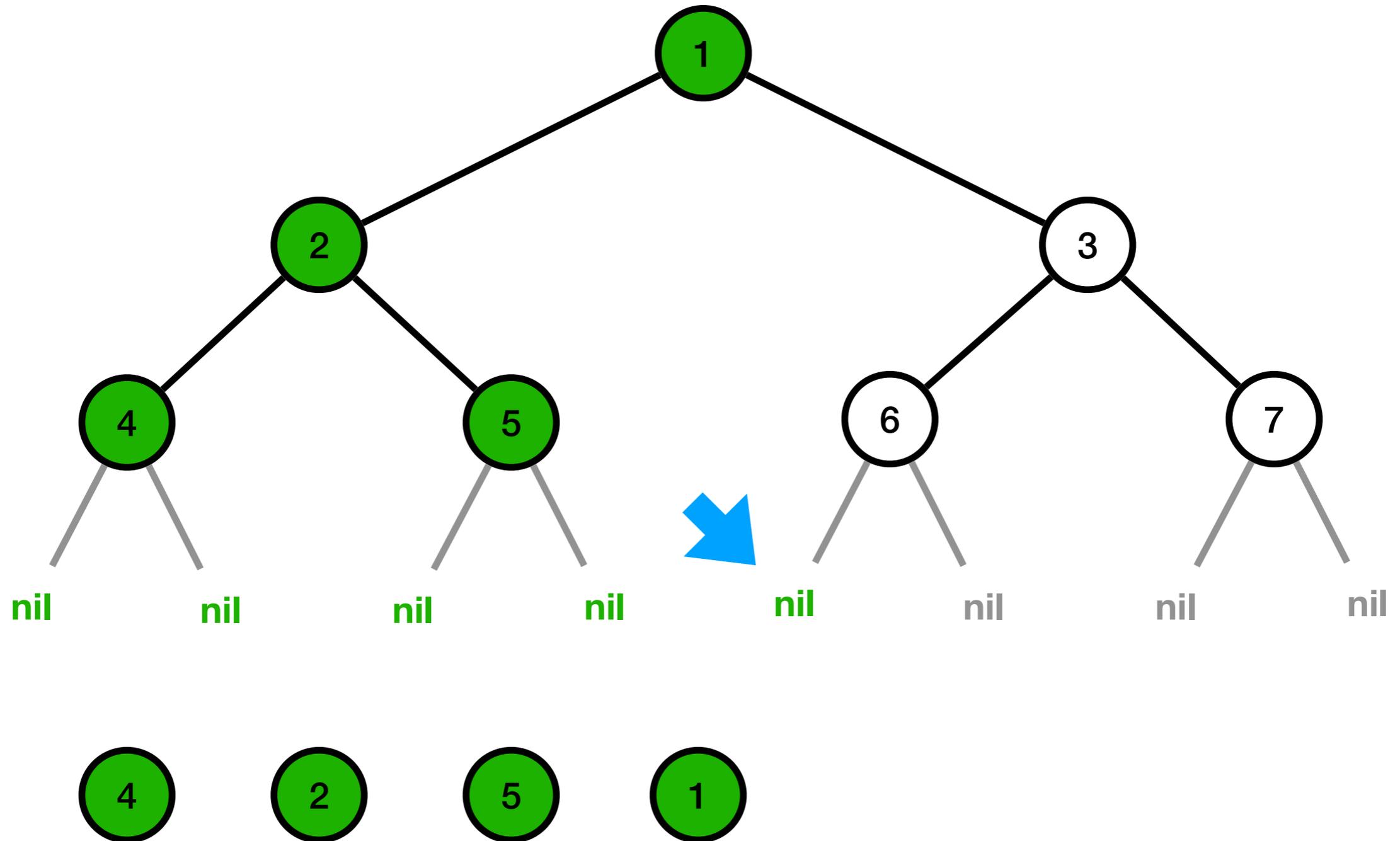
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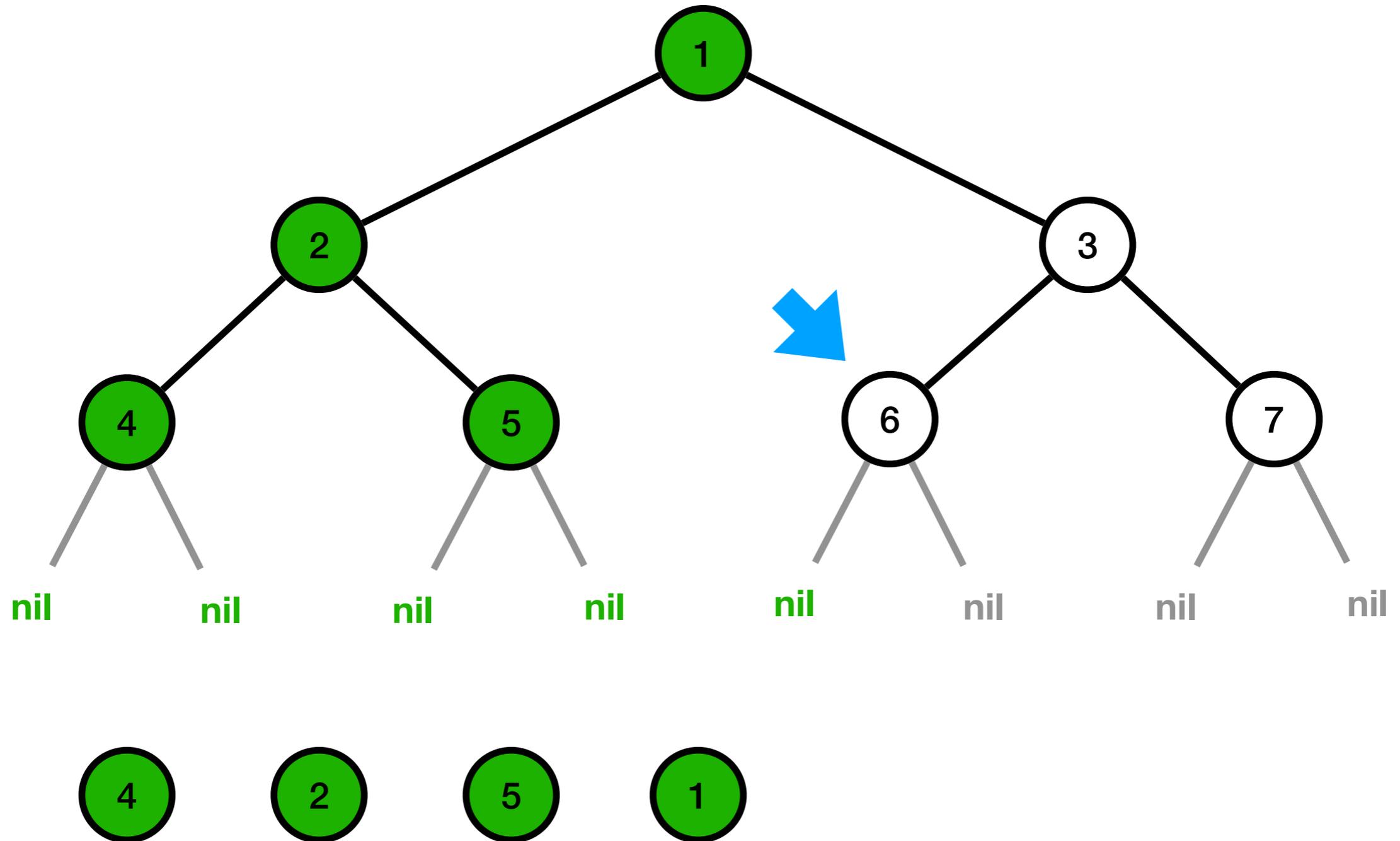
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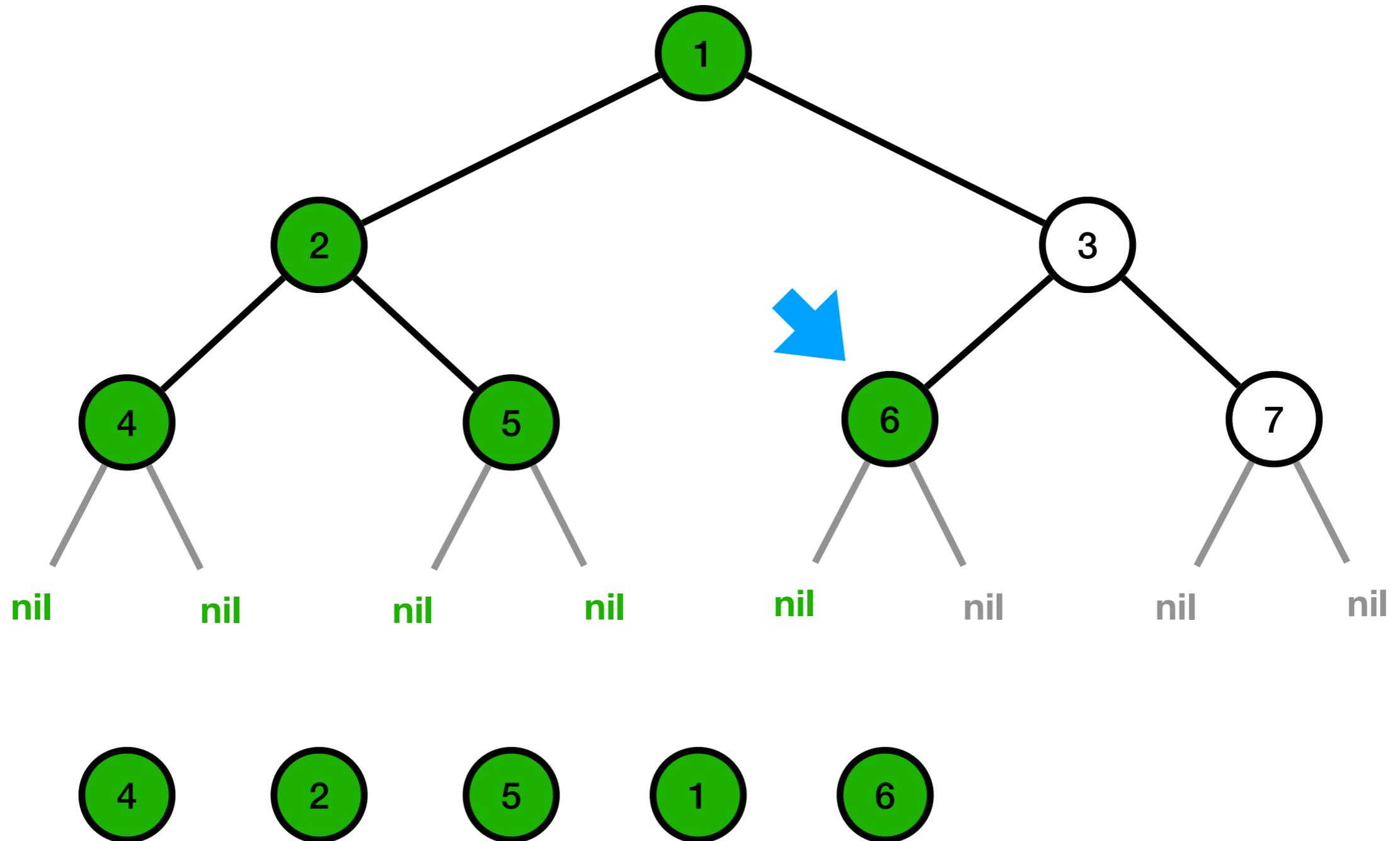
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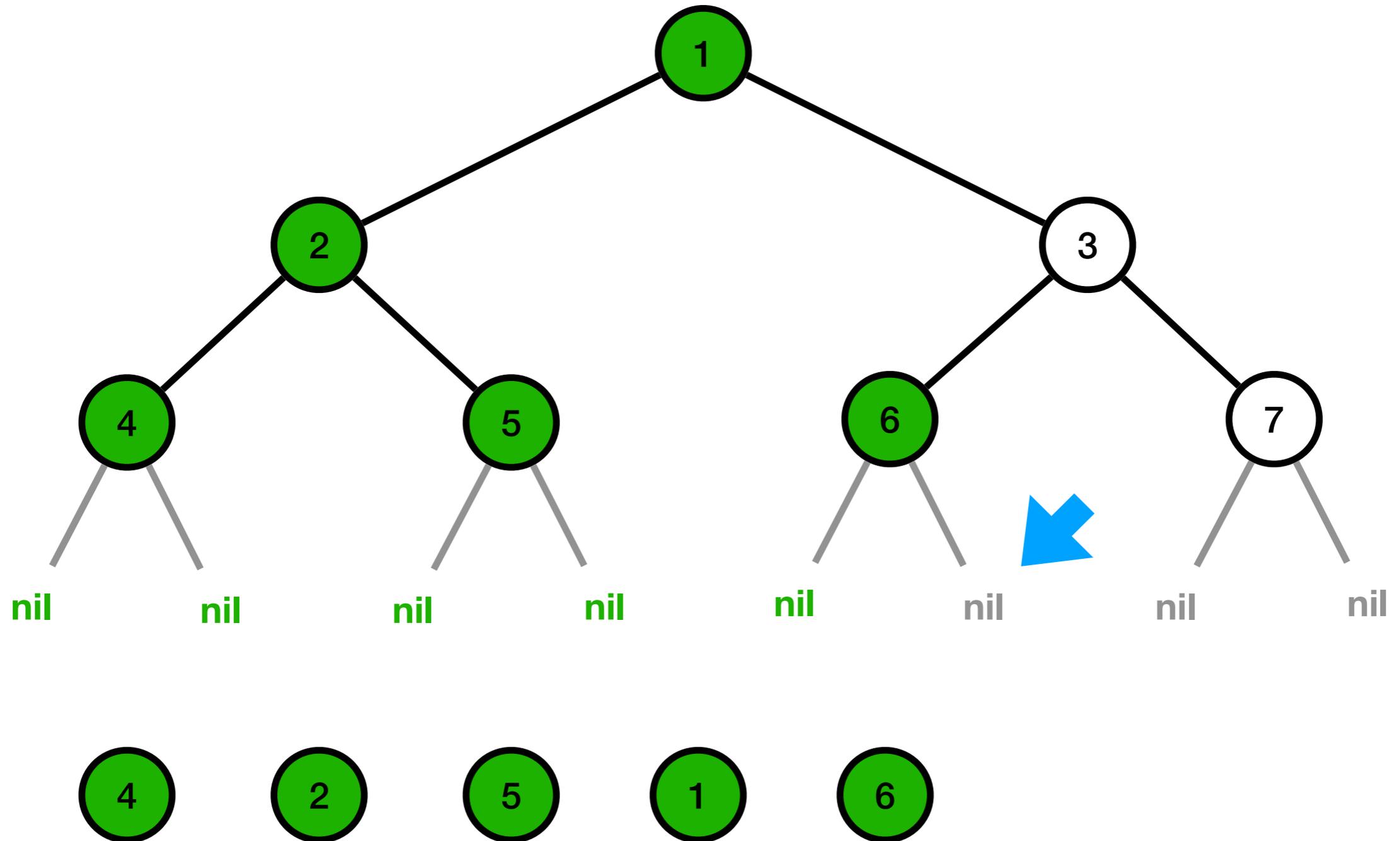
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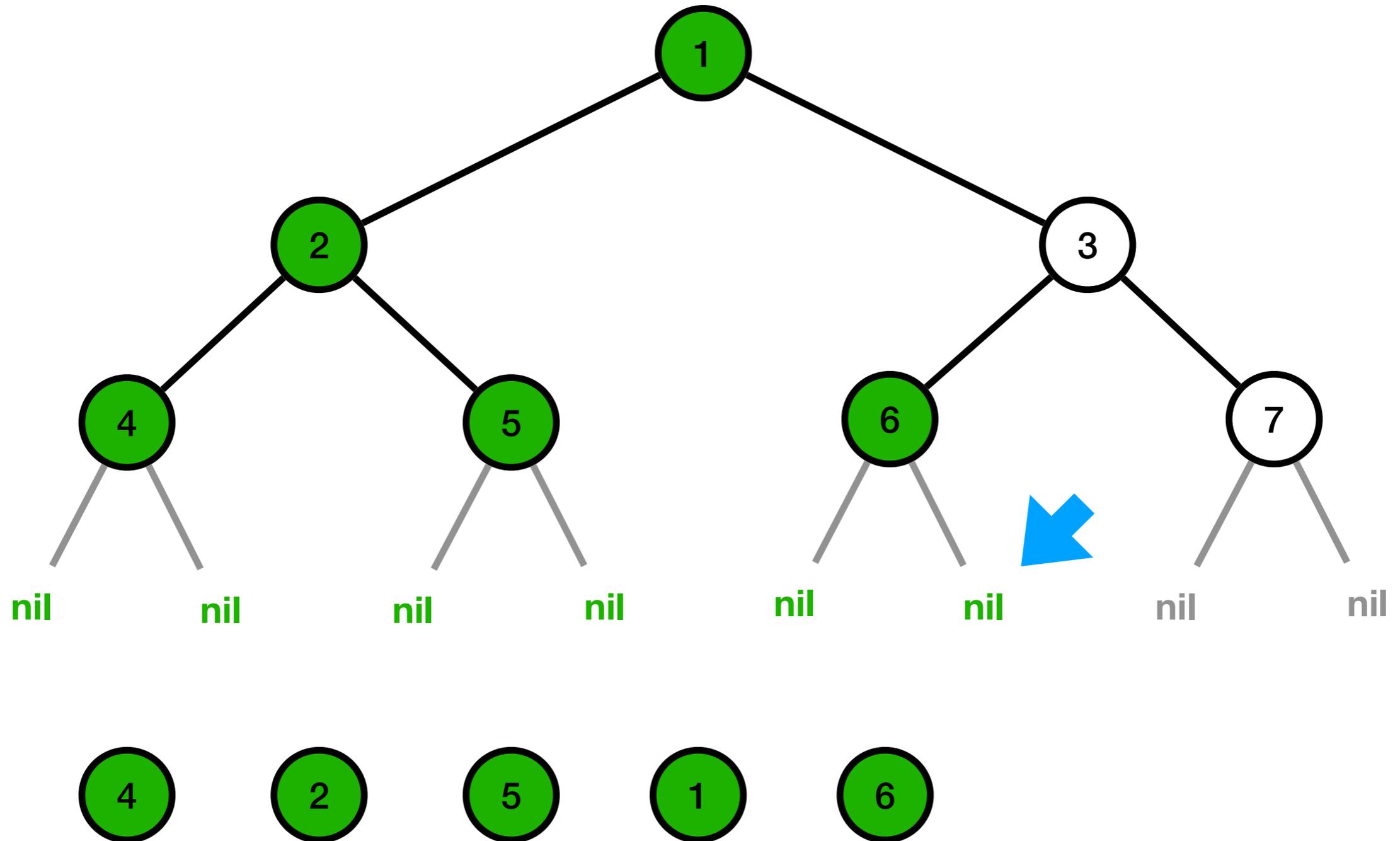
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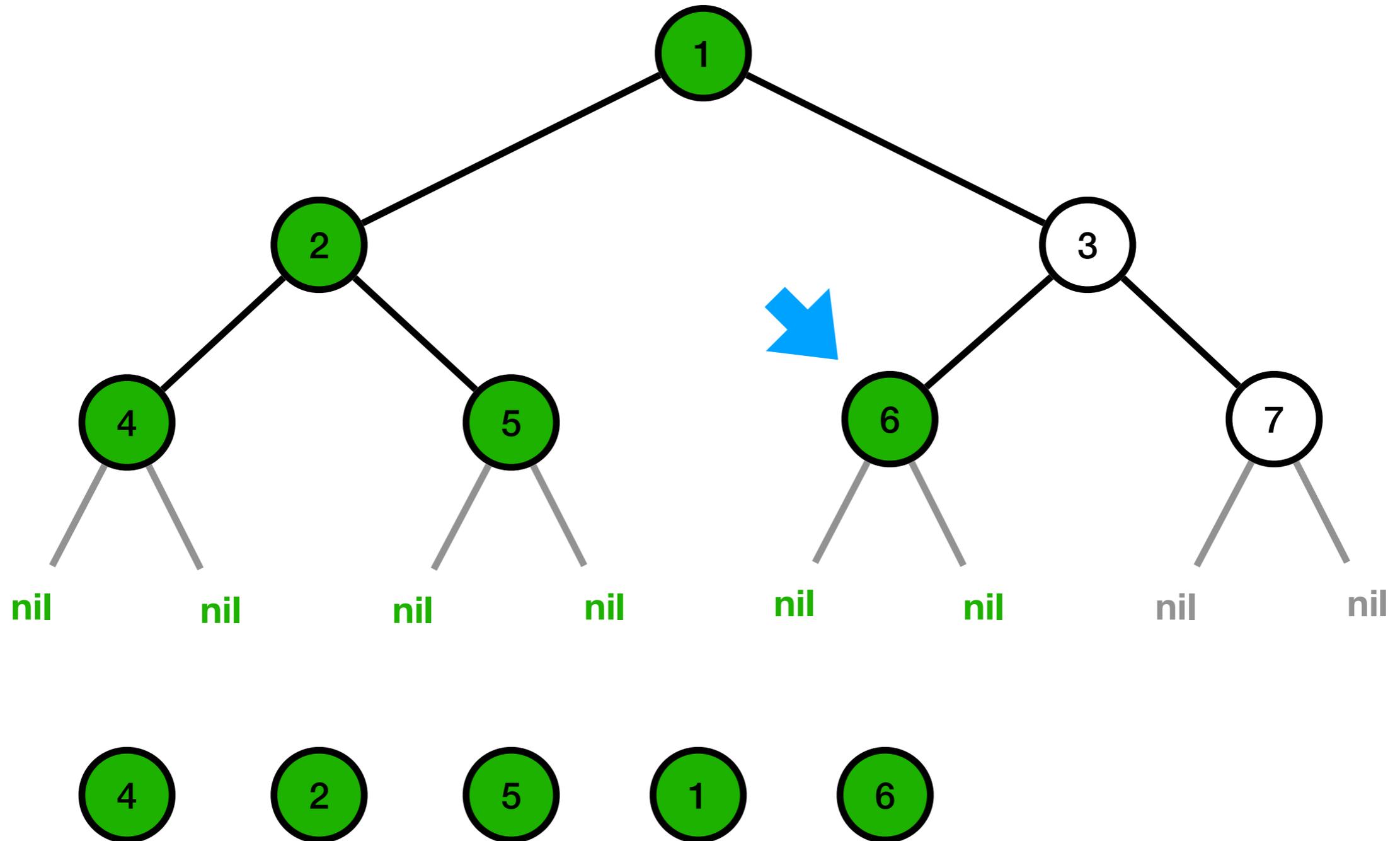
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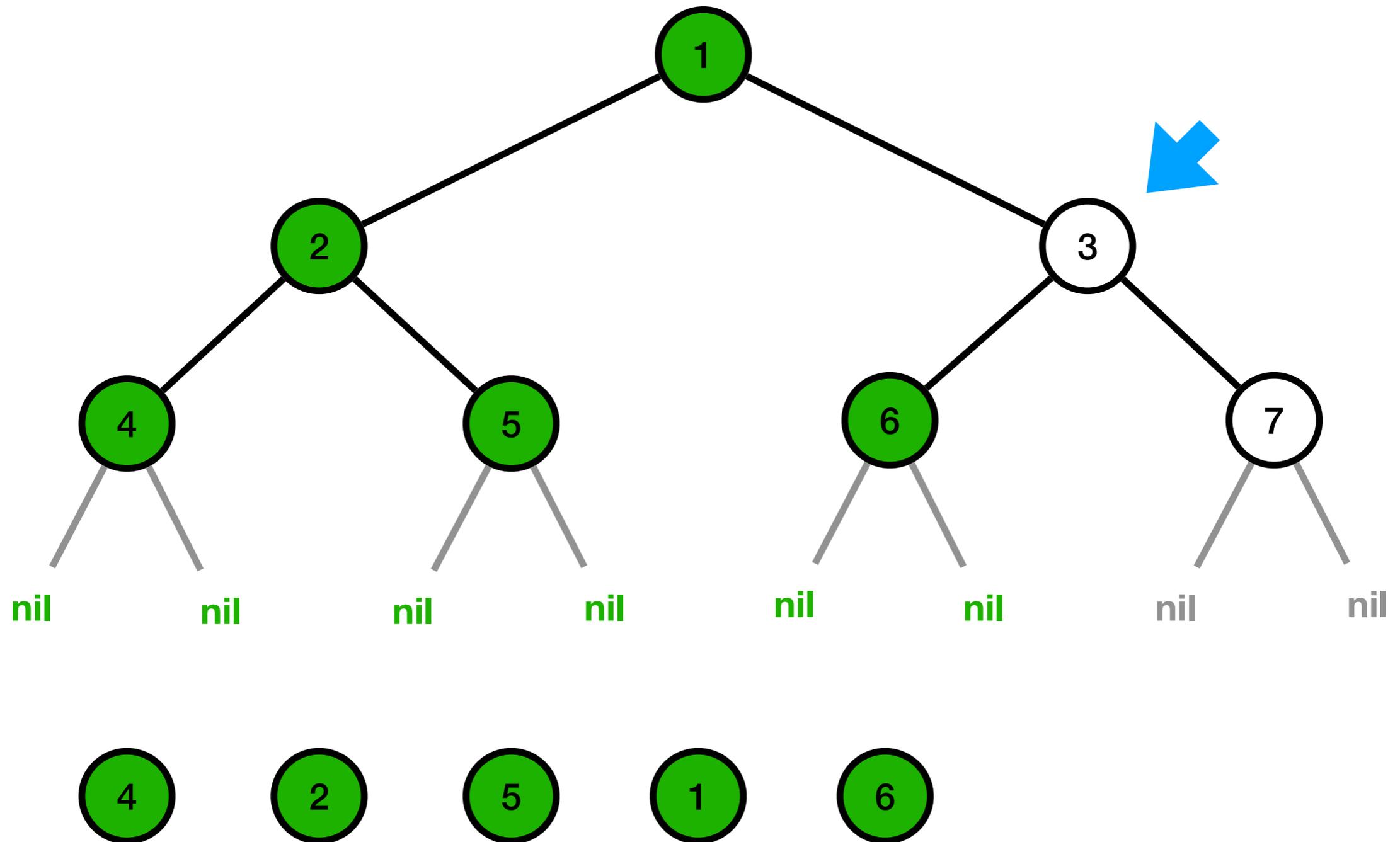
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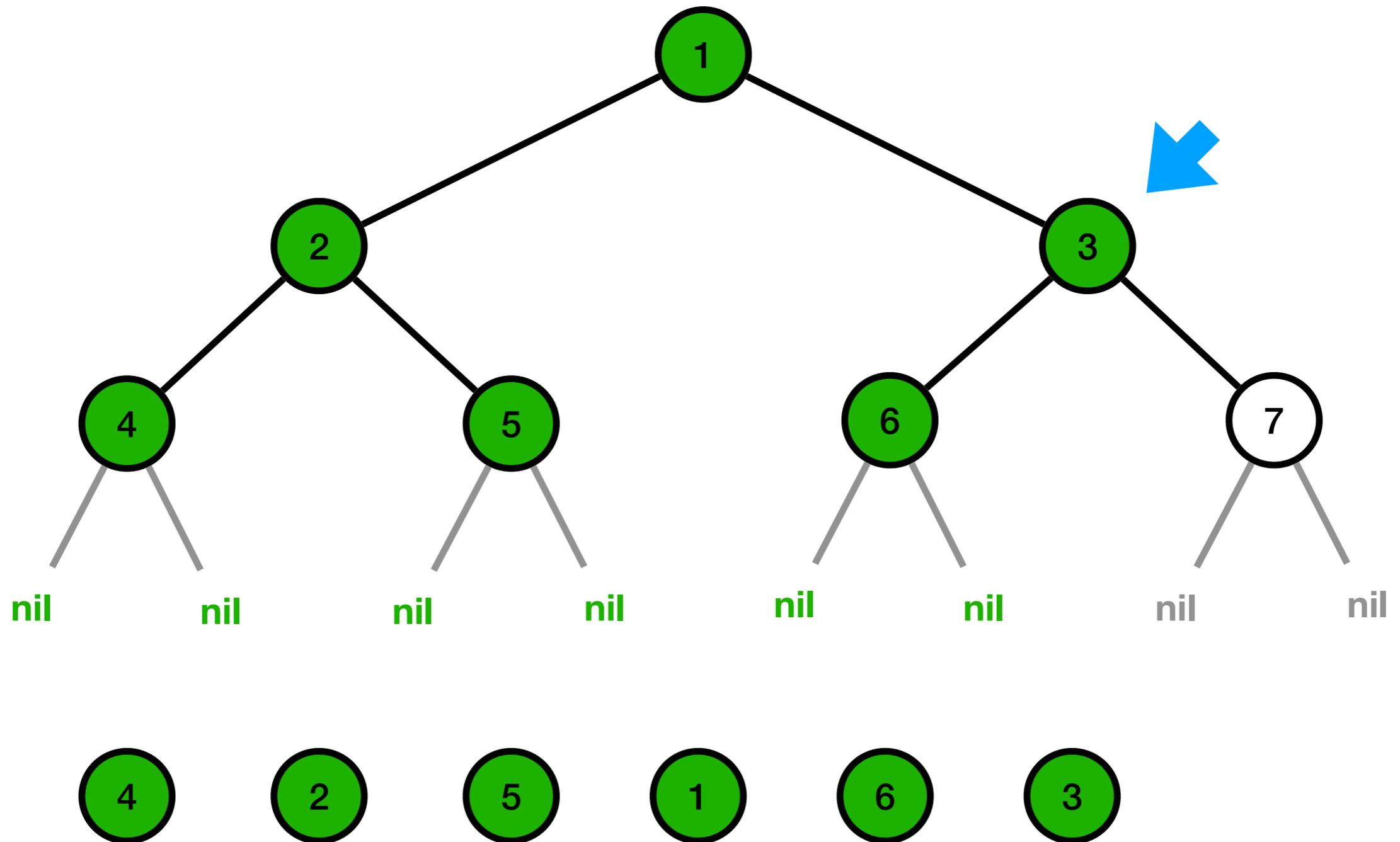
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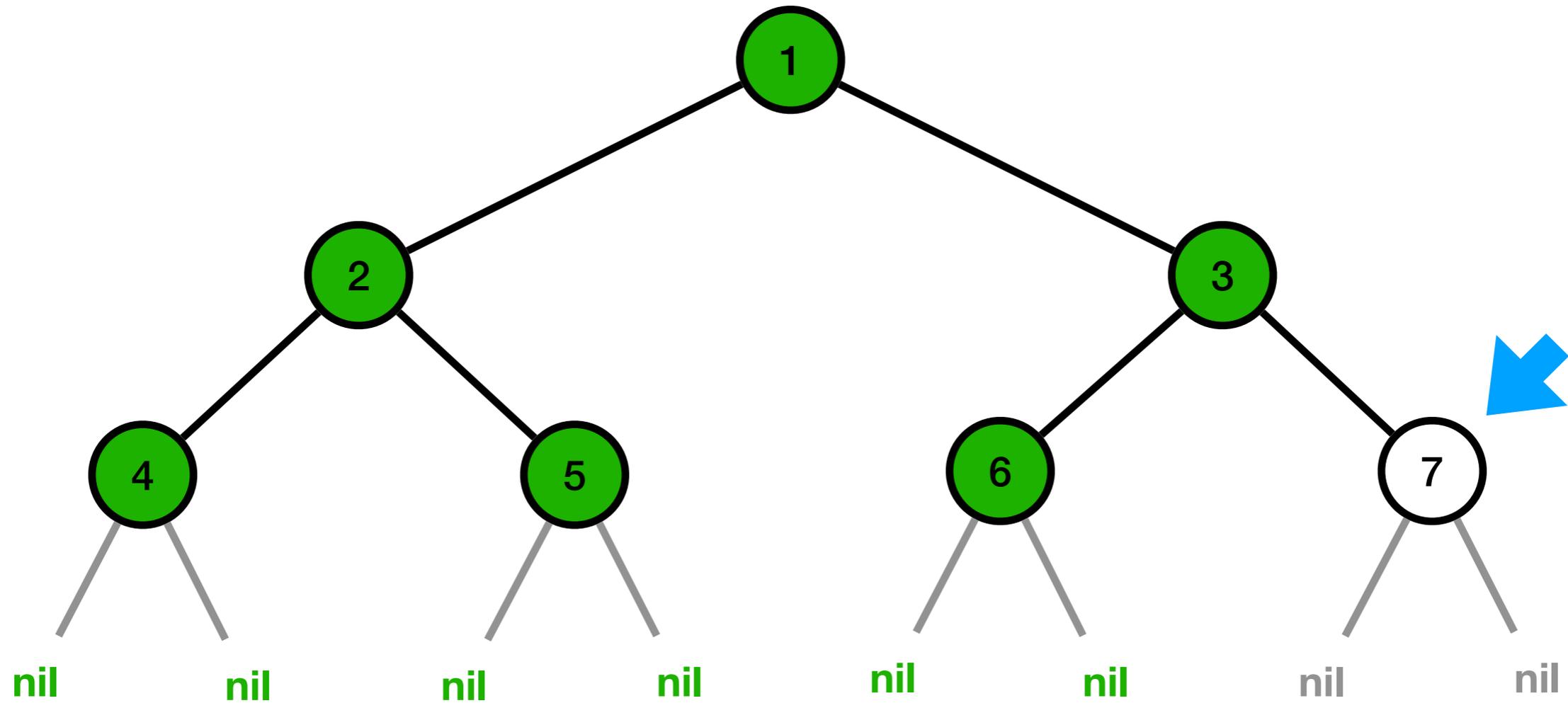
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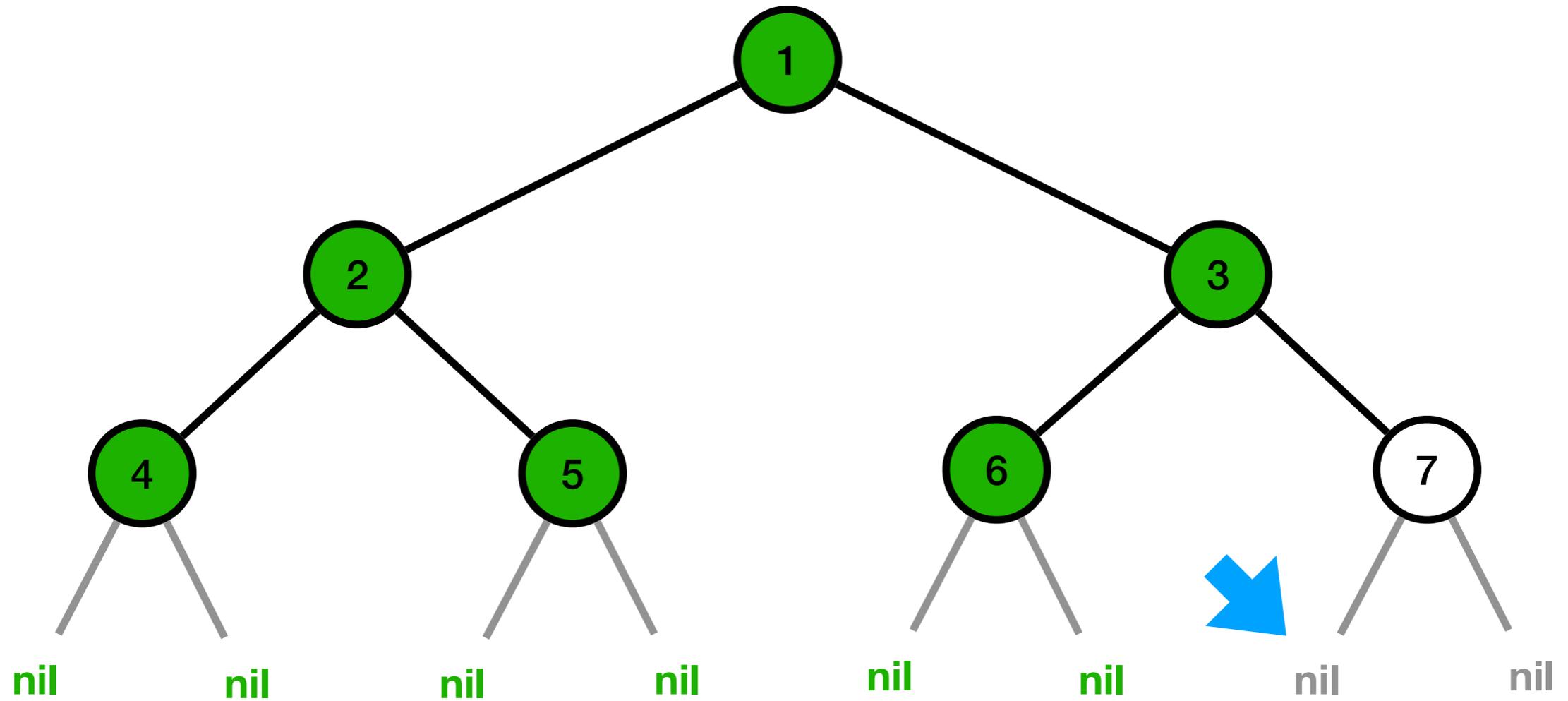
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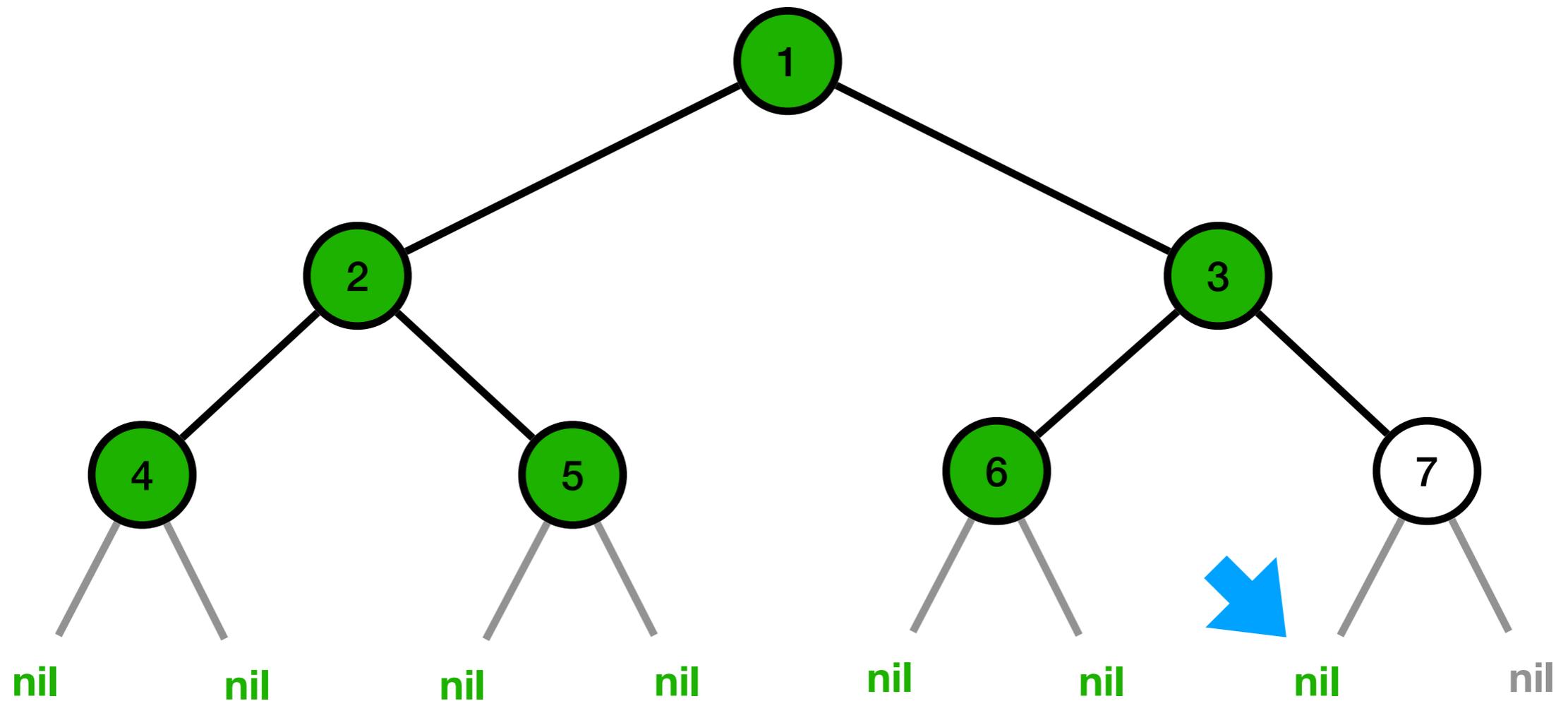
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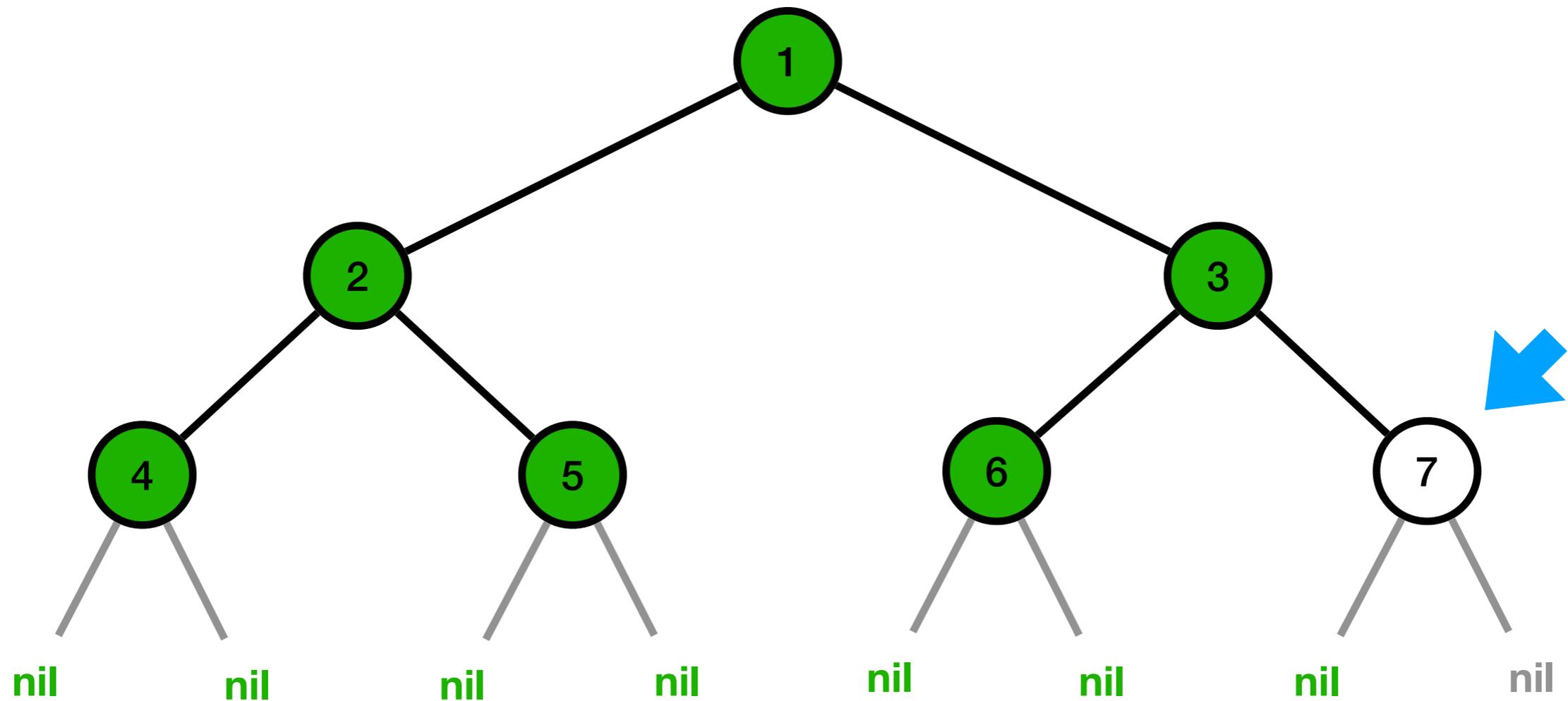
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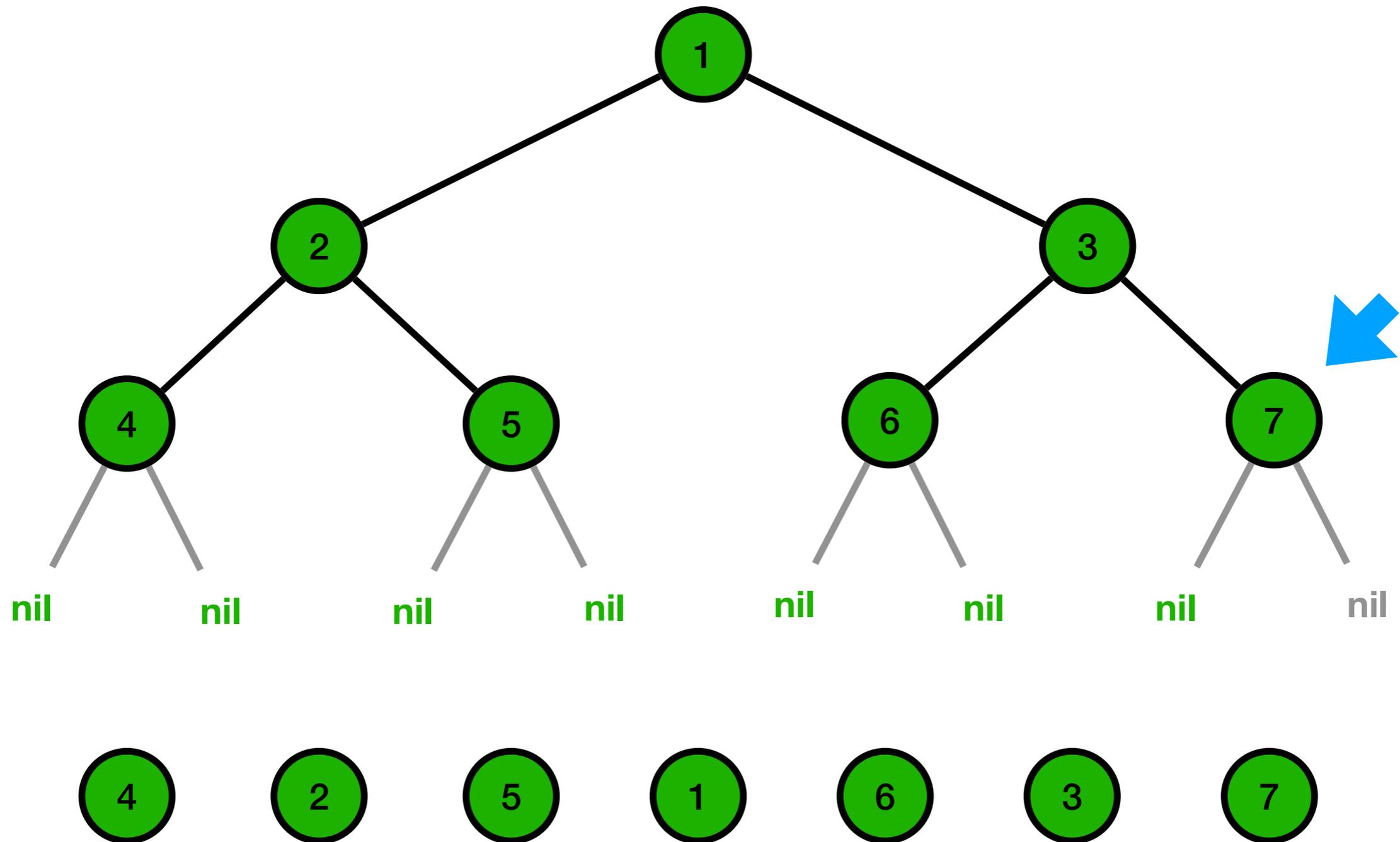
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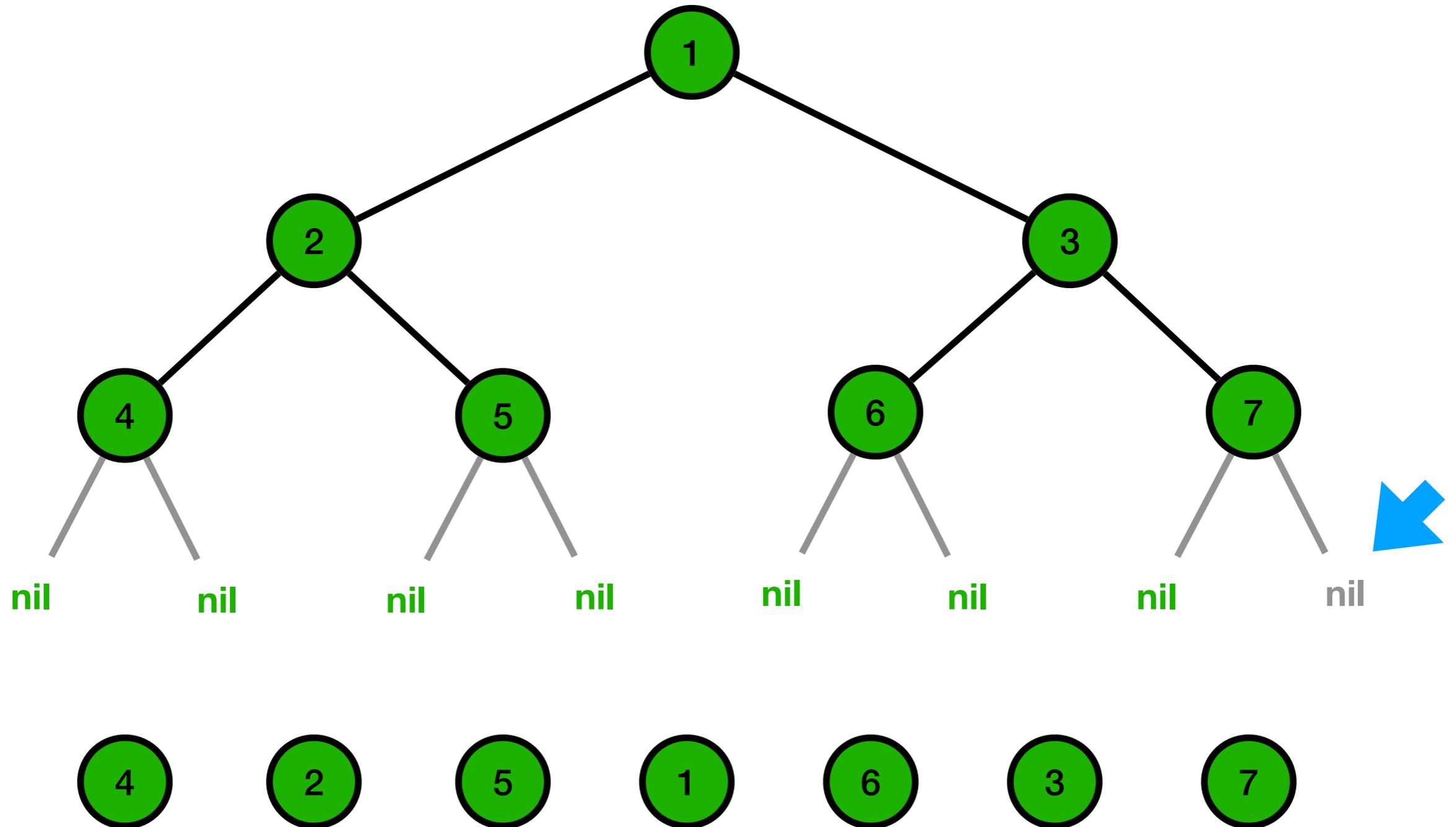
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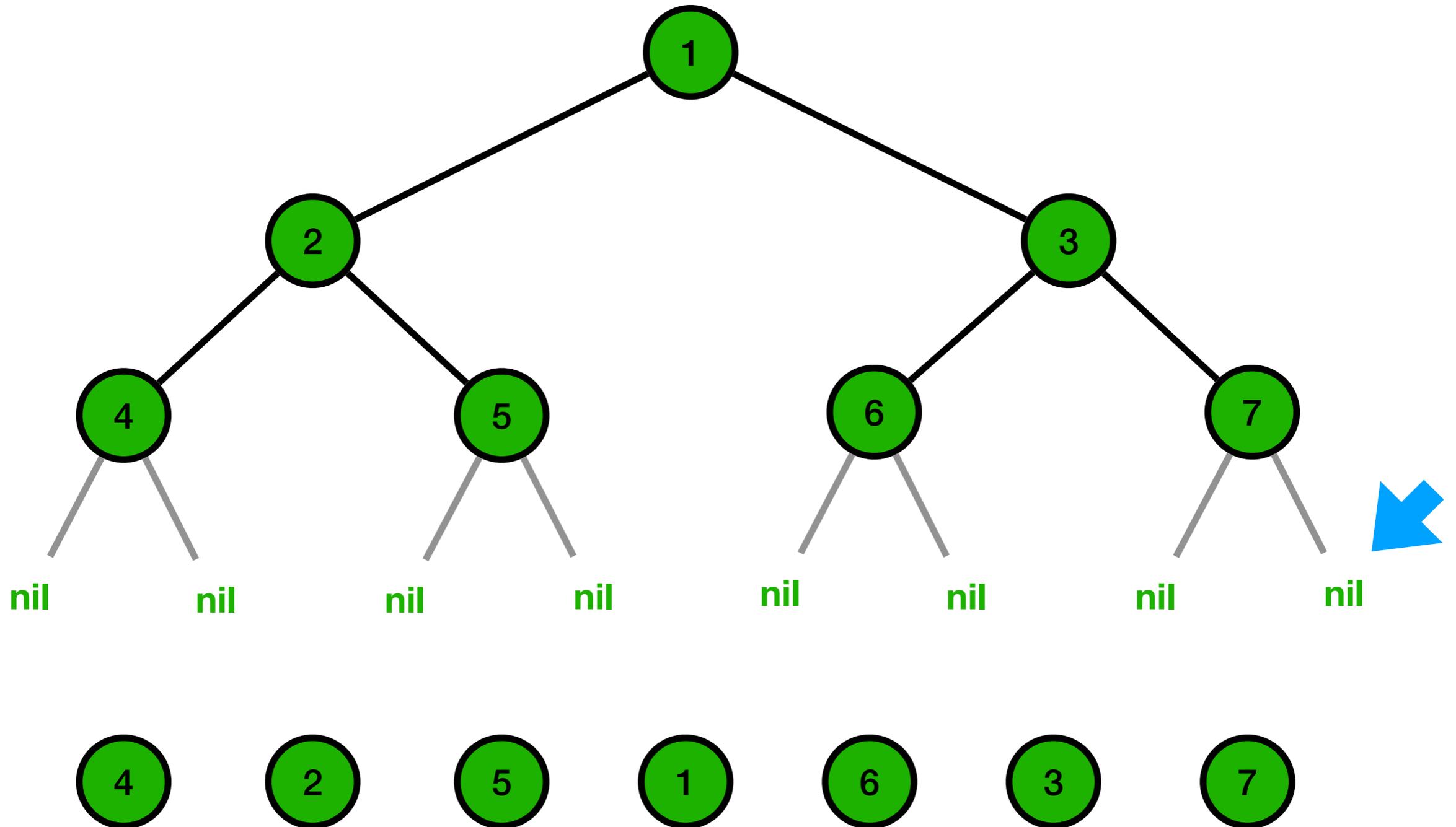
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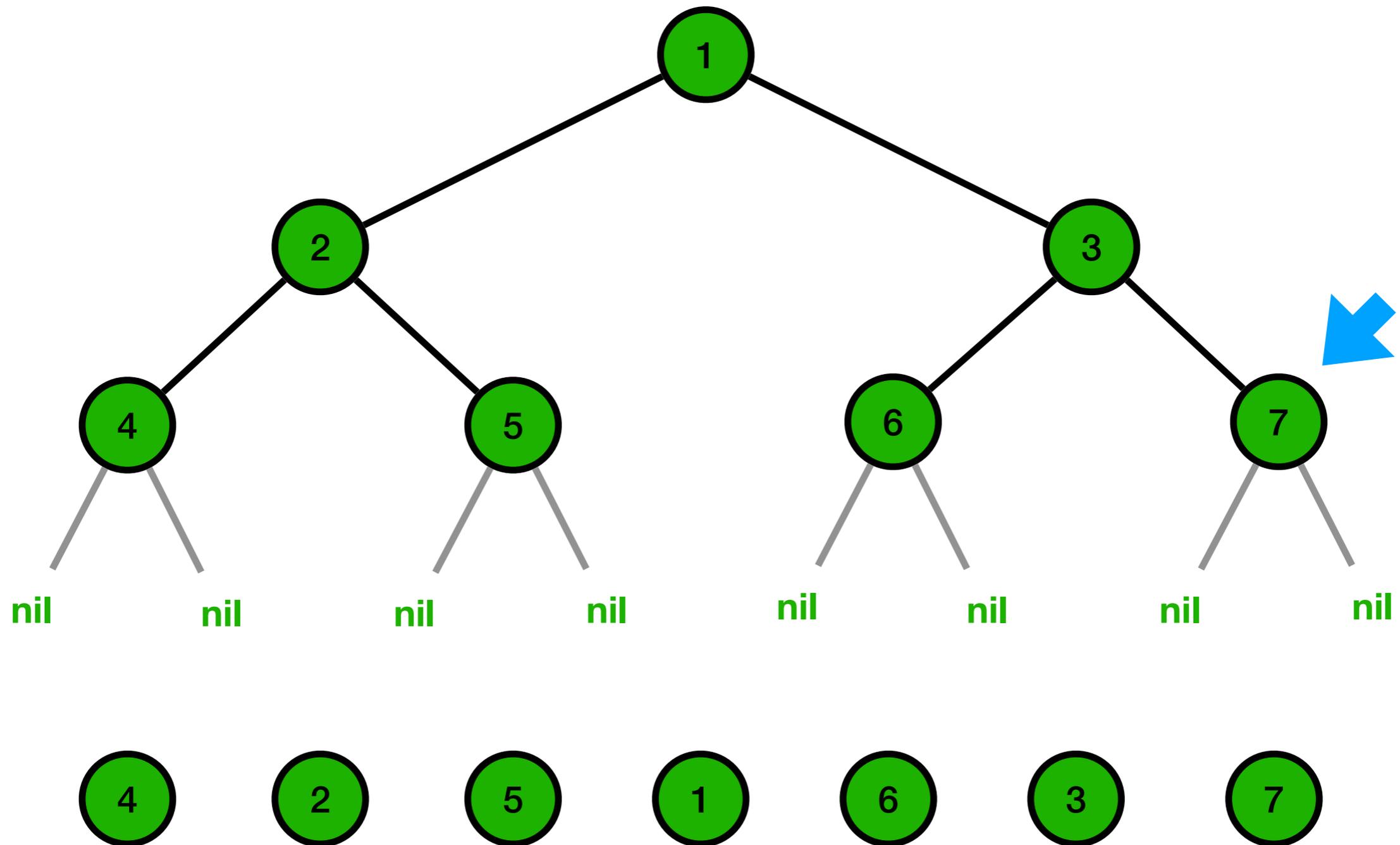
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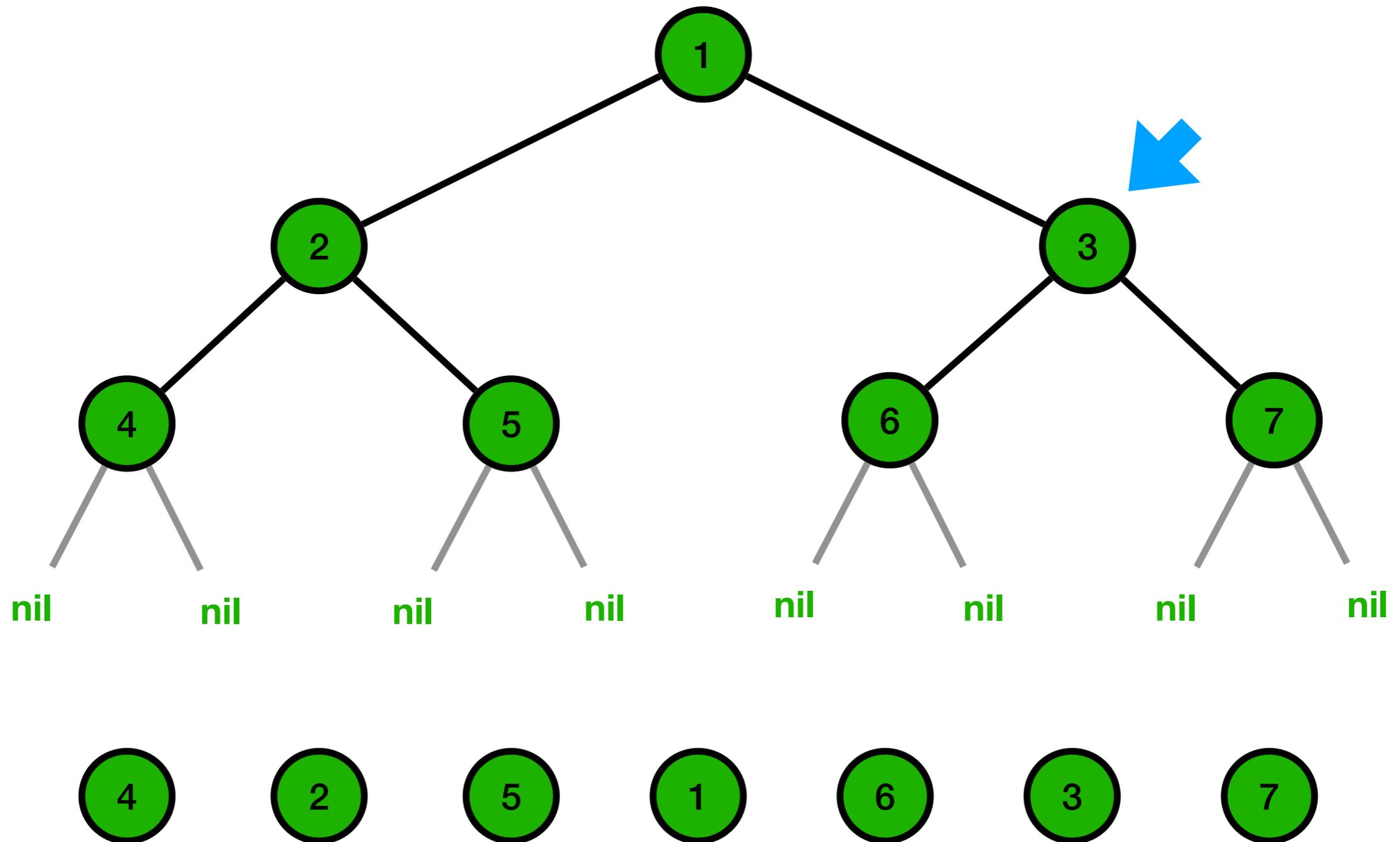
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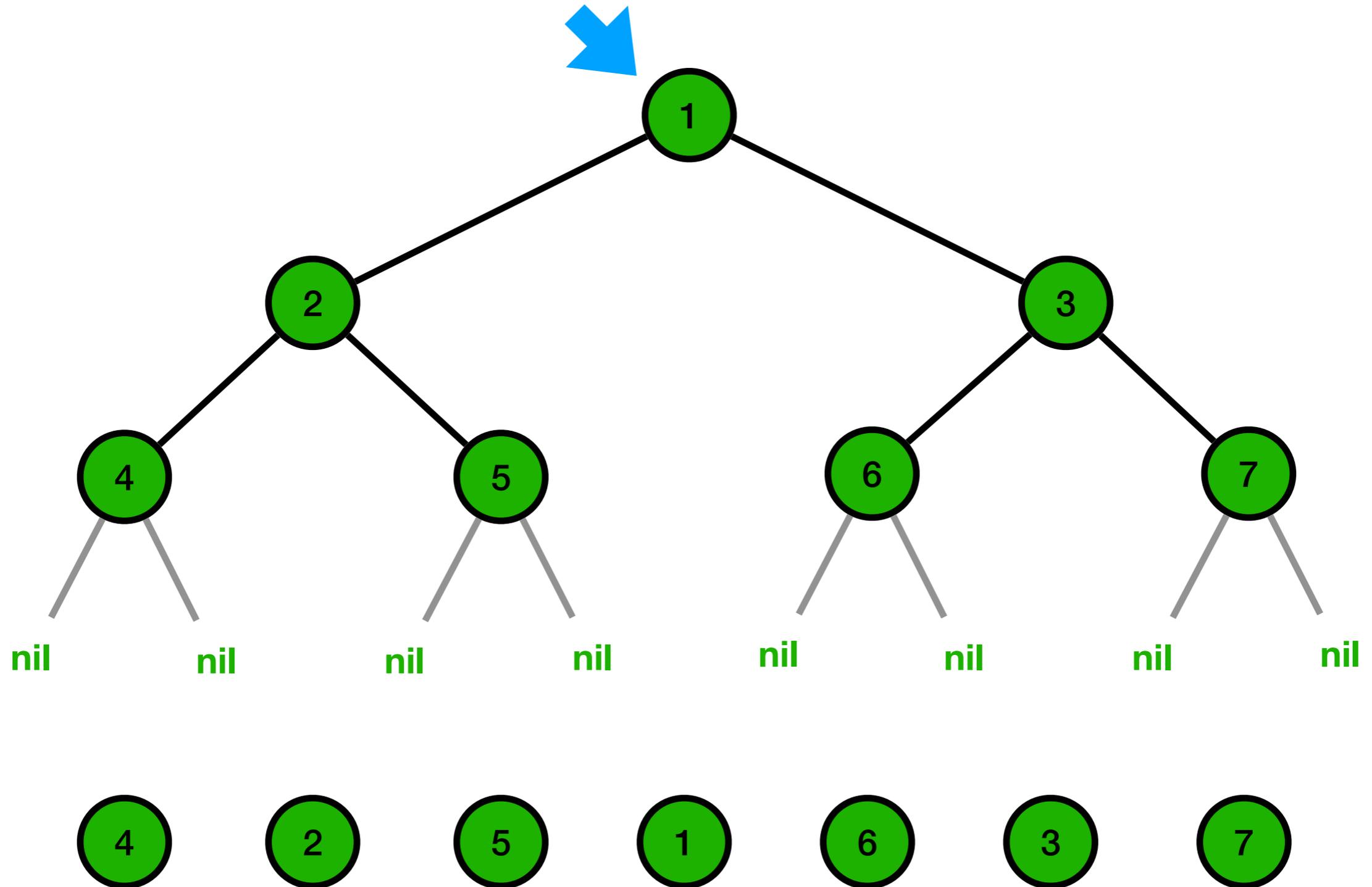
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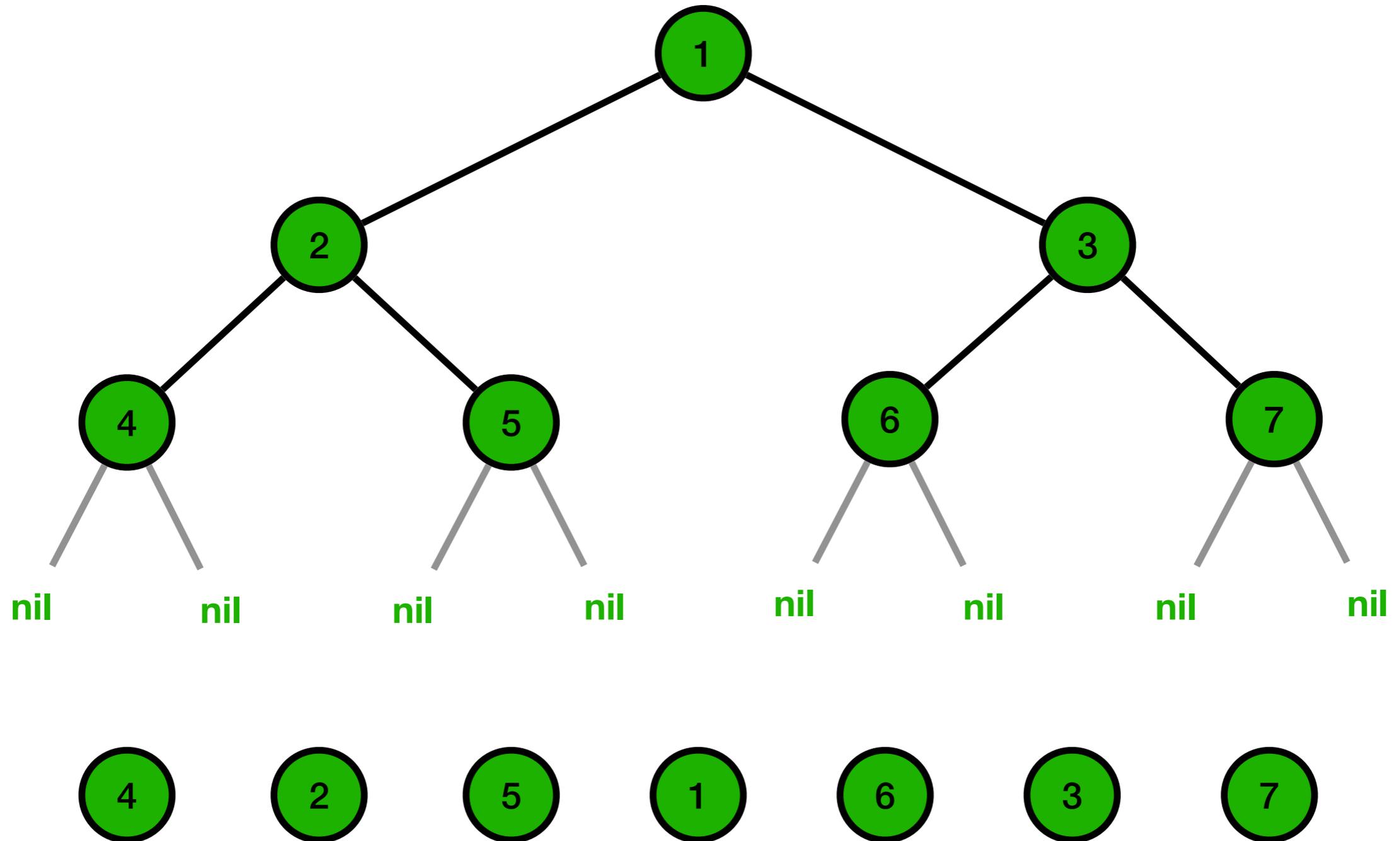
Parcours infixe



Parcours infixe



Parcours infixe



Expressions arithmétiques

Une expression arithmétique (totalement parenthésée) est :

- soit un nombre entier n
- soit une somme parenthésée $(e_1 + e_2)$, où e_1 et e_2 sont deux sub-expressions (totalement parenthésée)
- soit une soustraction parenthésée $(e_1 - e_2)$
- soit un produit parenthésé $(e_1 \times e_2)$
- soit une division parenthésée $(e_1 \div e_2)$

Exemples d'expressions

Exemples d'expressions

5

3

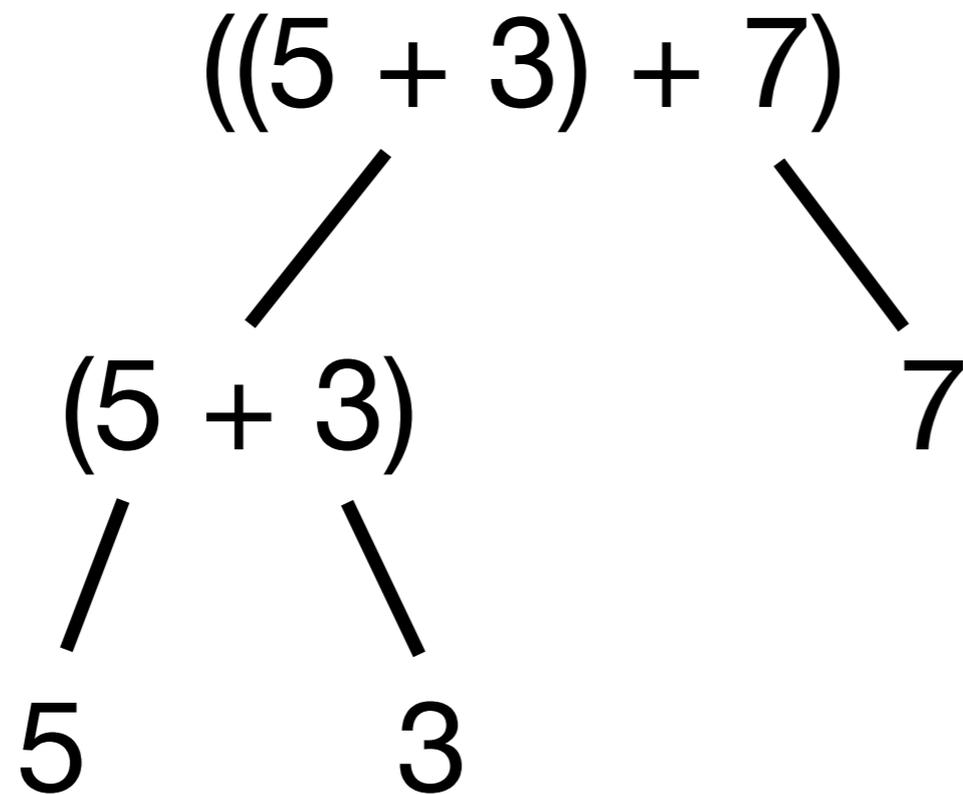
Exemples d'expressions

$$\begin{array}{c} (5 + 3) \\ / \quad \backslash \\ 5 \quad 3 \end{array}$$

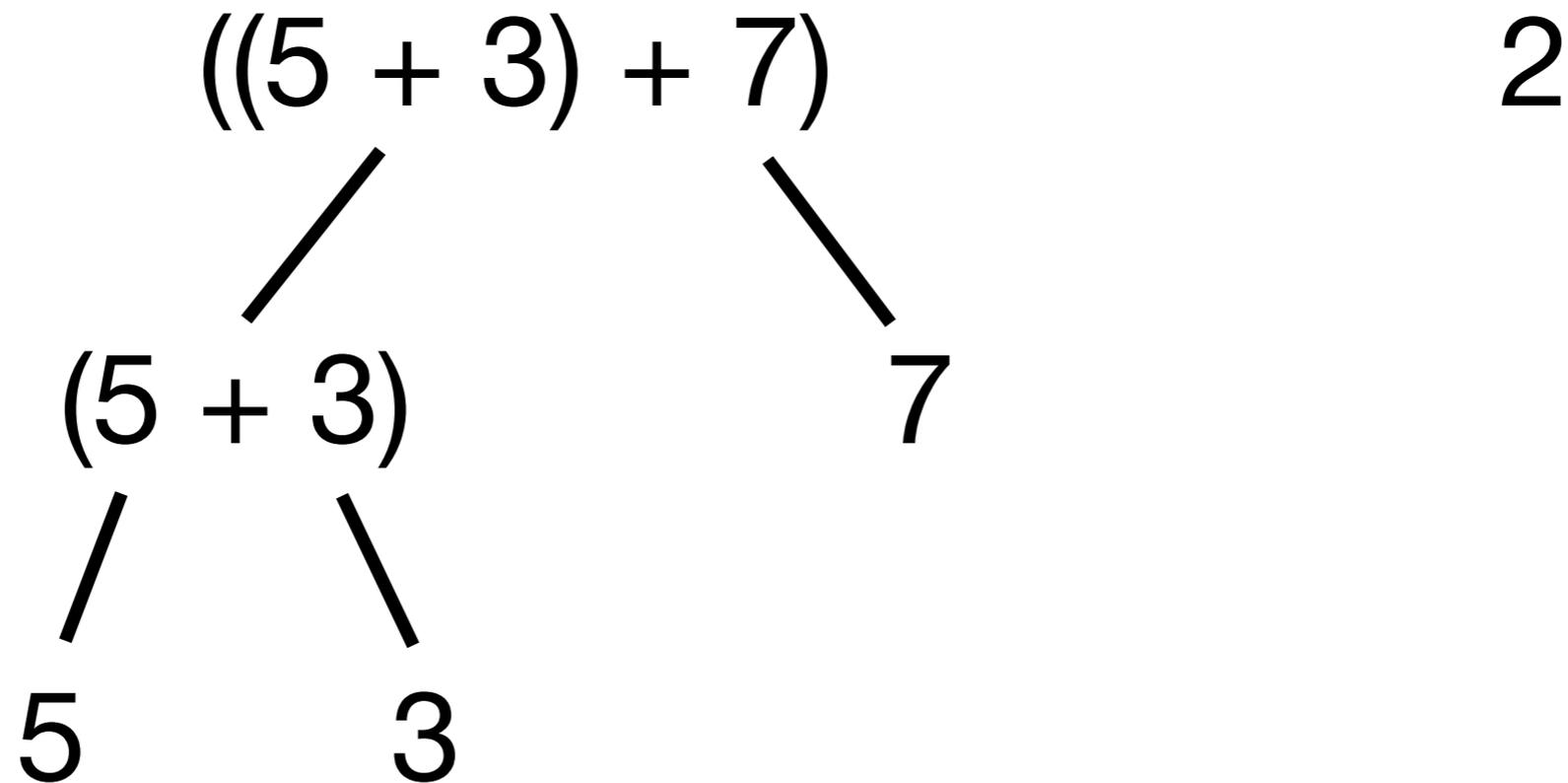
Exemples d'expressions

$$\begin{array}{c} (5 + 3) \\ / \quad \backslash \\ 5 \quad 3 \end{array} \quad 7$$

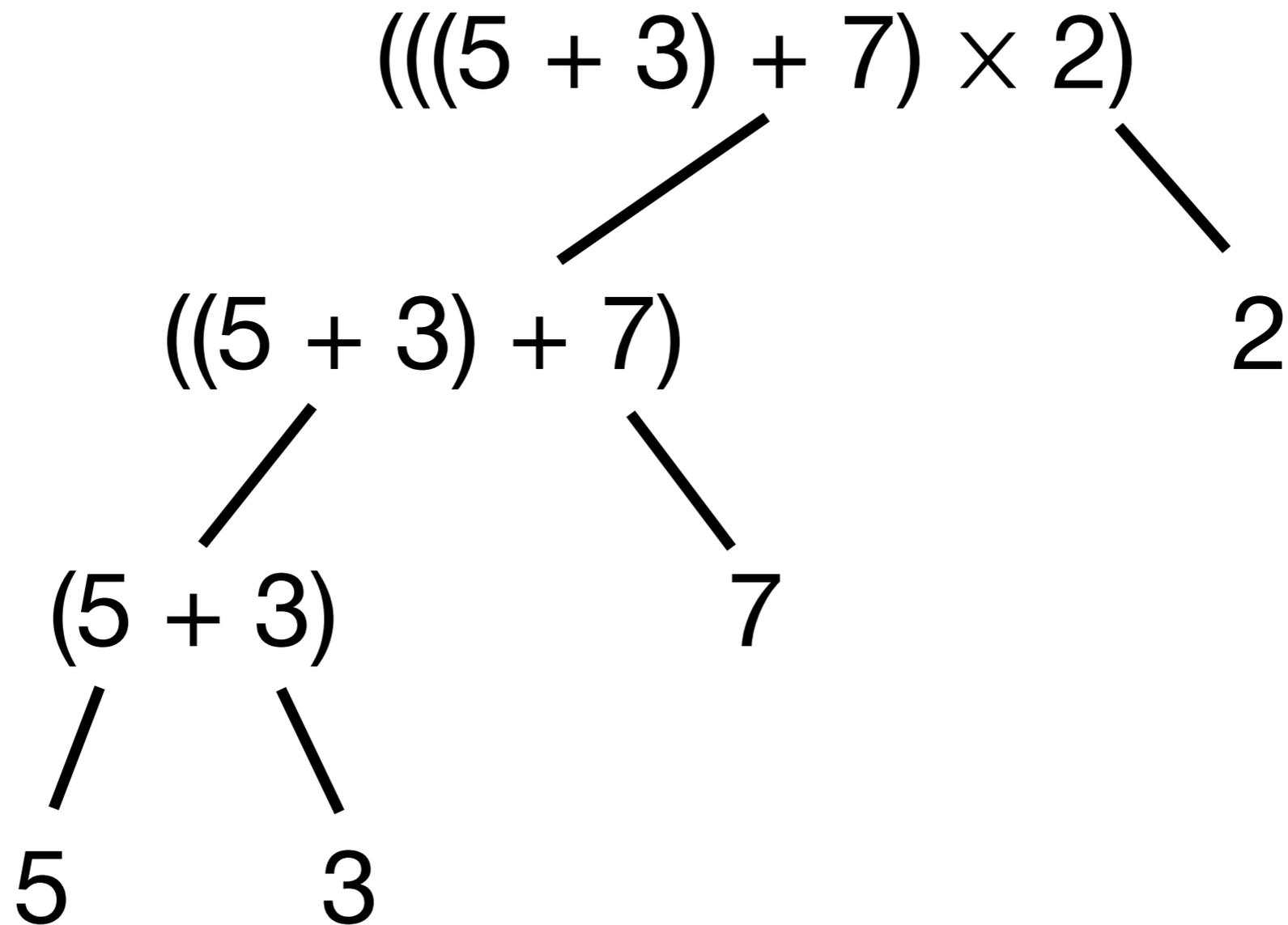
Exemples d'expressions



Exemples d'expressions



Exemples d'expressions



Exemples d'expressions

5

3

7

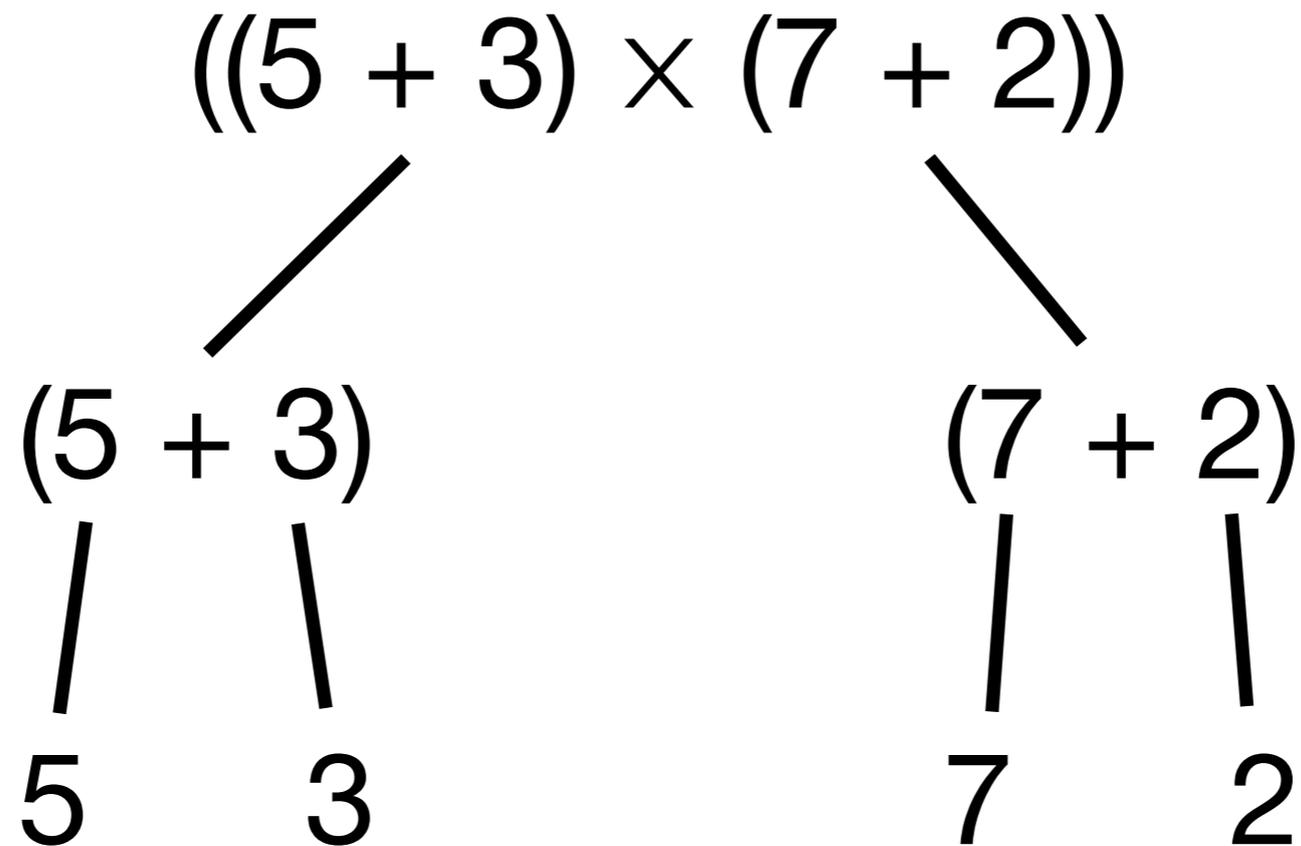
2

Exemples d'expressions

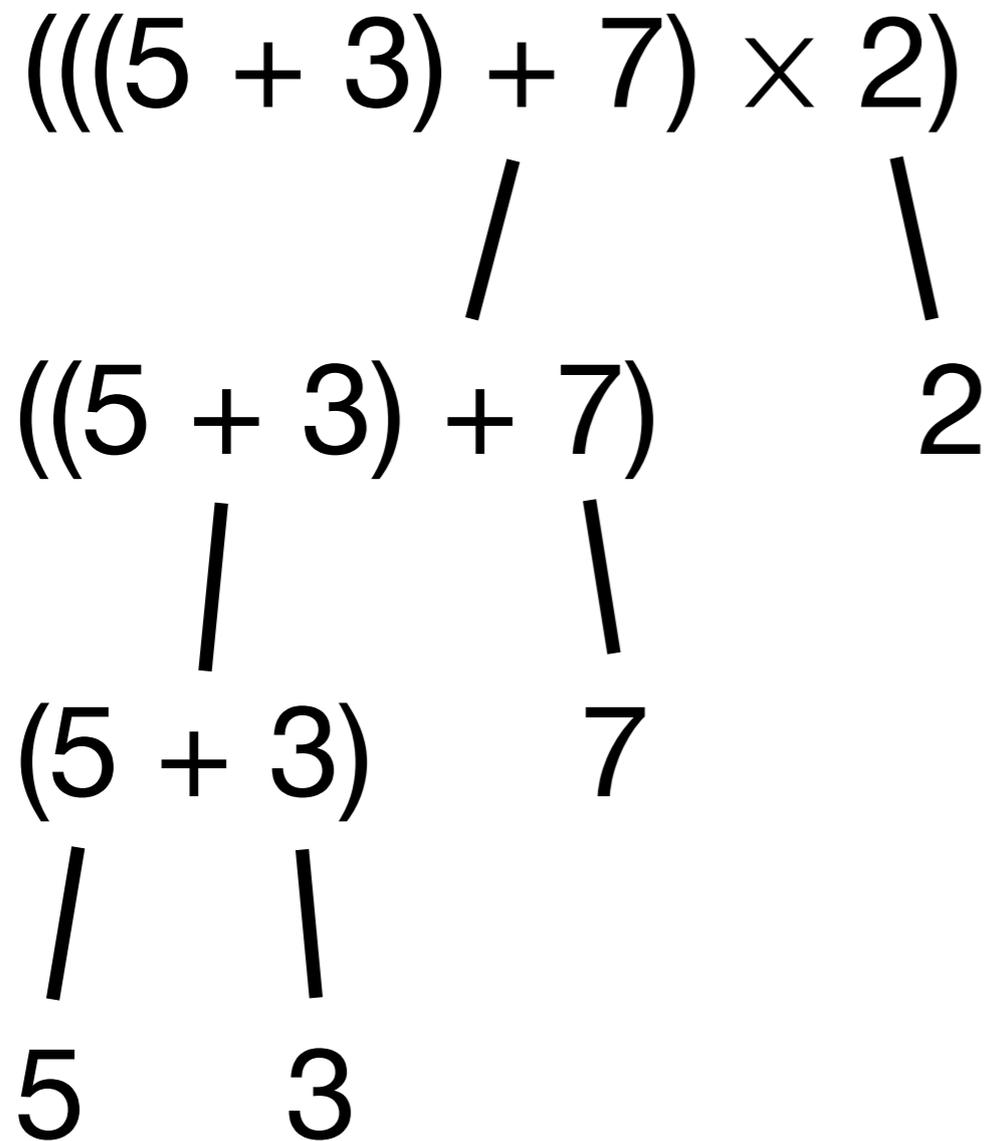
$$\begin{array}{c} (5 + 3) \\ | \quad \backslash \\ 5 \quad 3 \end{array}$$

$$\begin{array}{c} (7 + 2) \\ | \quad \backslash \\ 7 \quad 2 \end{array}$$

Exemples d'expressions



Représentation d'expressions



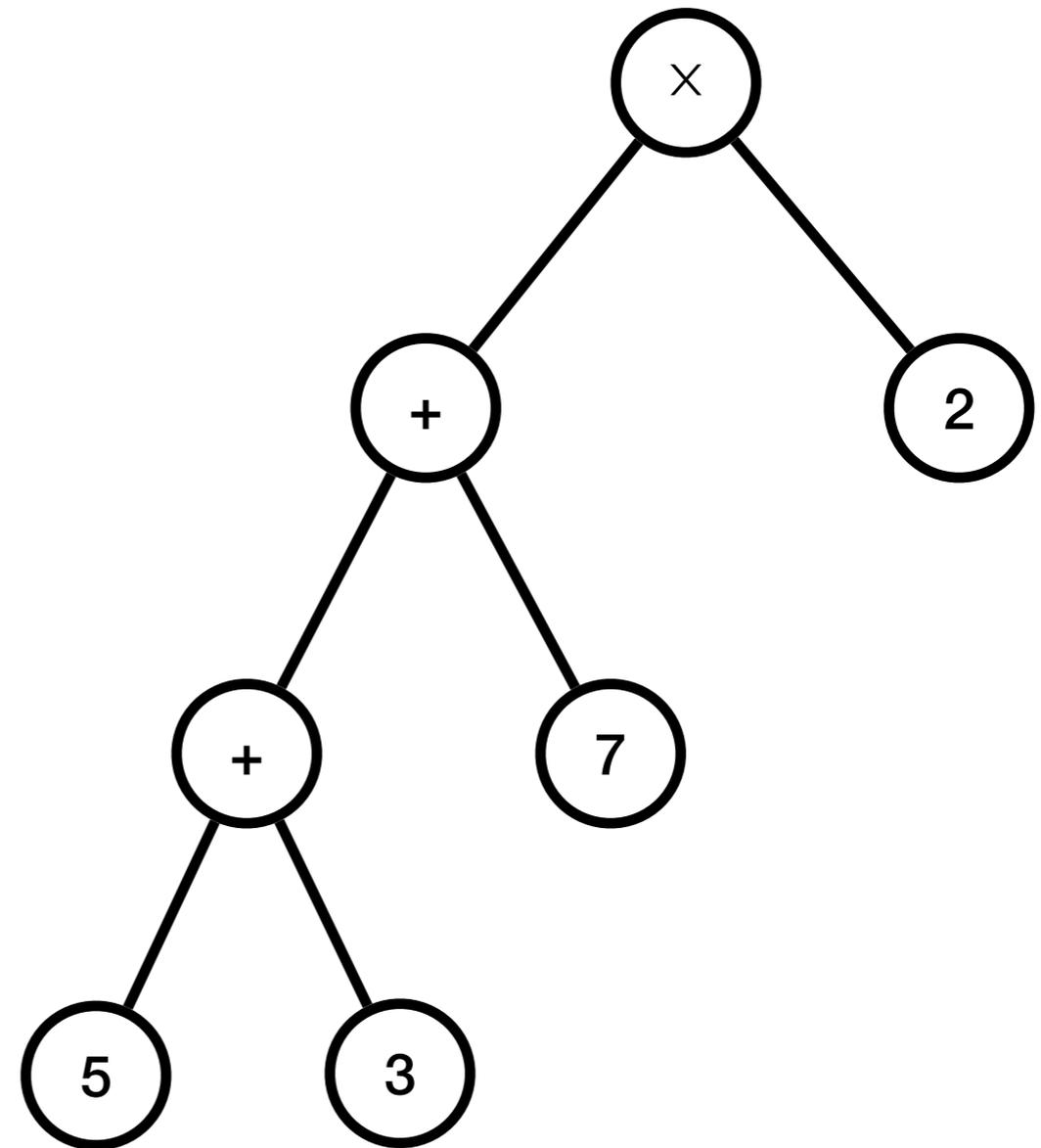
Représentation d'expressions

$((5 + 3) + 7) \times 2$

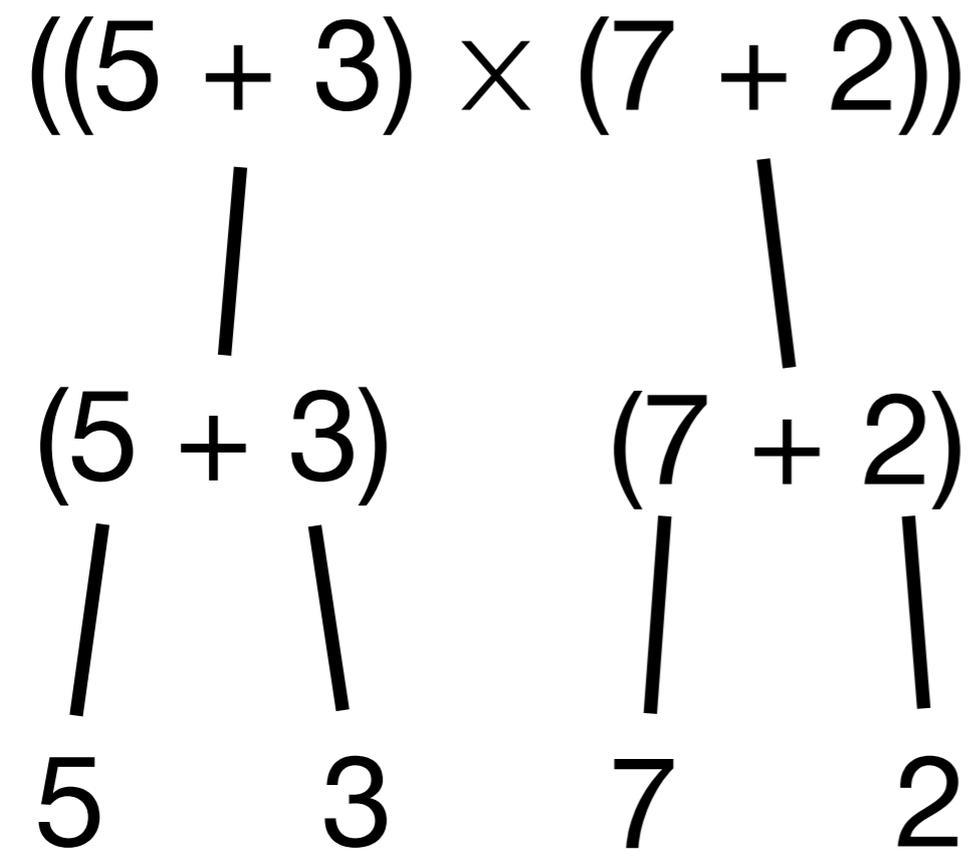
$((5 + 3) + 7)$ 2

$(5 + 3)$ 7

5 3

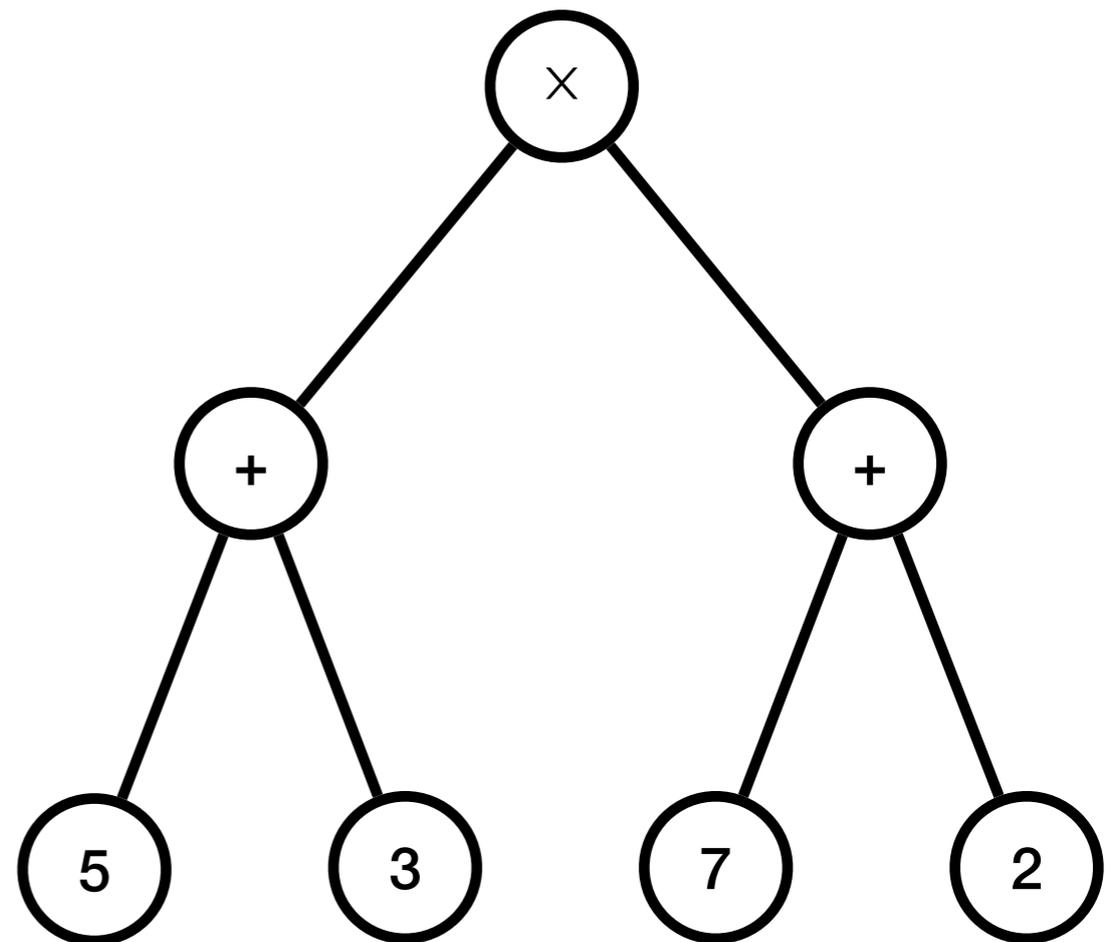
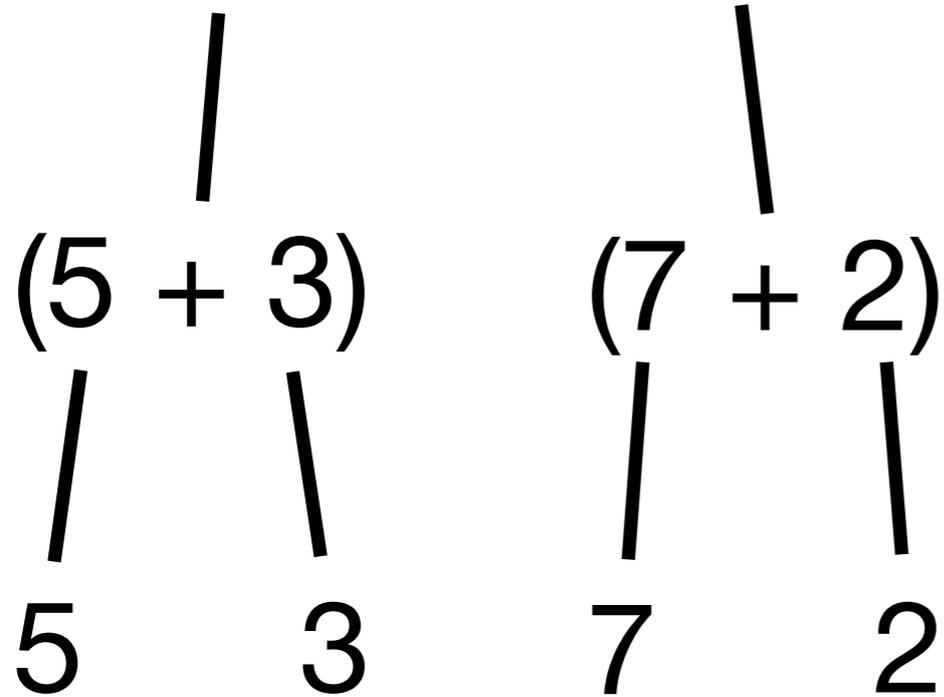


Représentation d'expressions

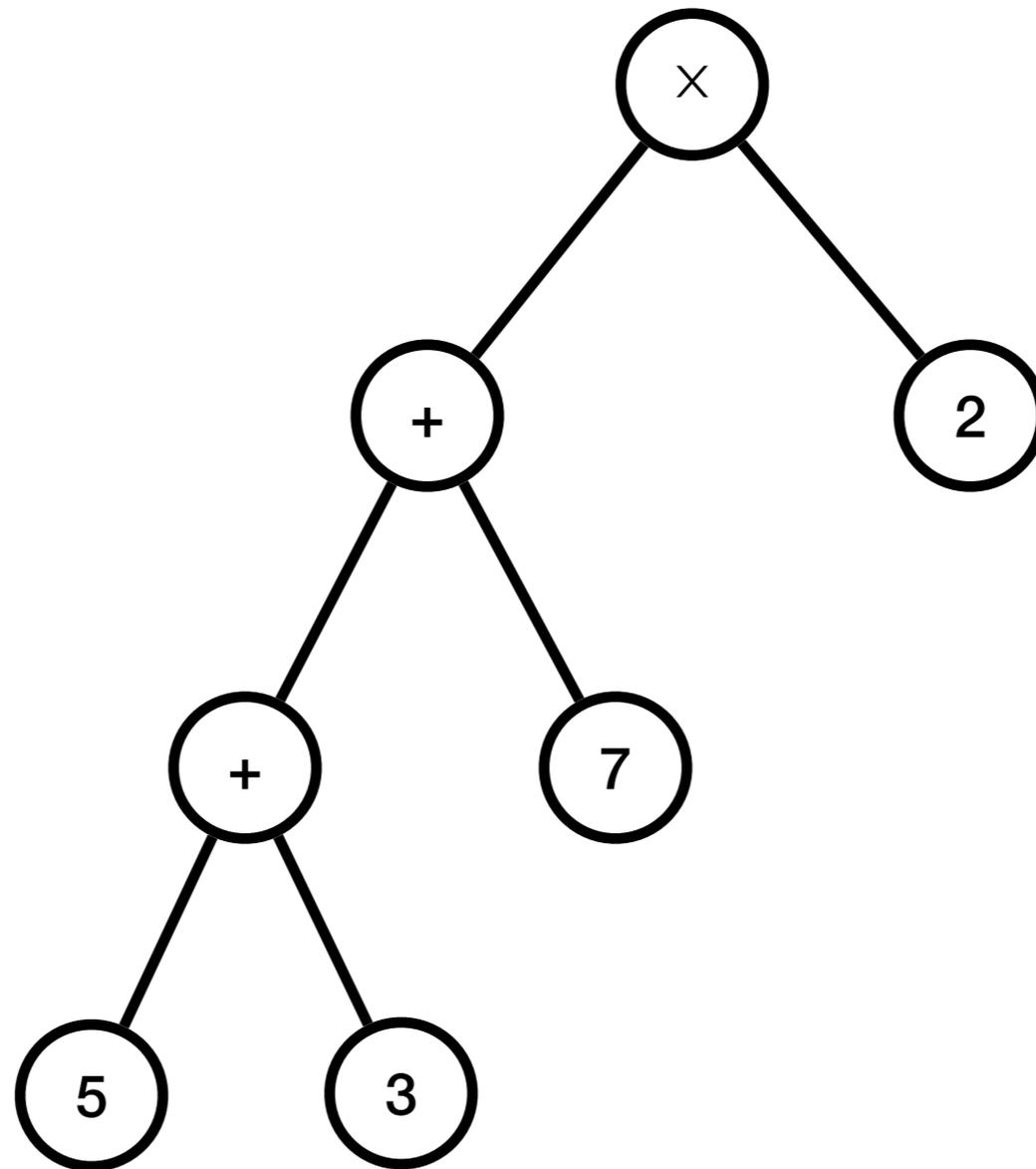


Représentation d'expressions

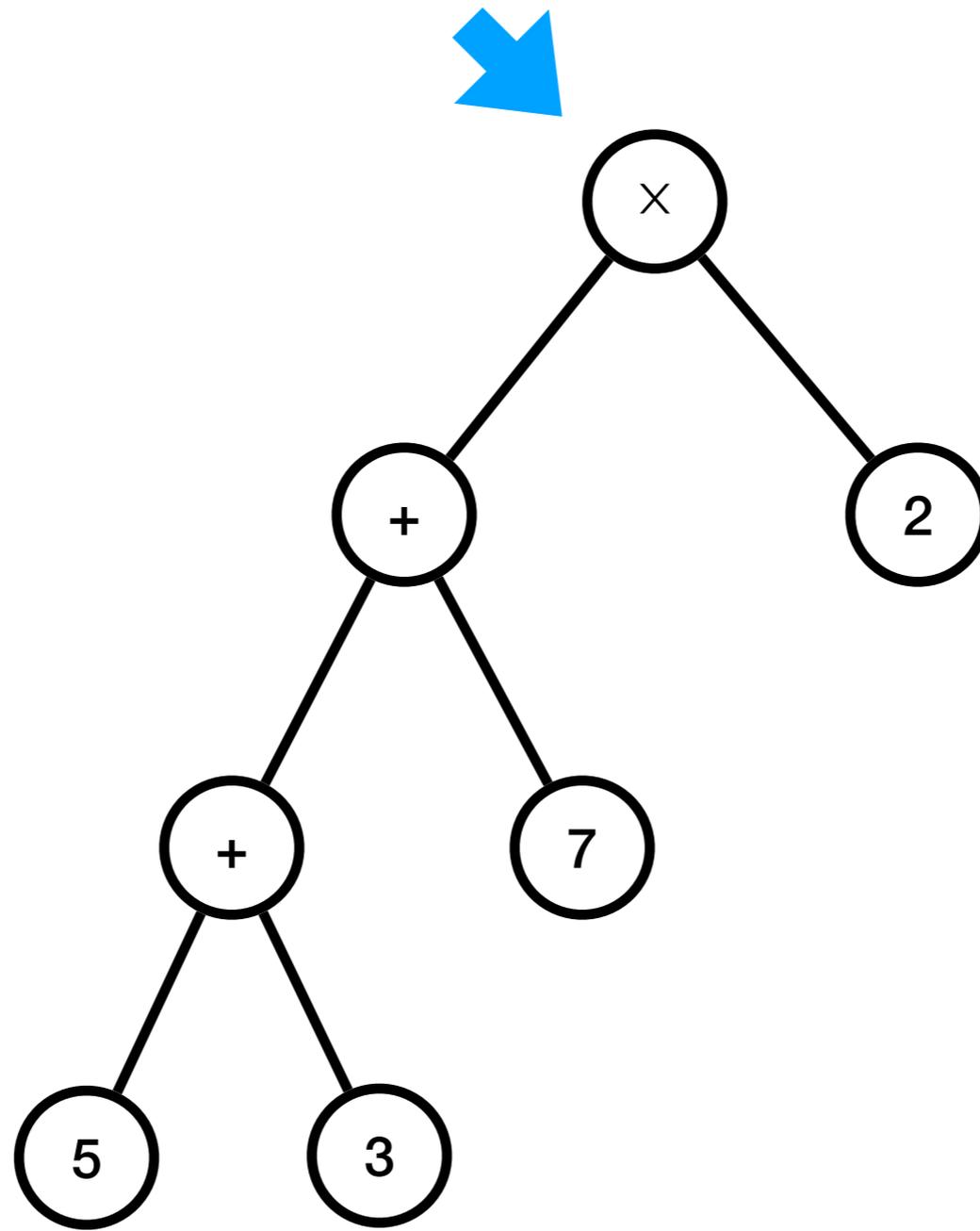
$((5 + 3) \times (7 + 2))$



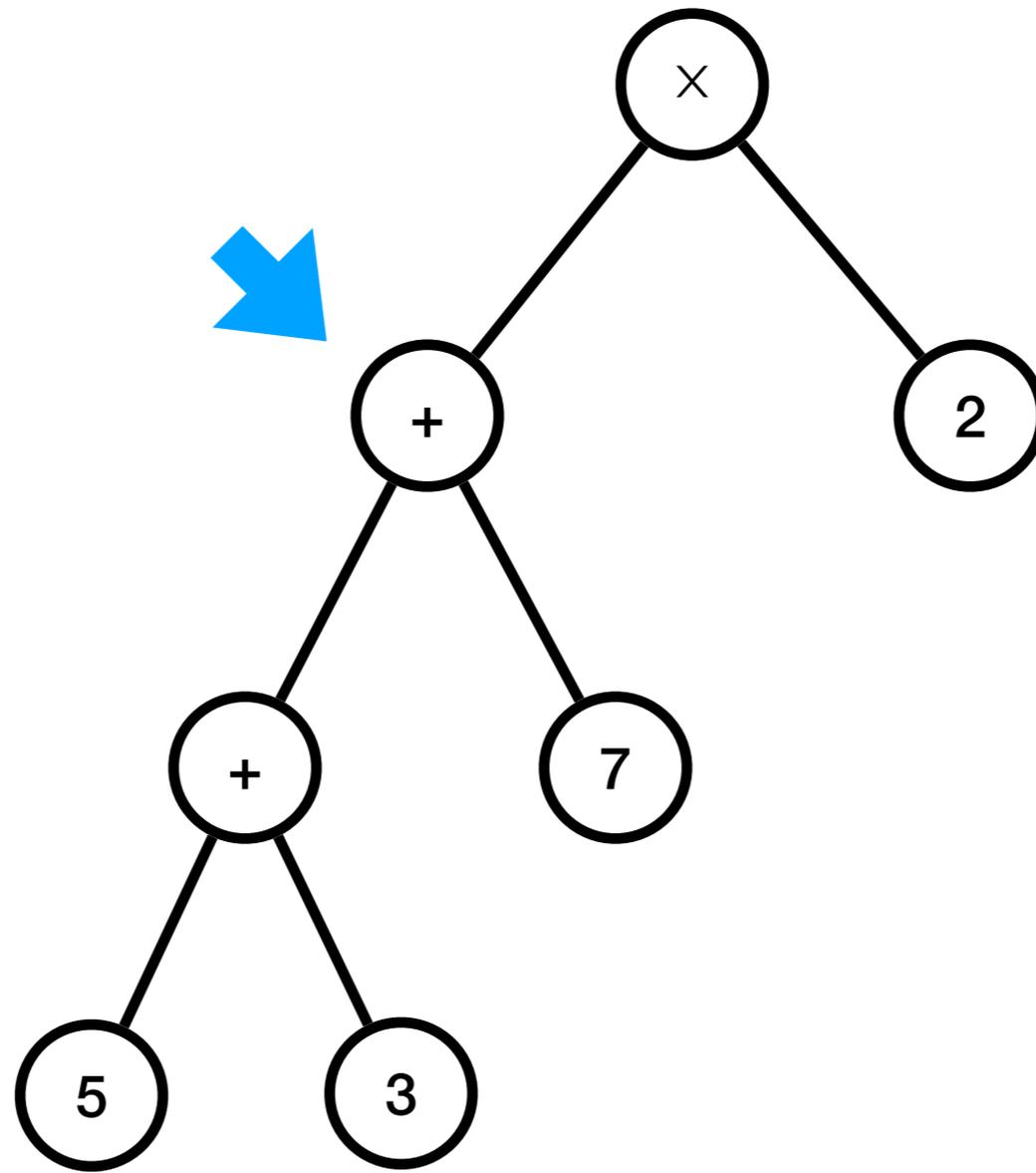
Évaluer $((5 + 3) + 7) \times 2$



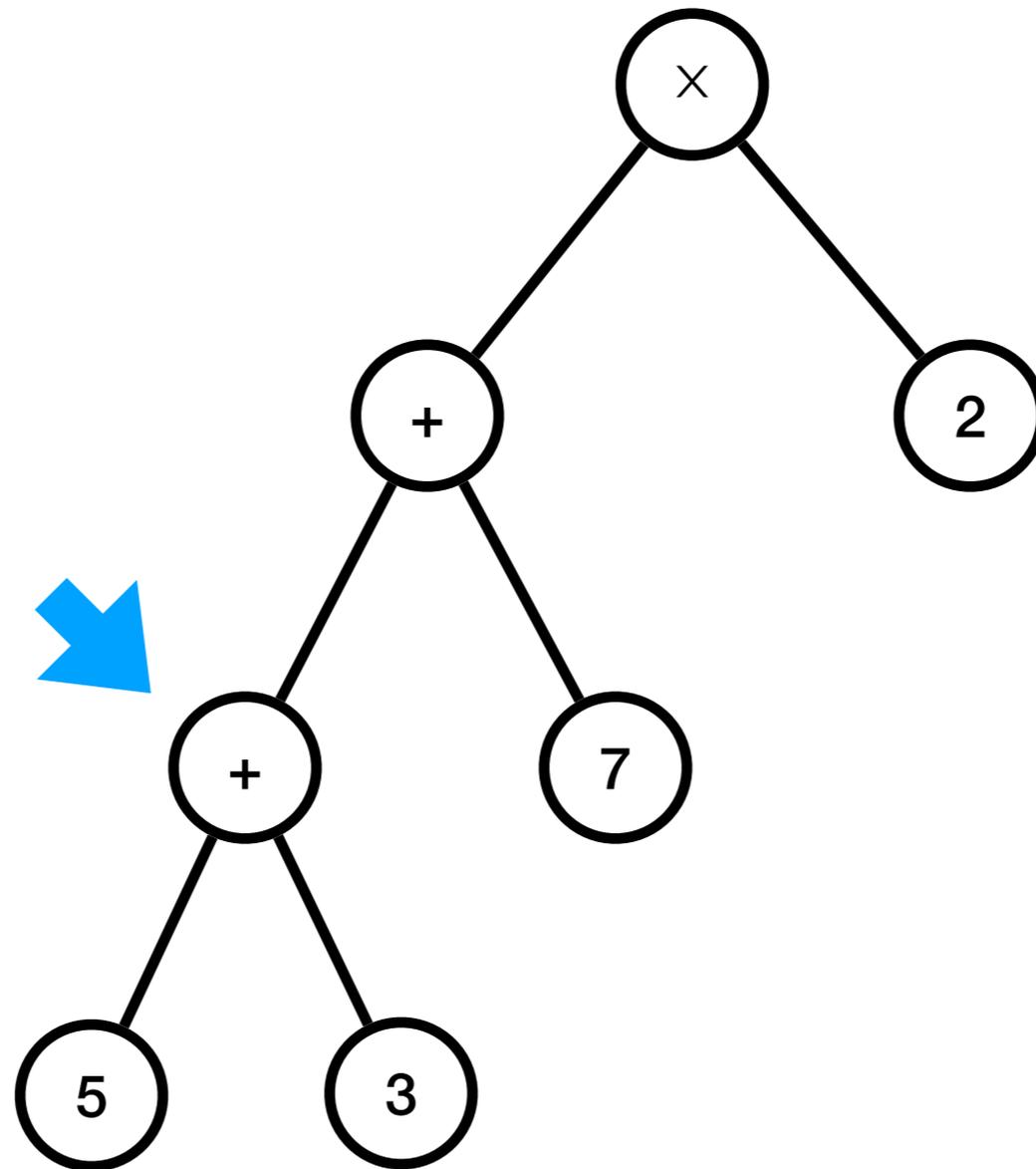
Évaluer $((5 + 3) + 7) \times 2$



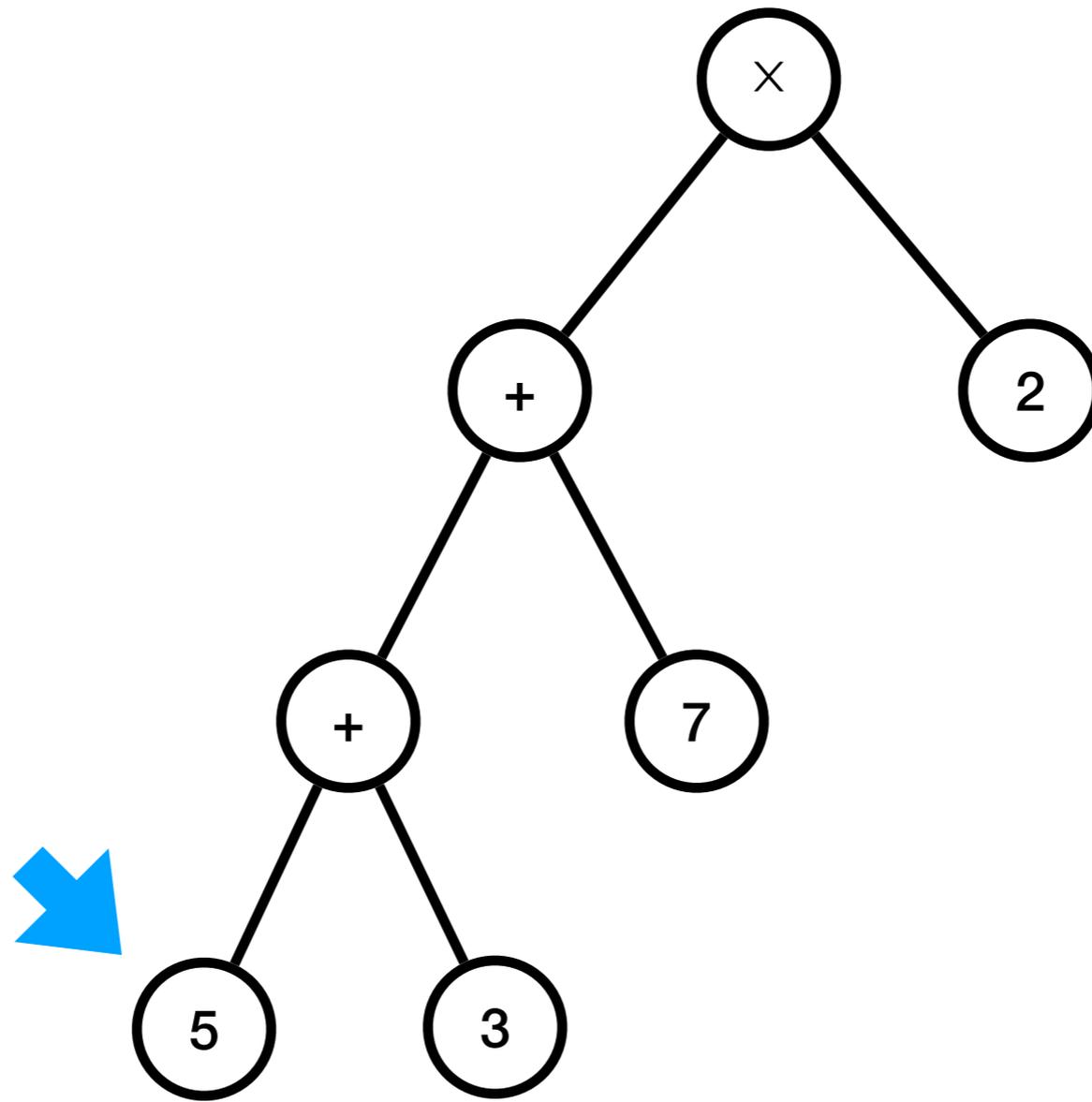
Évaluer $((5 + 3) + 7) \times 2$



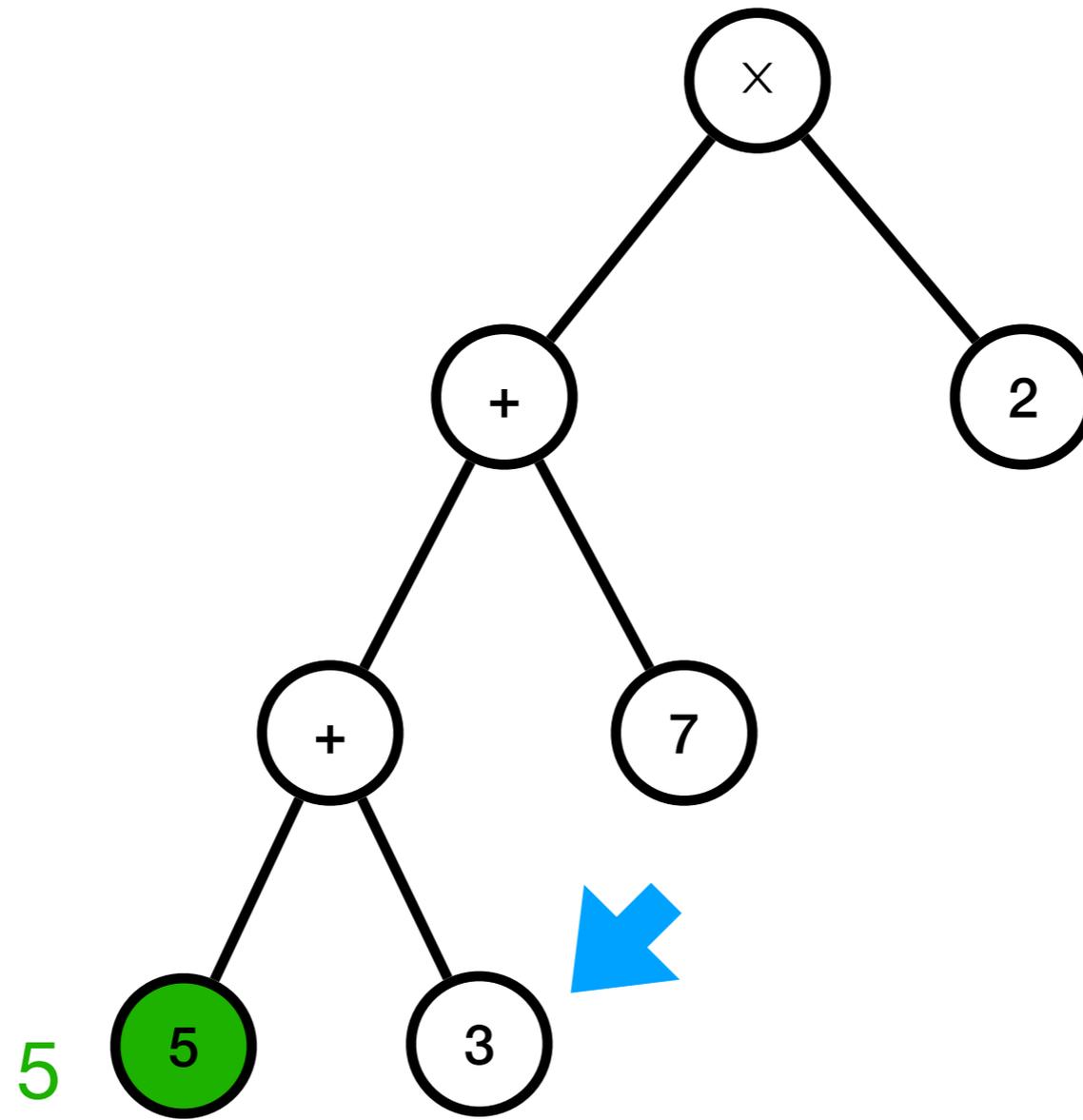
Évaluer $((5 + 3) + 7) \times 2$



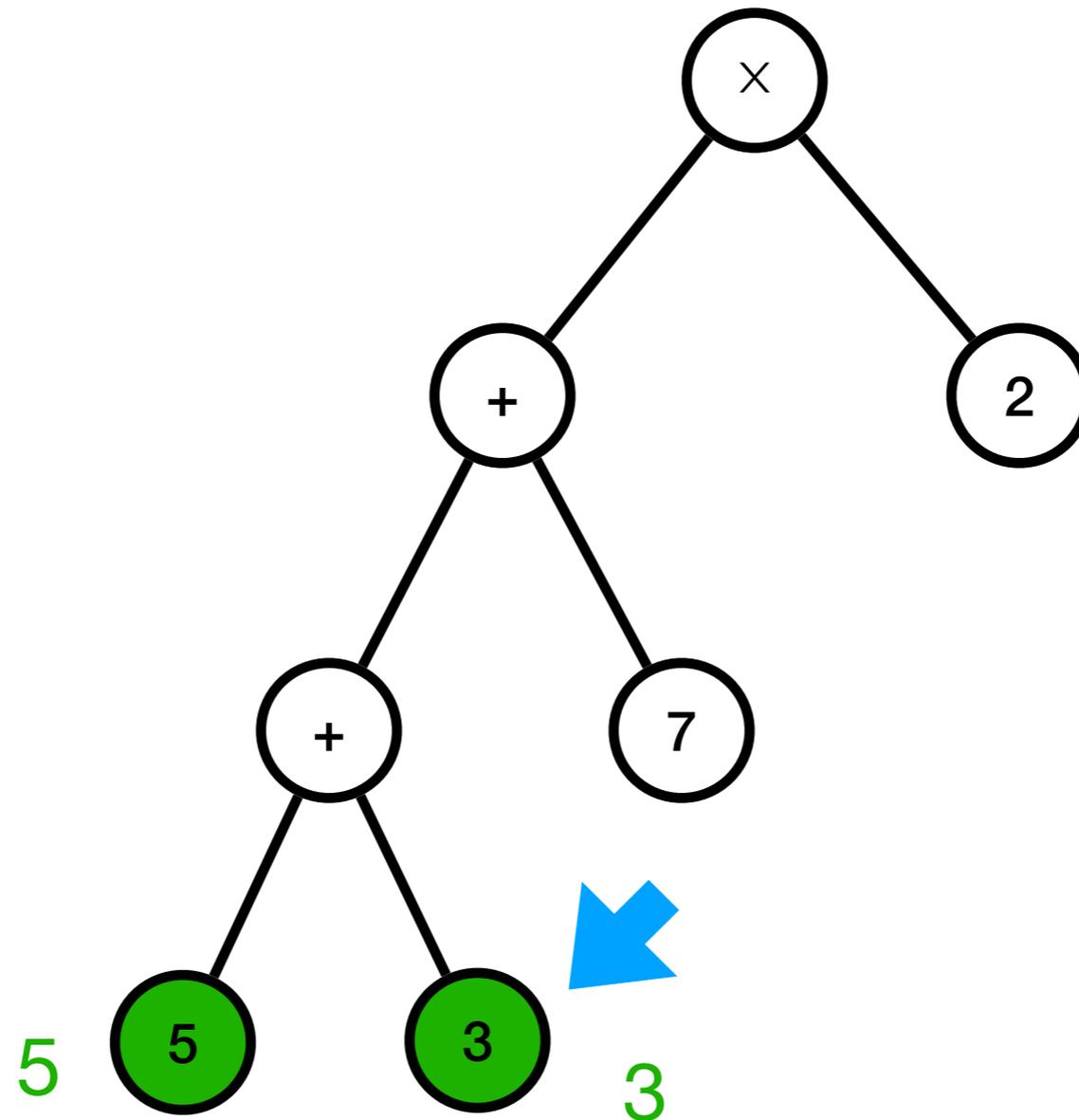
Évaluer $((5 + 3) + 7) \times 2$



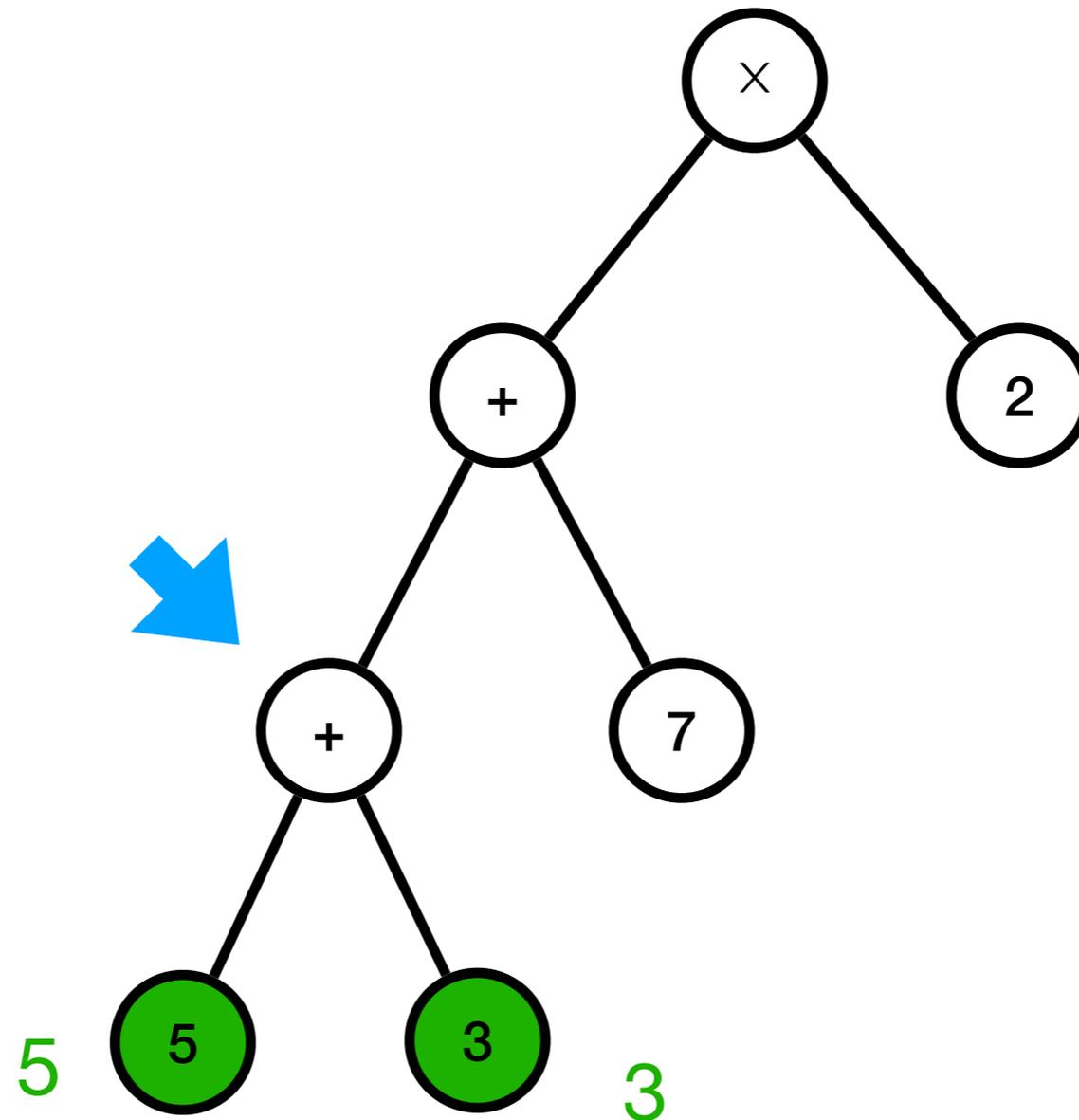
Évaluer $((5 + 3) + 7) \times 2$



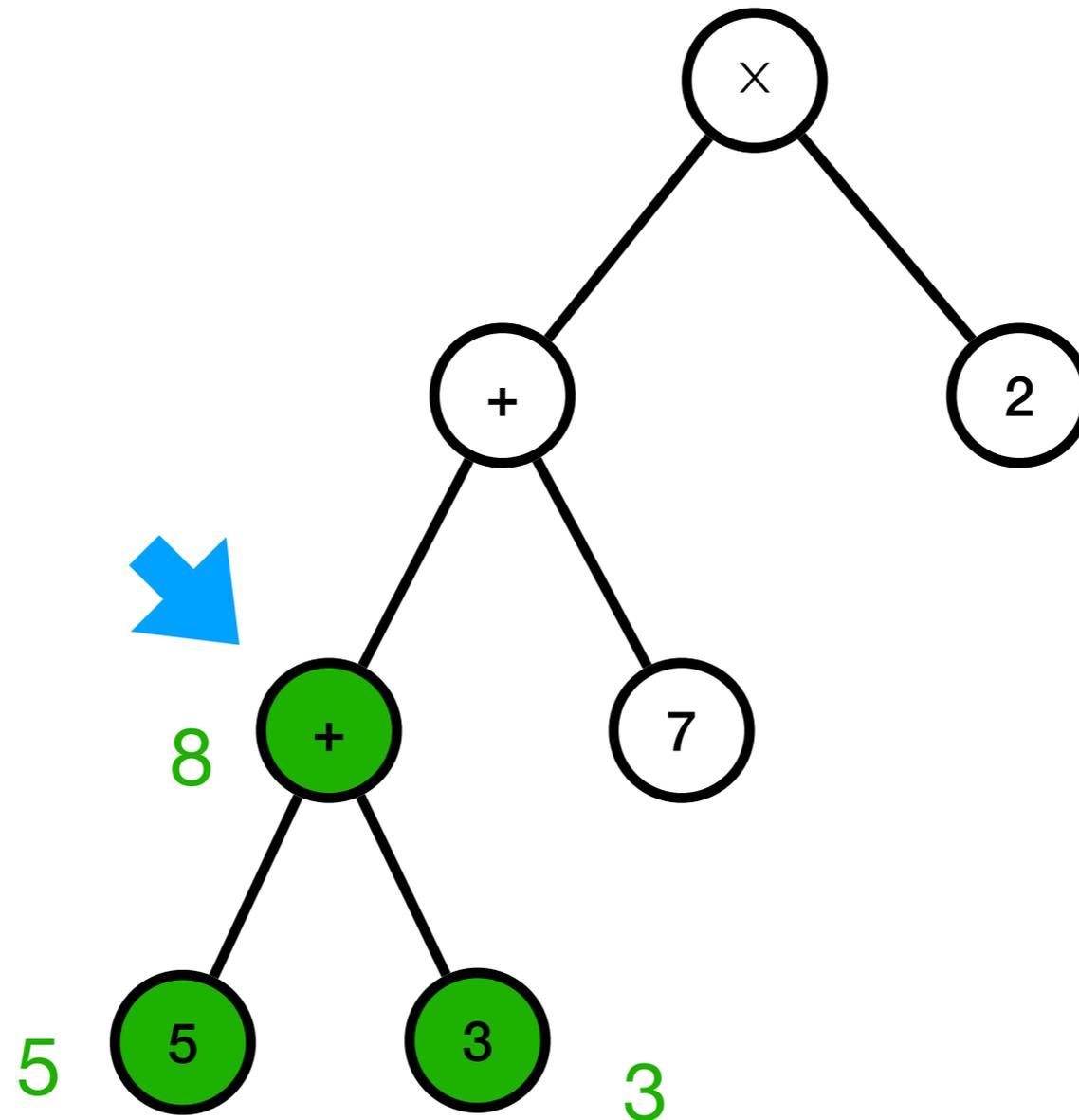
Évaluer $((5 + 3) + 7) \times 2$



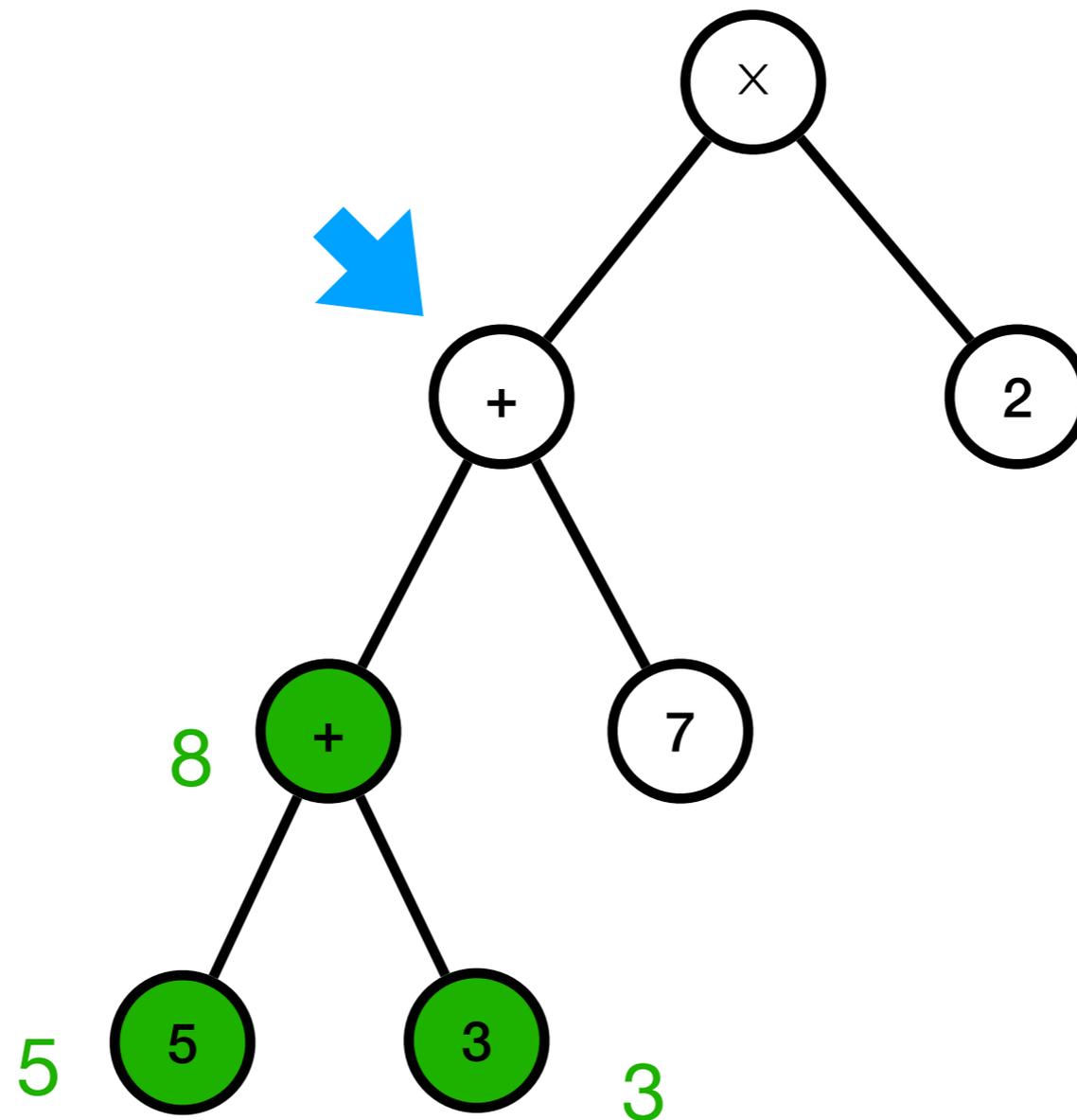
Évaluer $((5 + 3) + 7) \times 2$



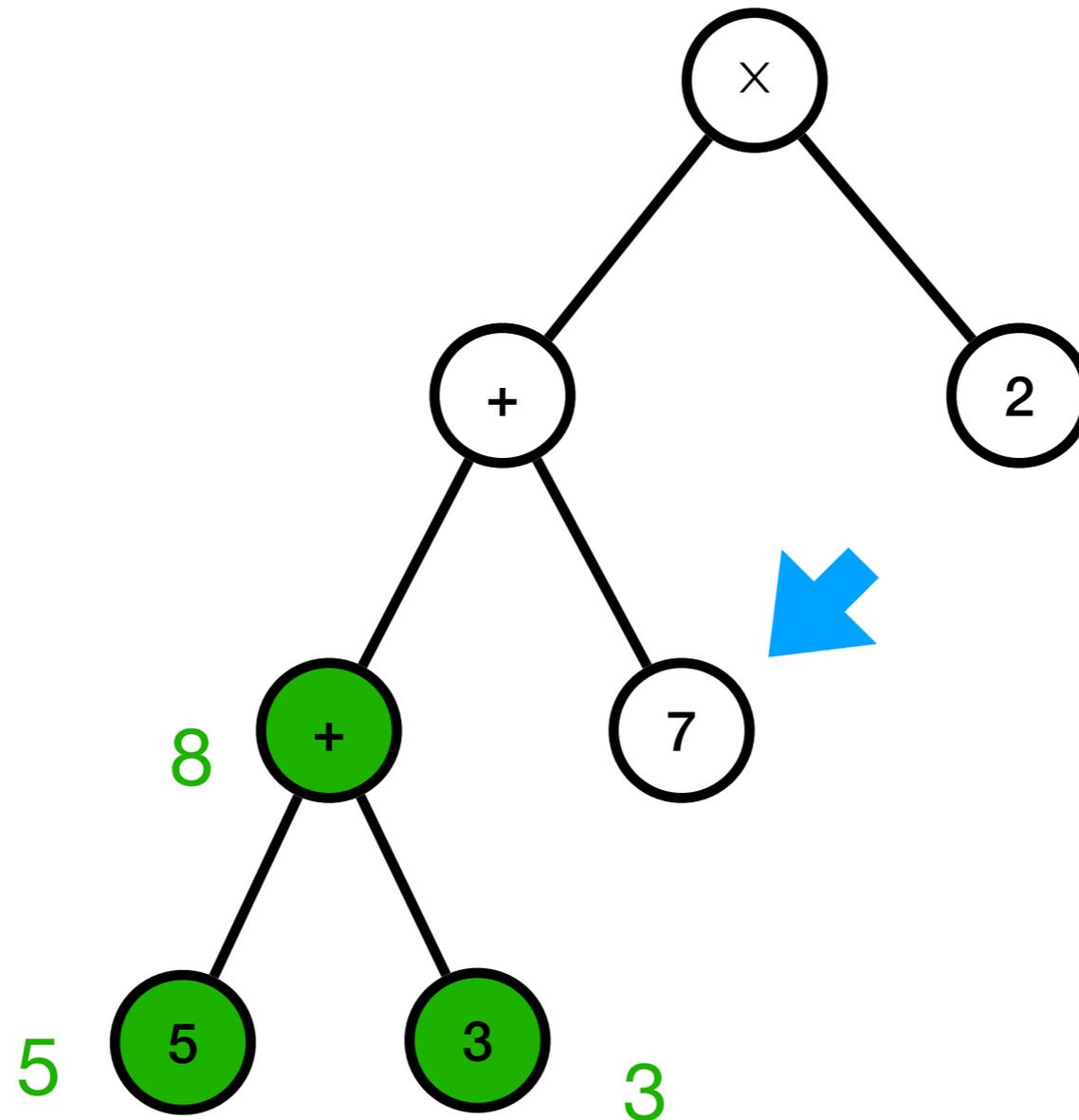
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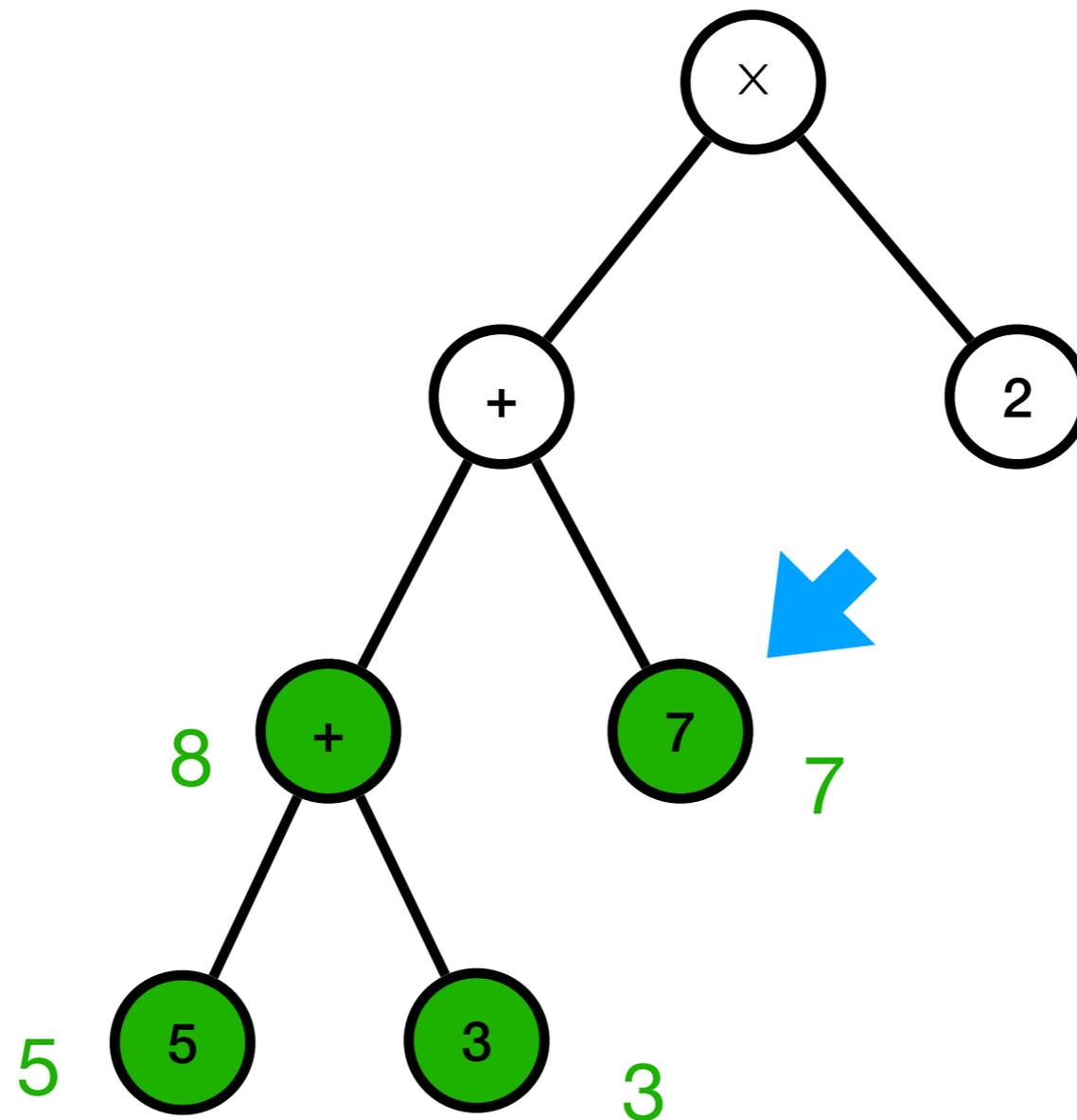
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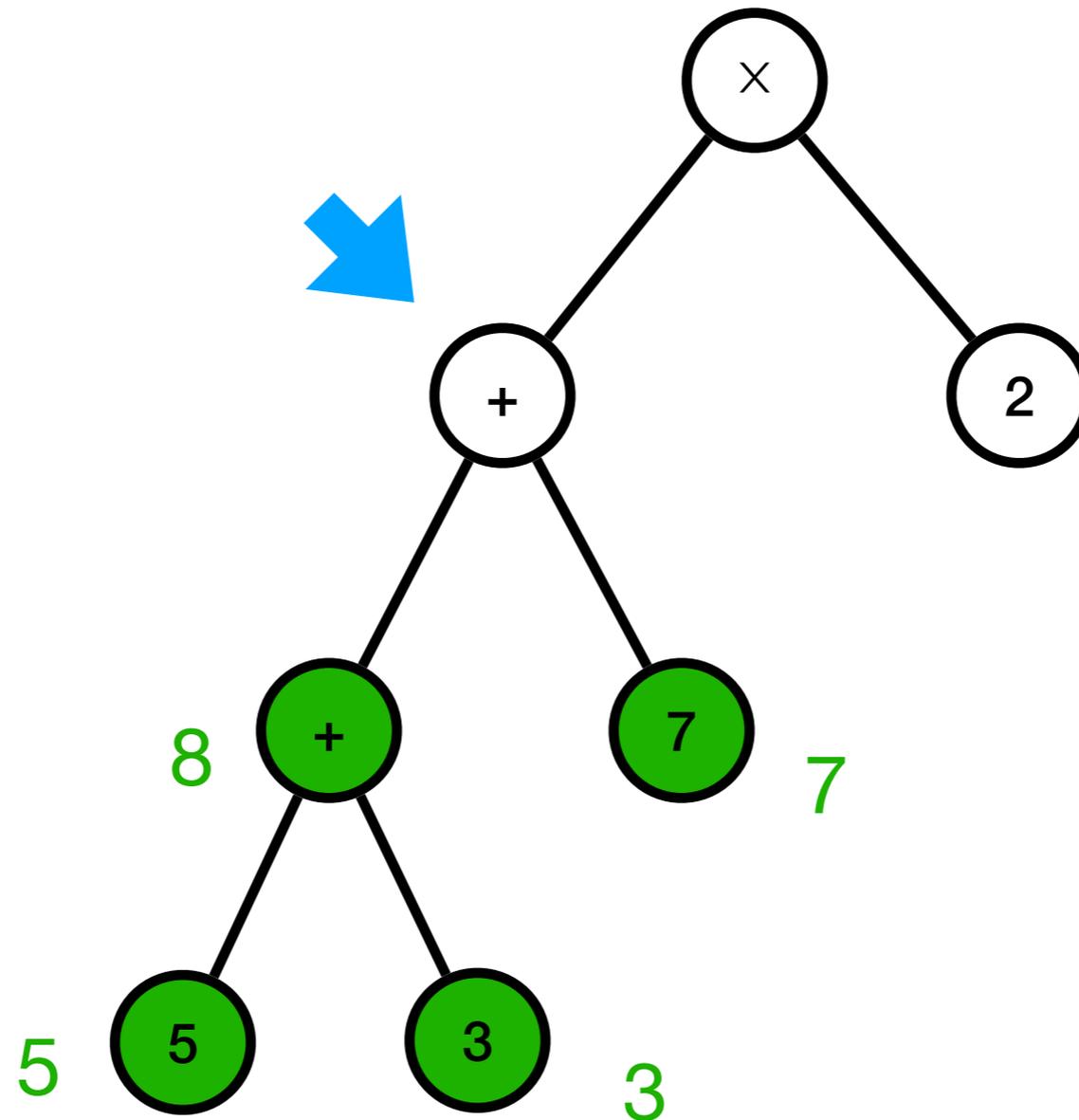
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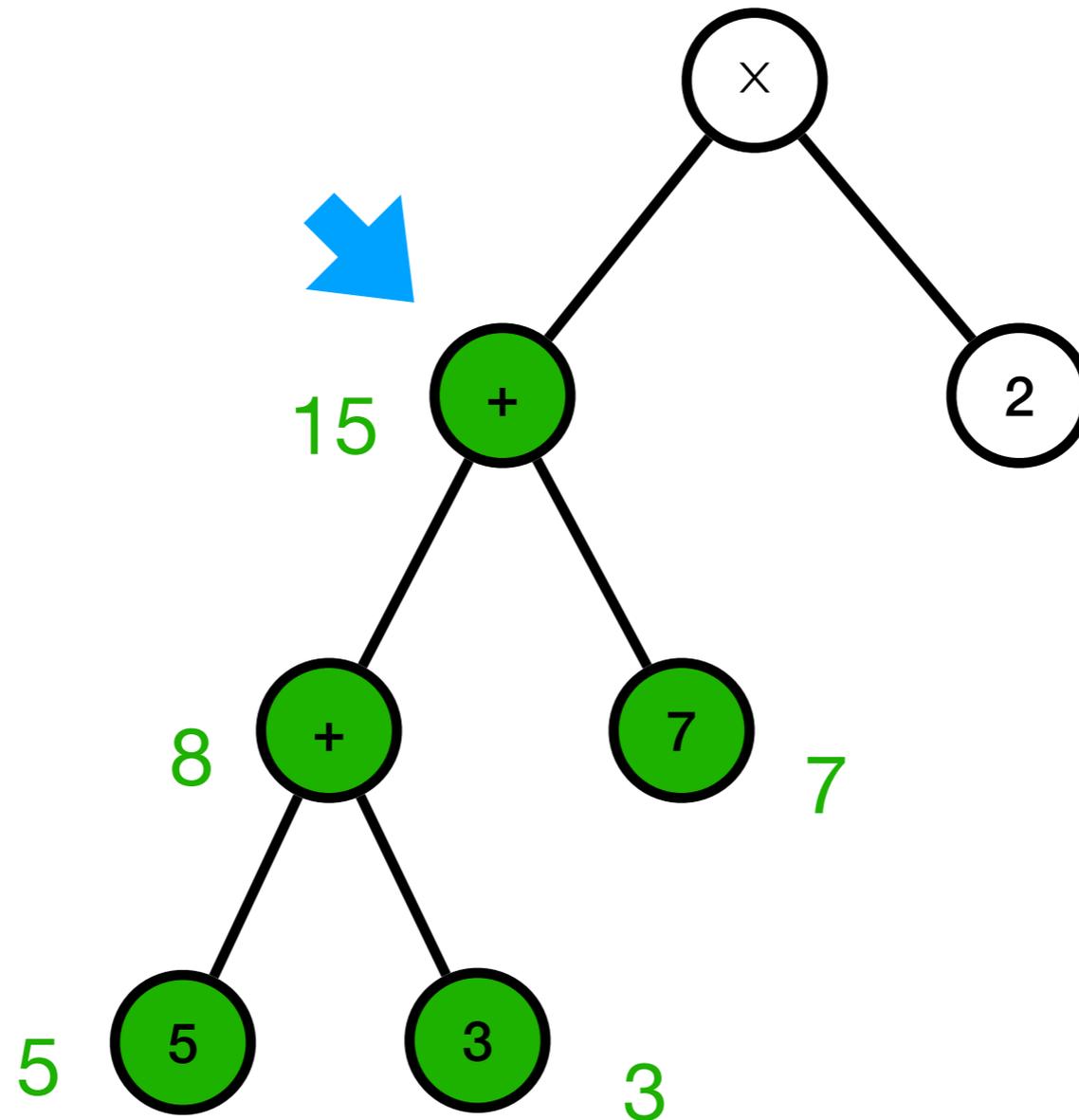
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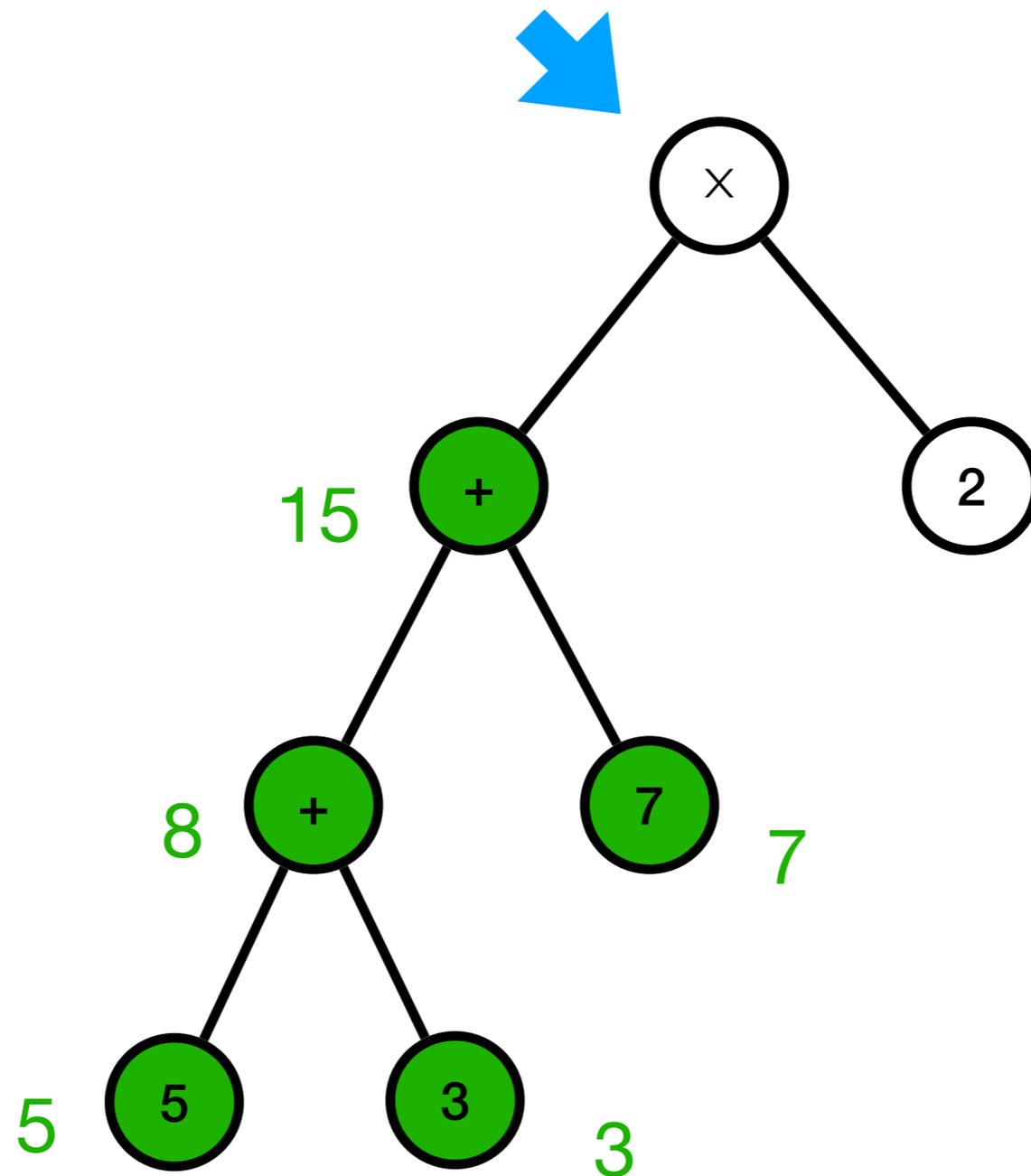
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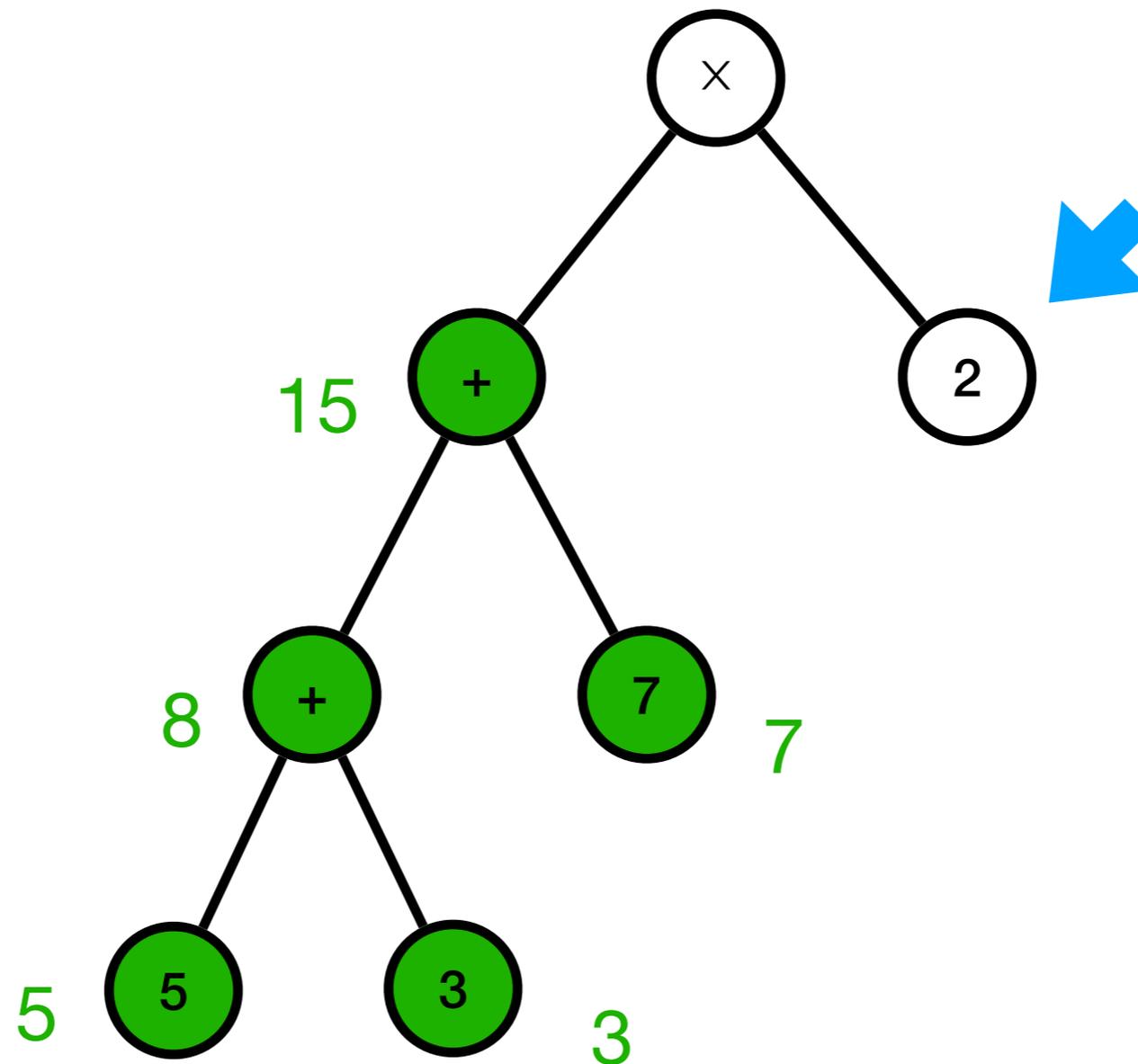
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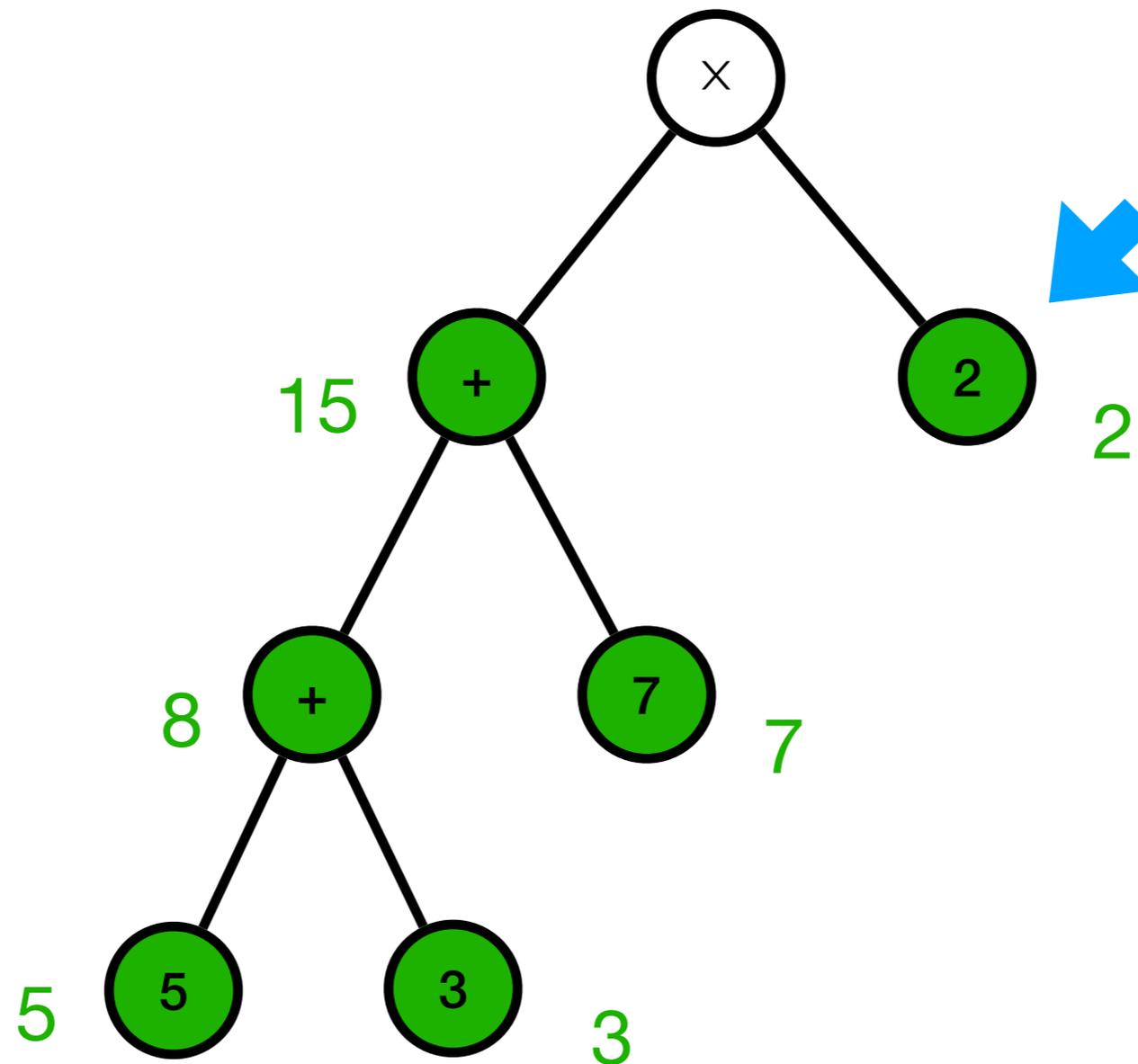
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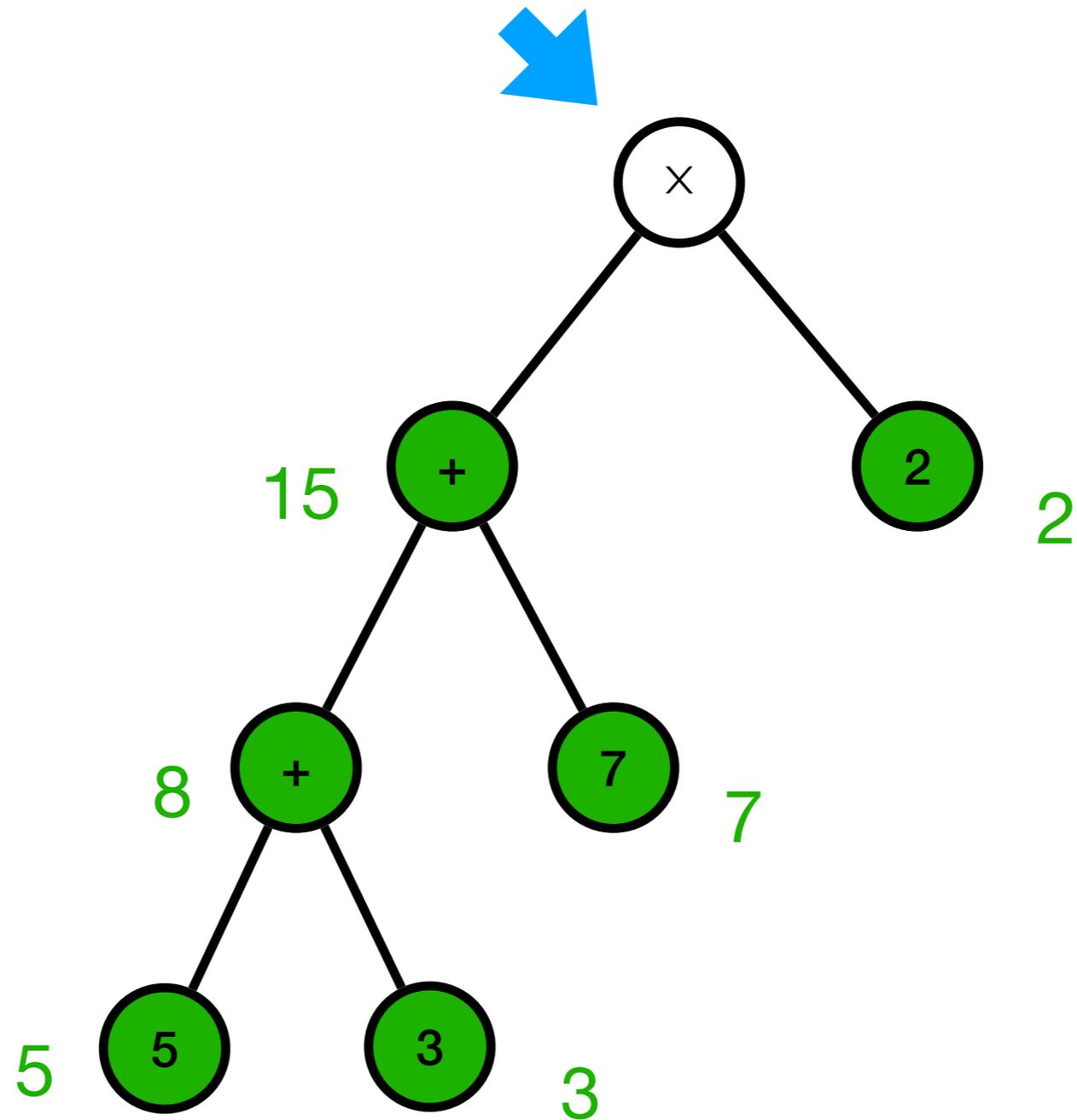
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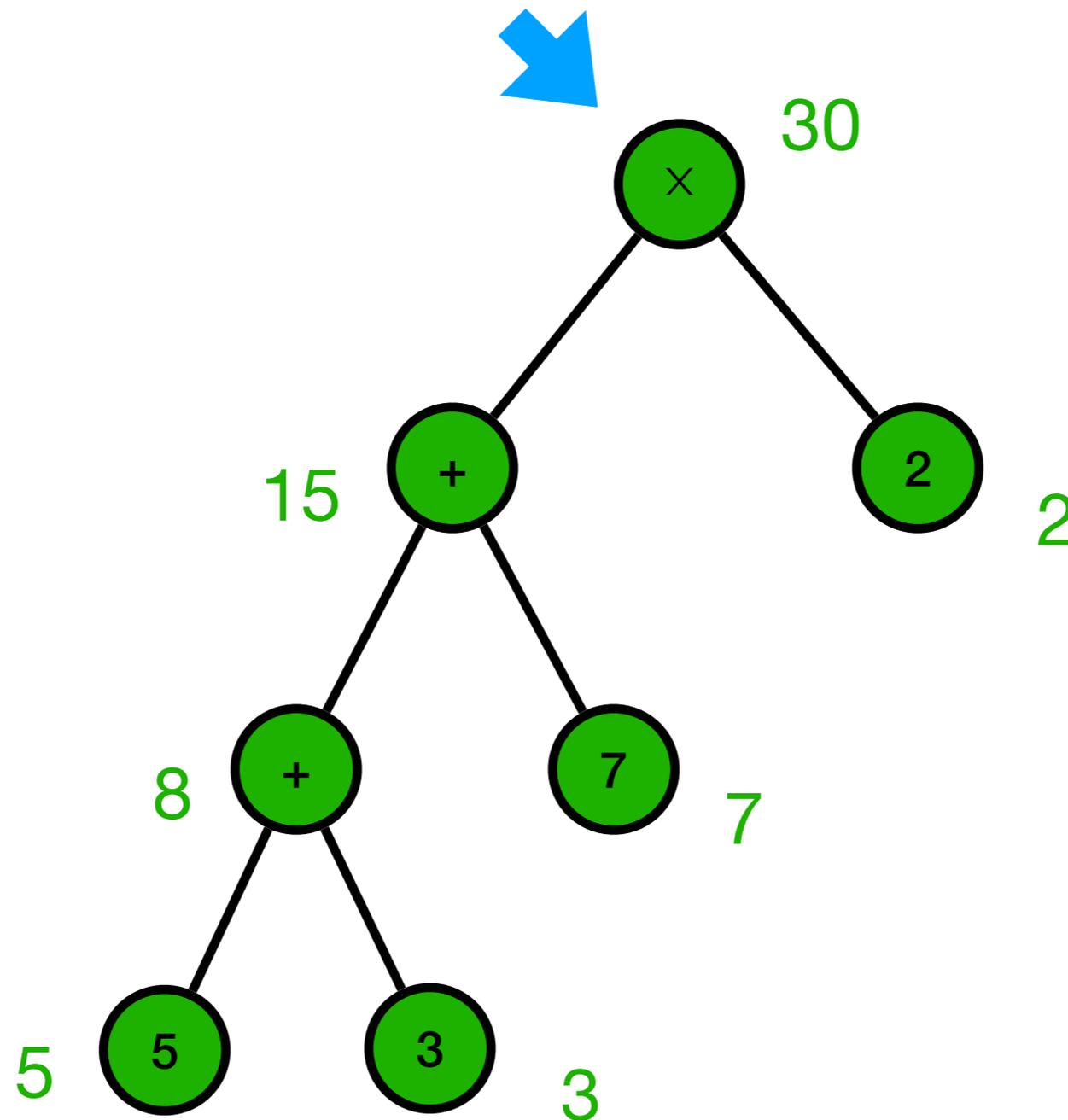
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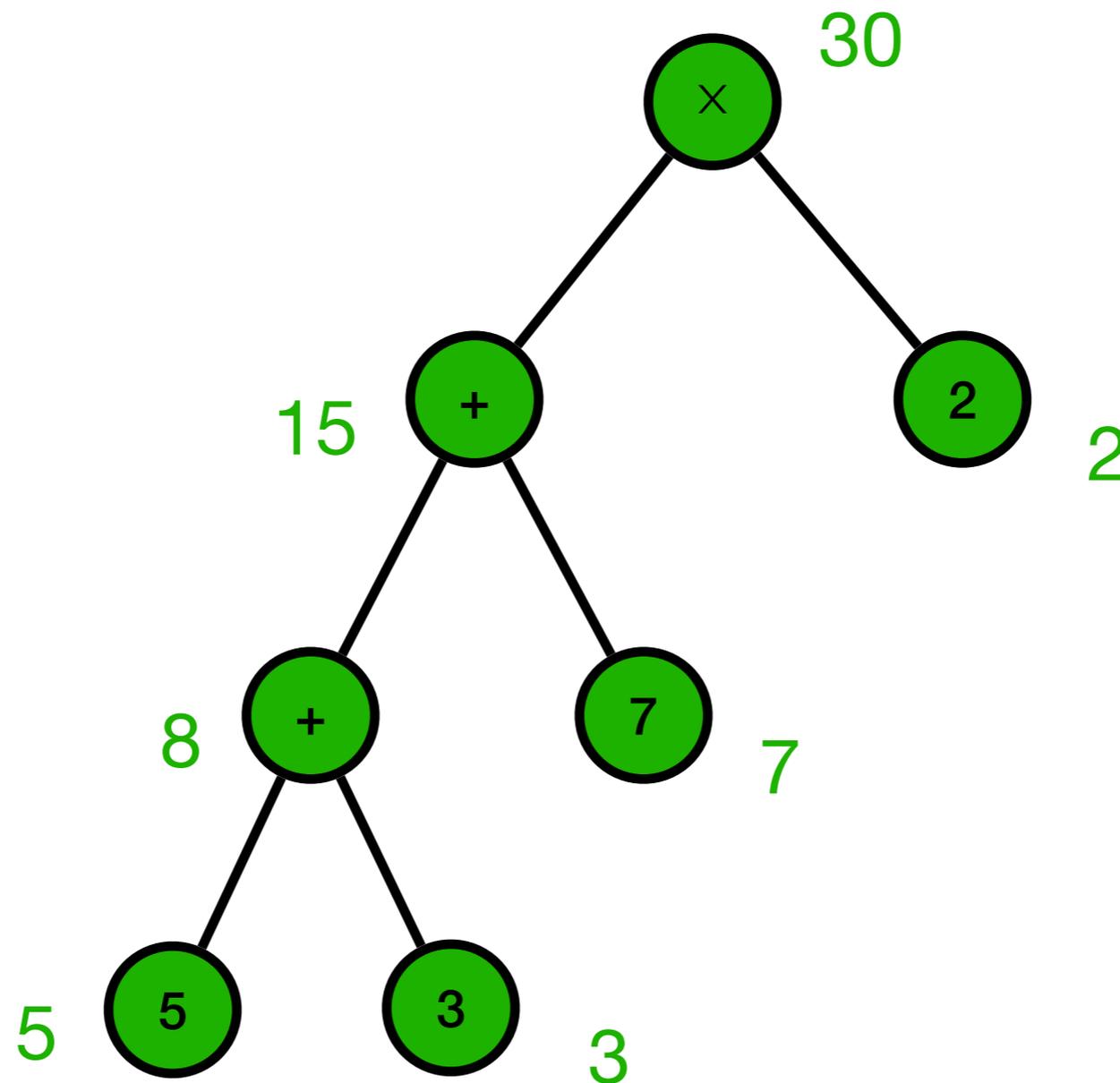
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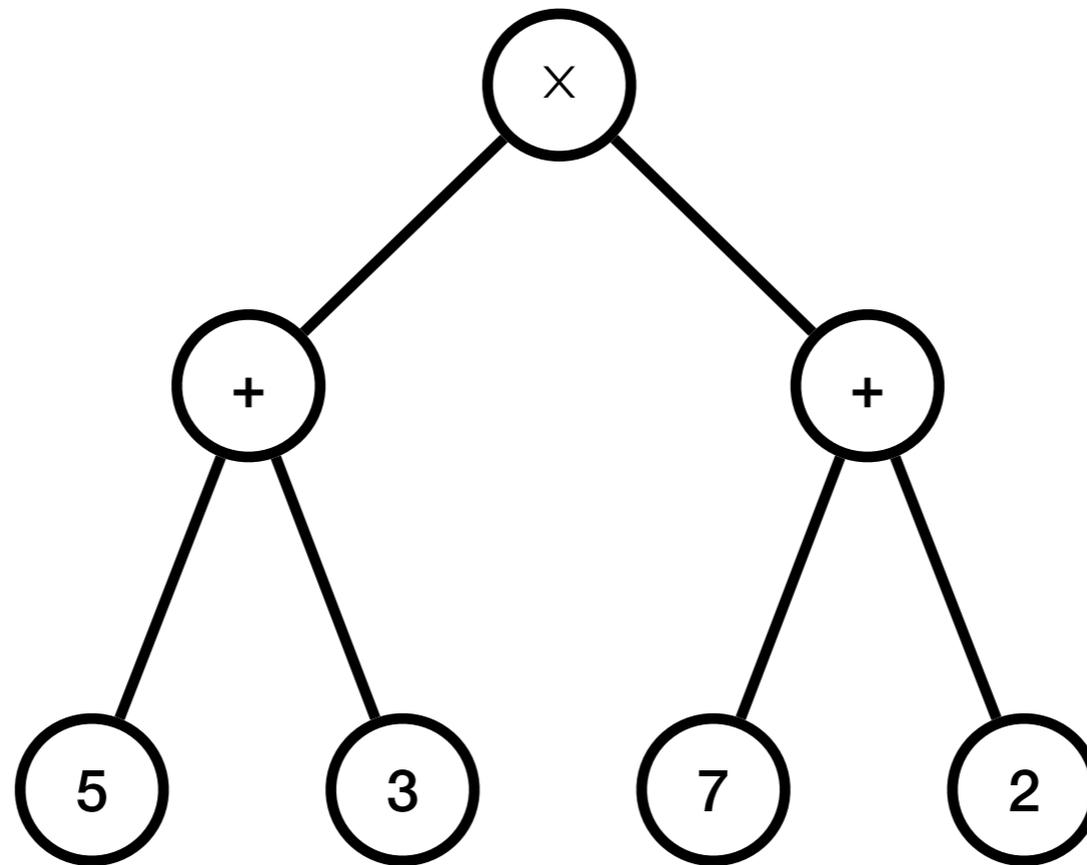
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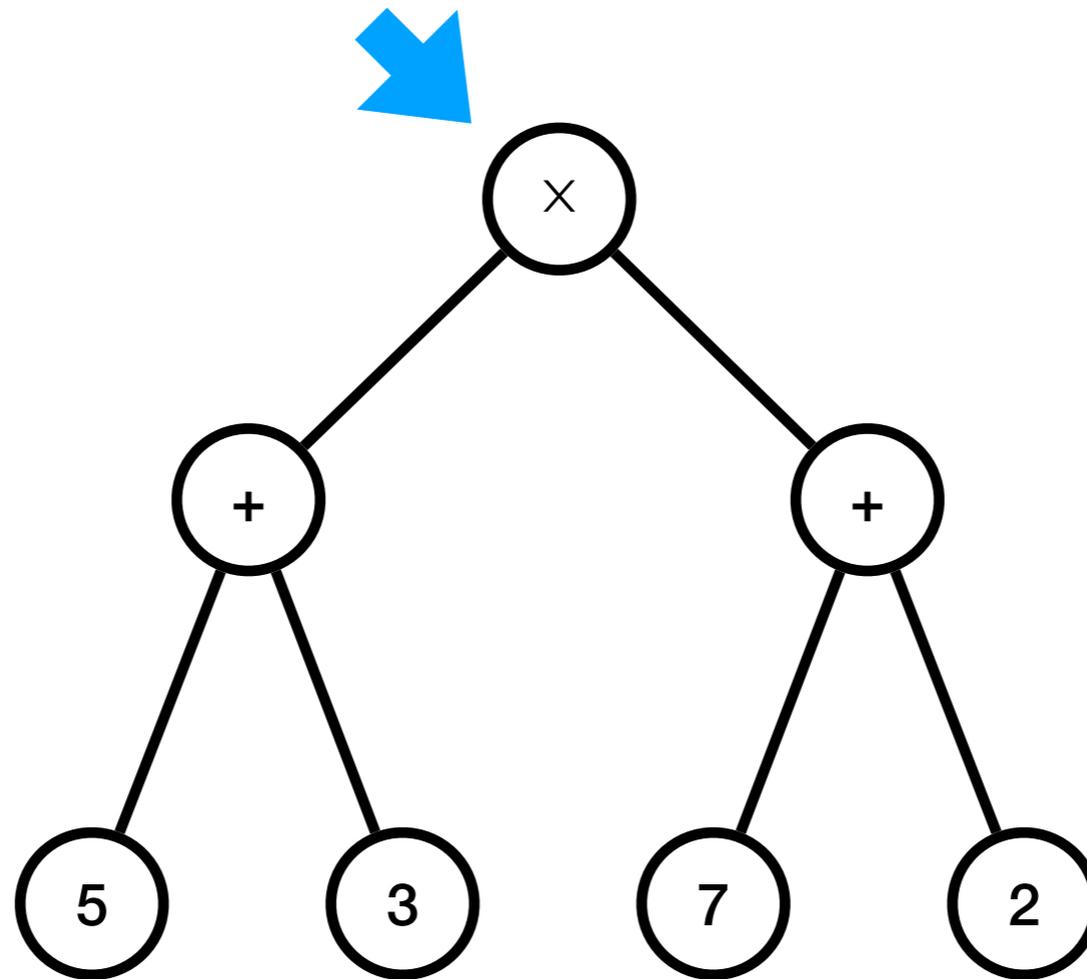
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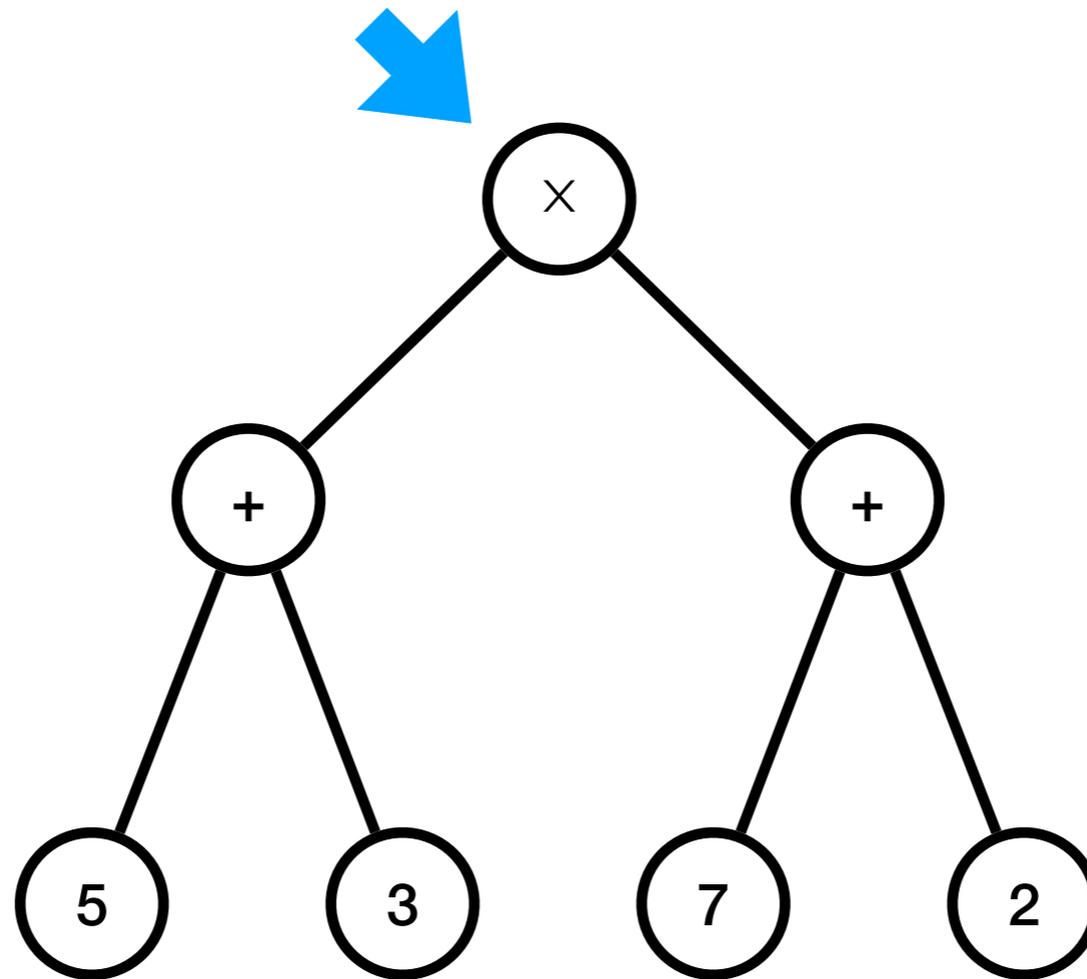
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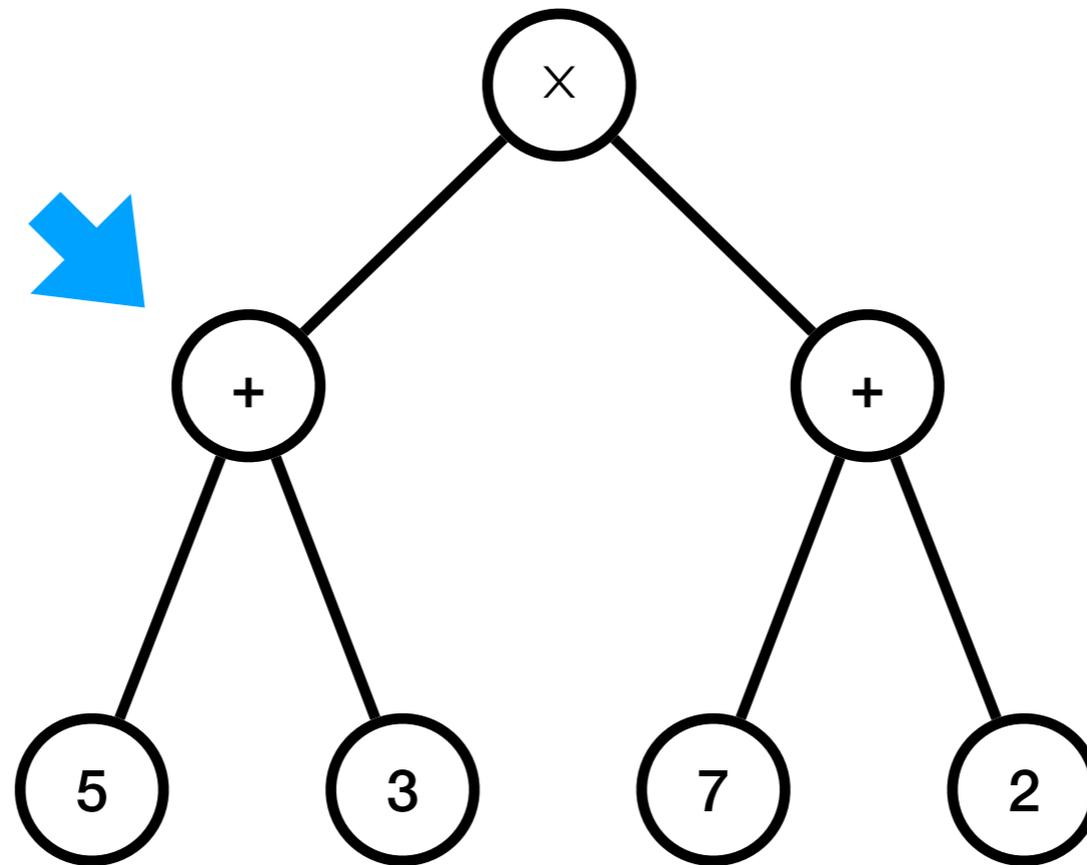


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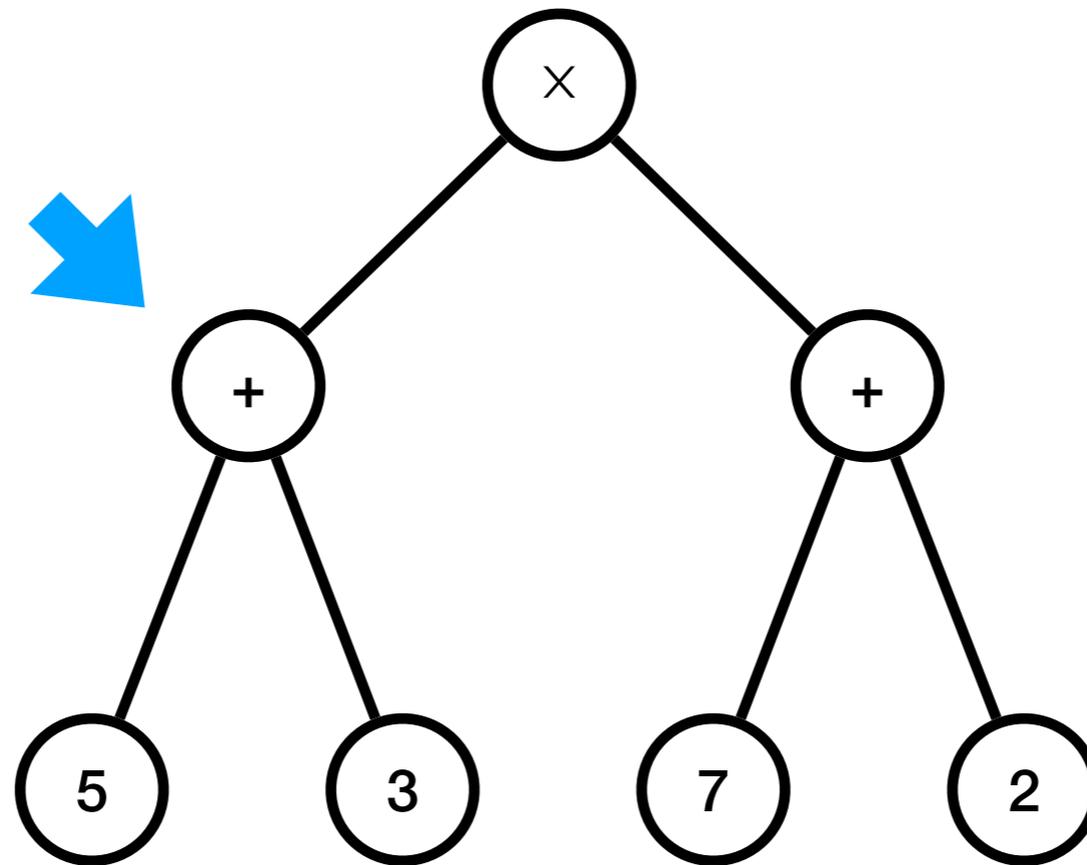
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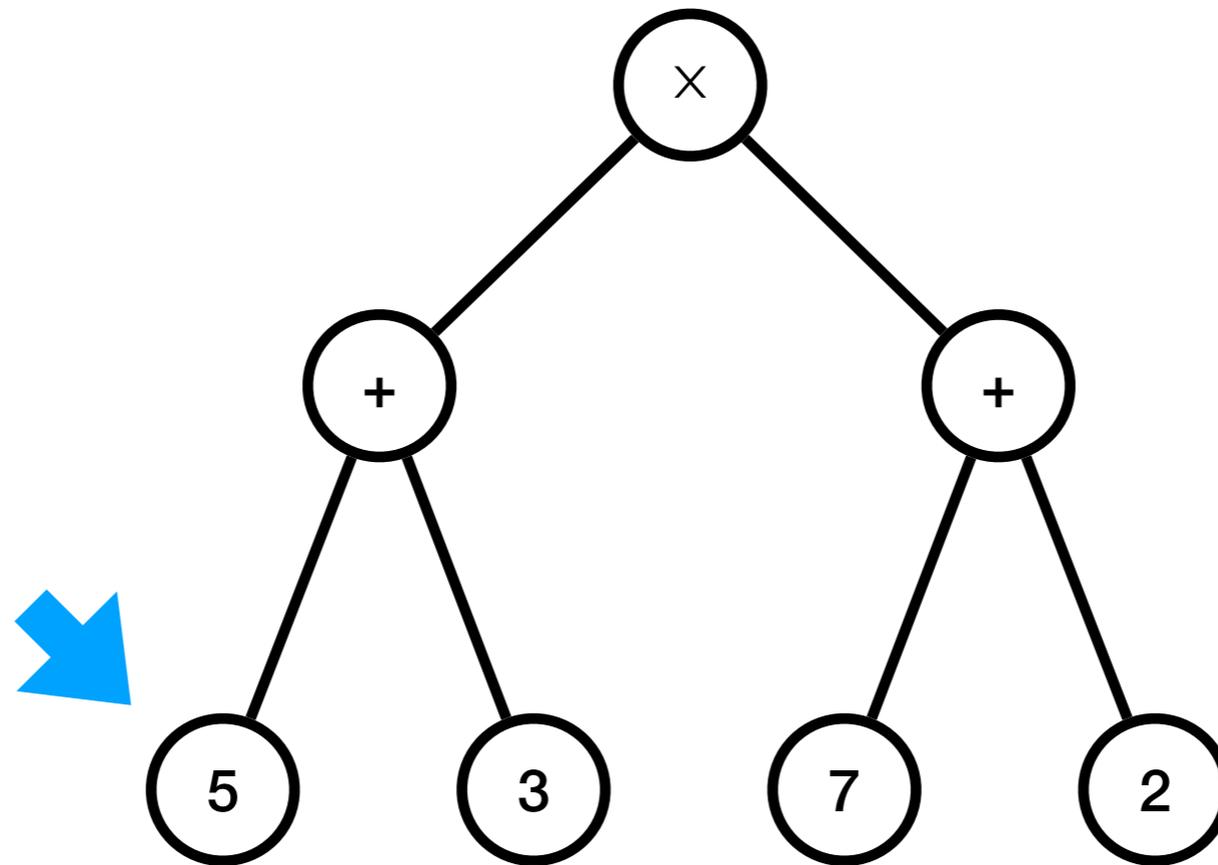
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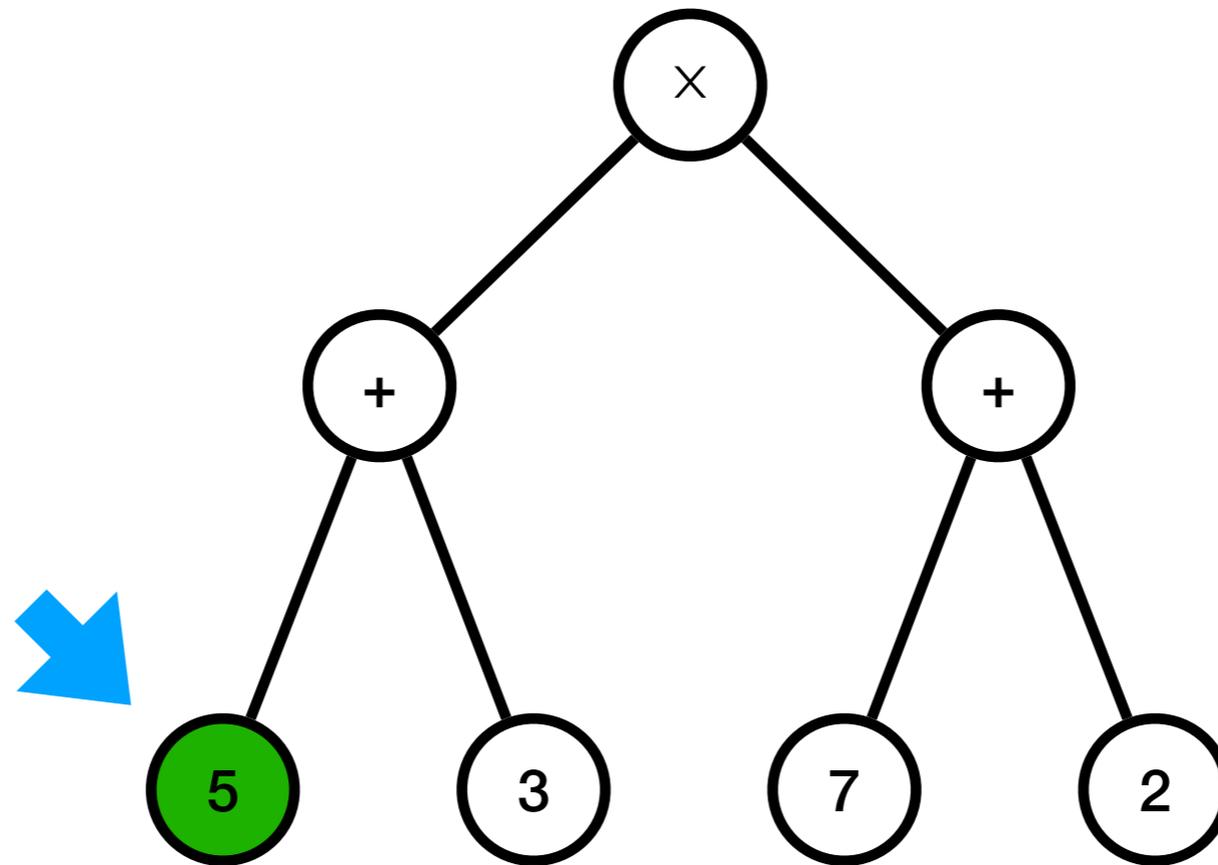
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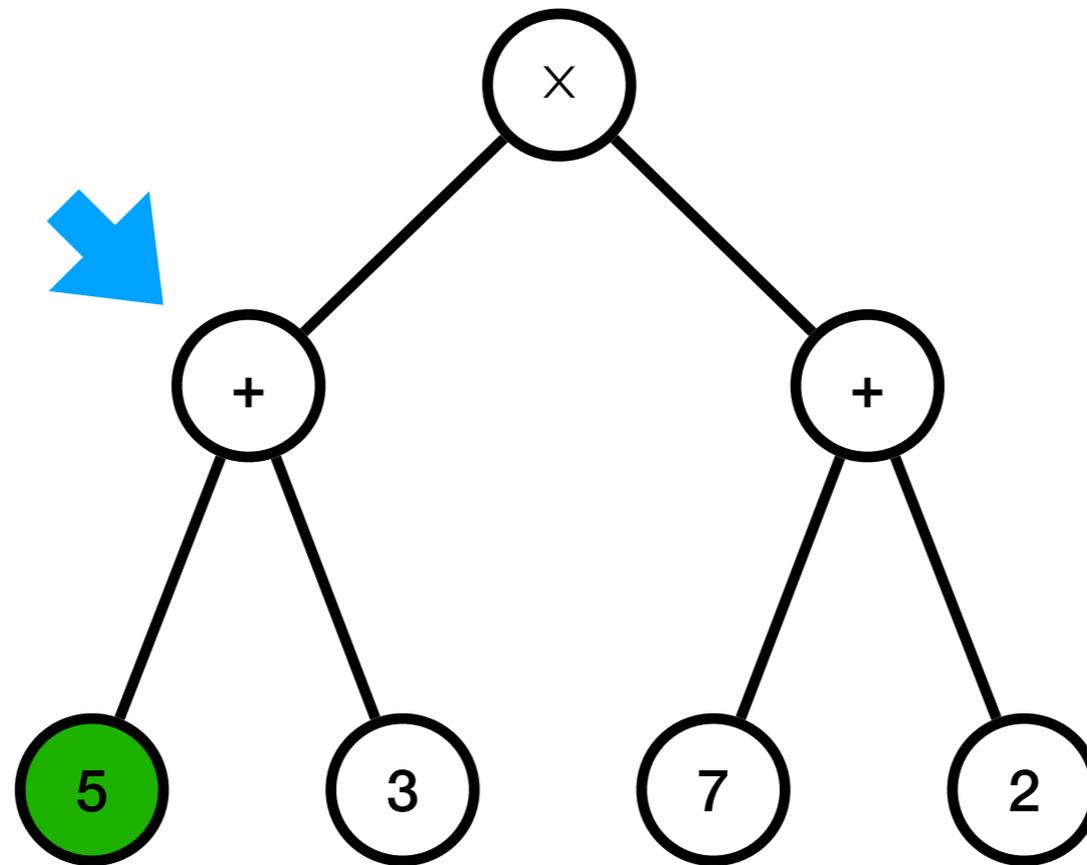
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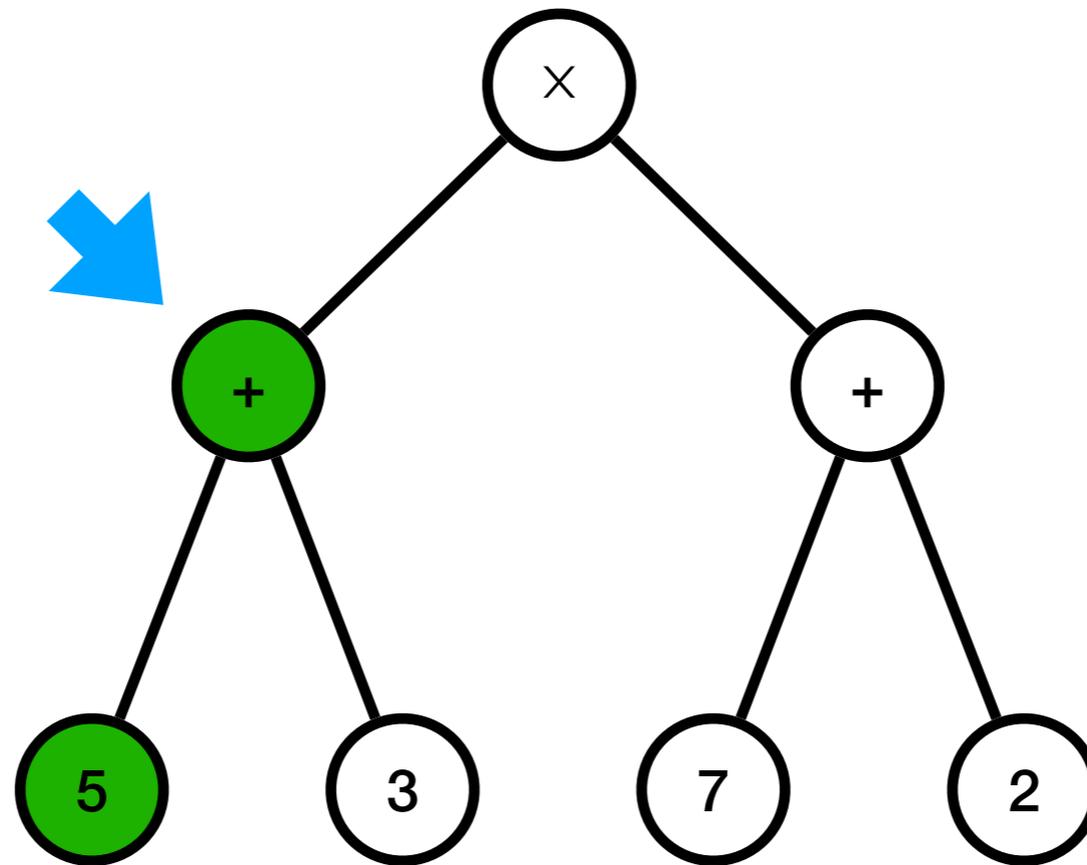
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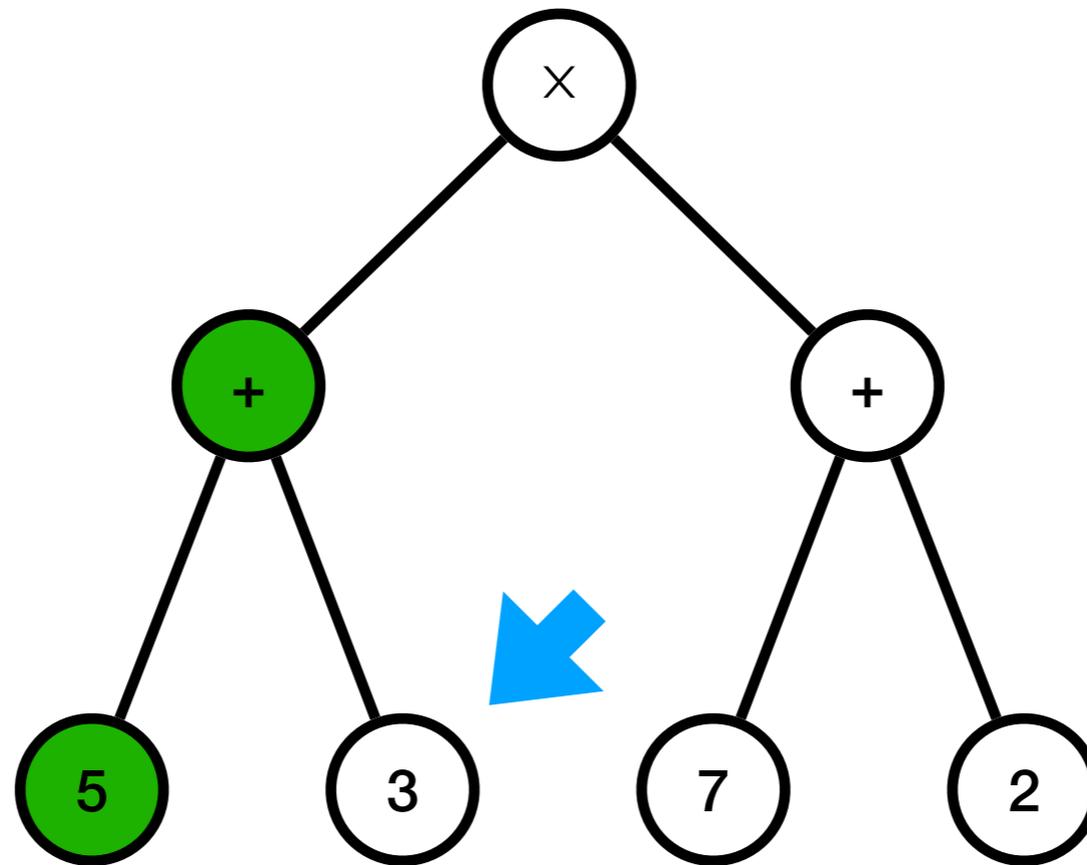
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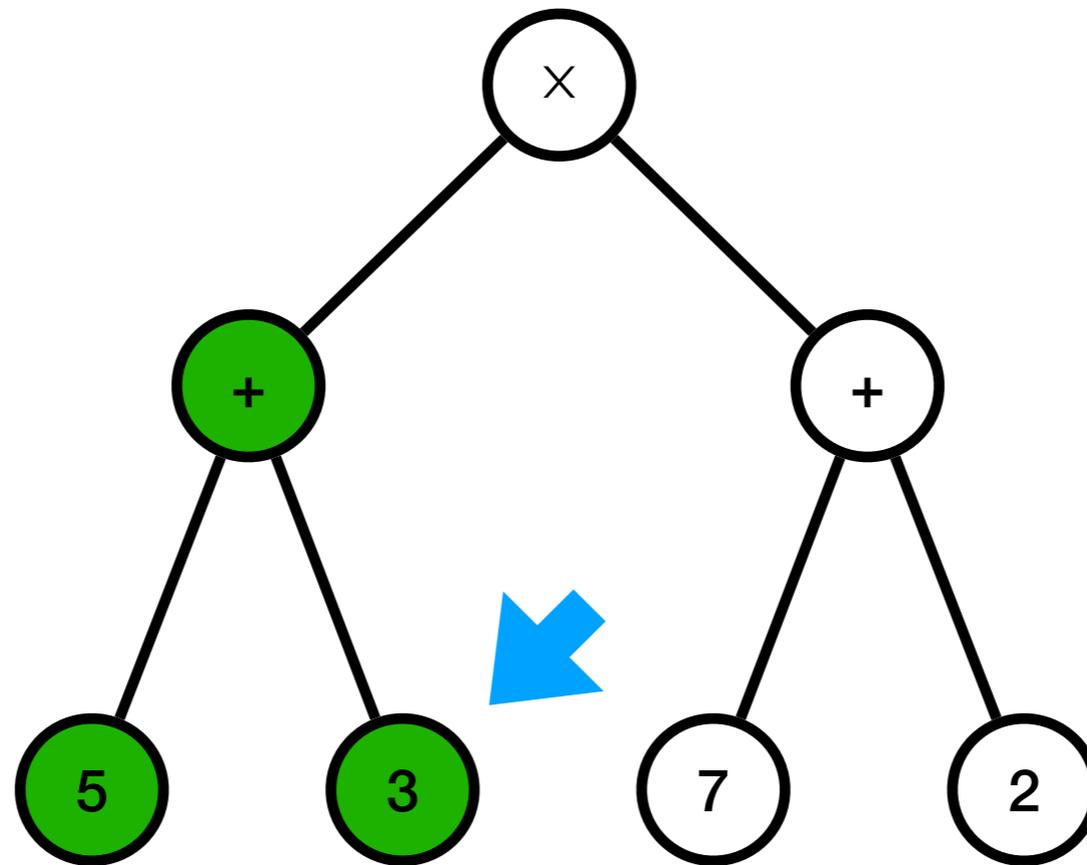
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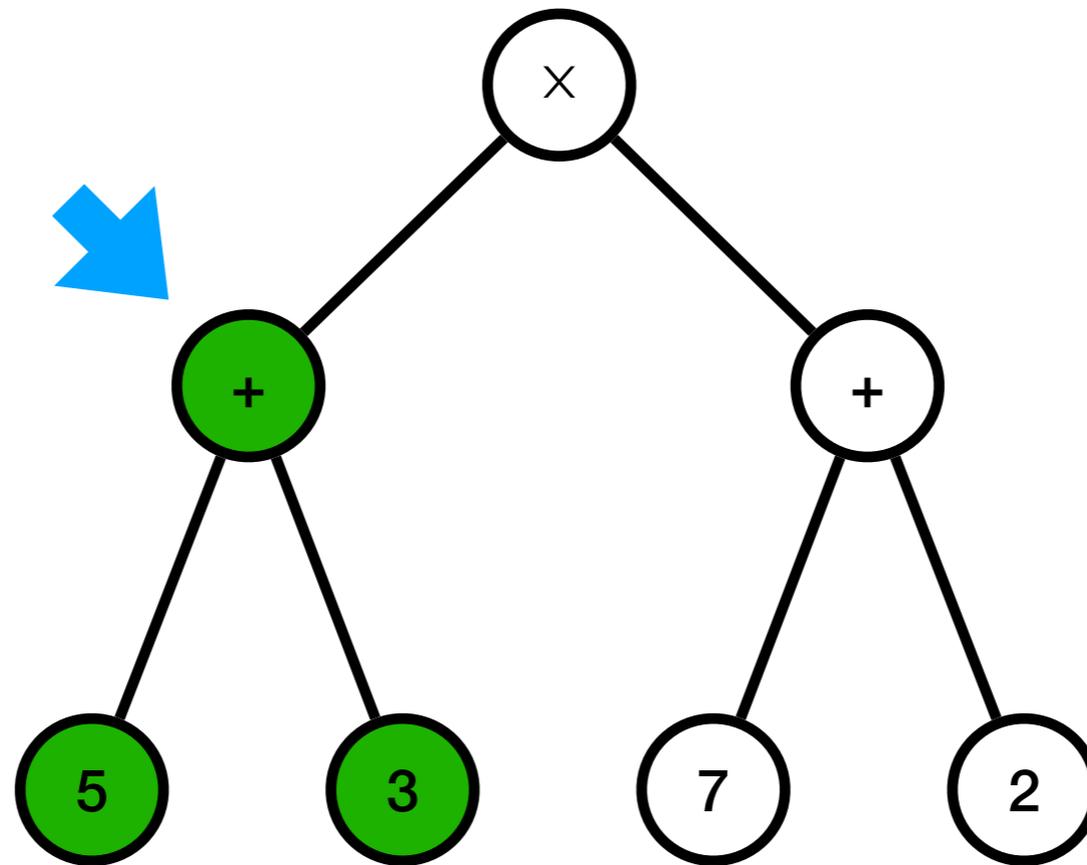
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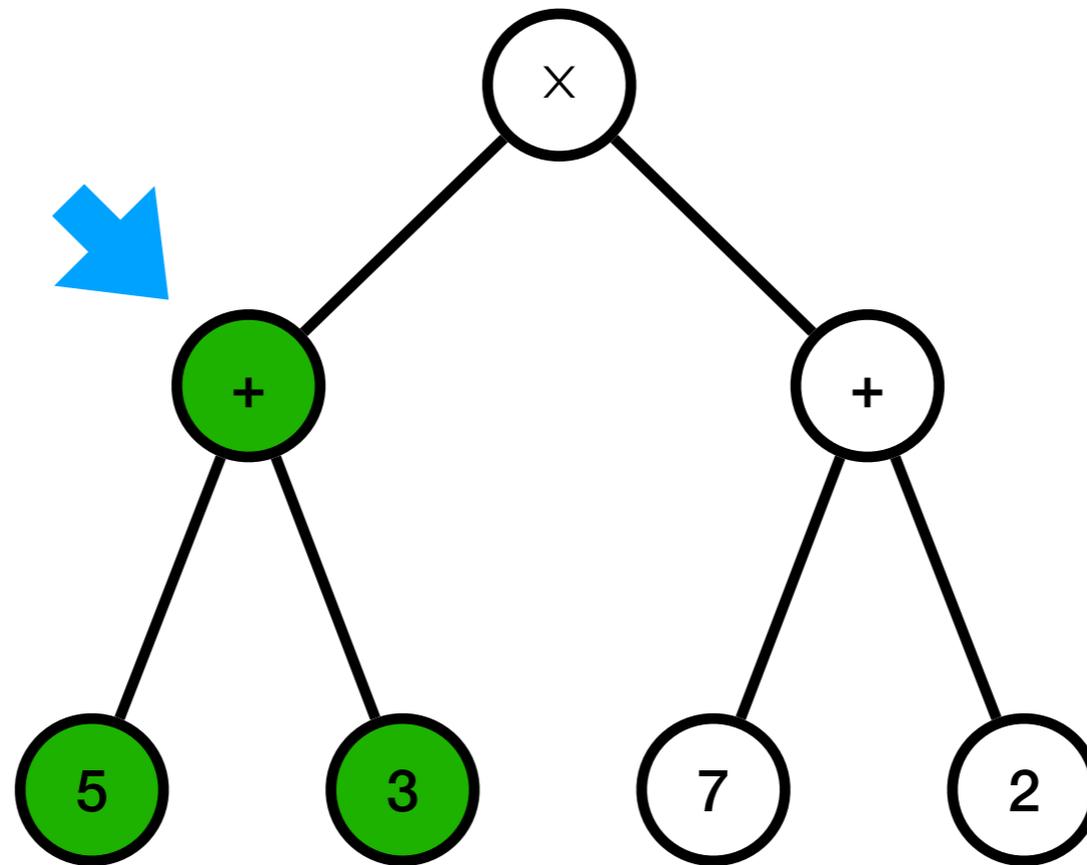
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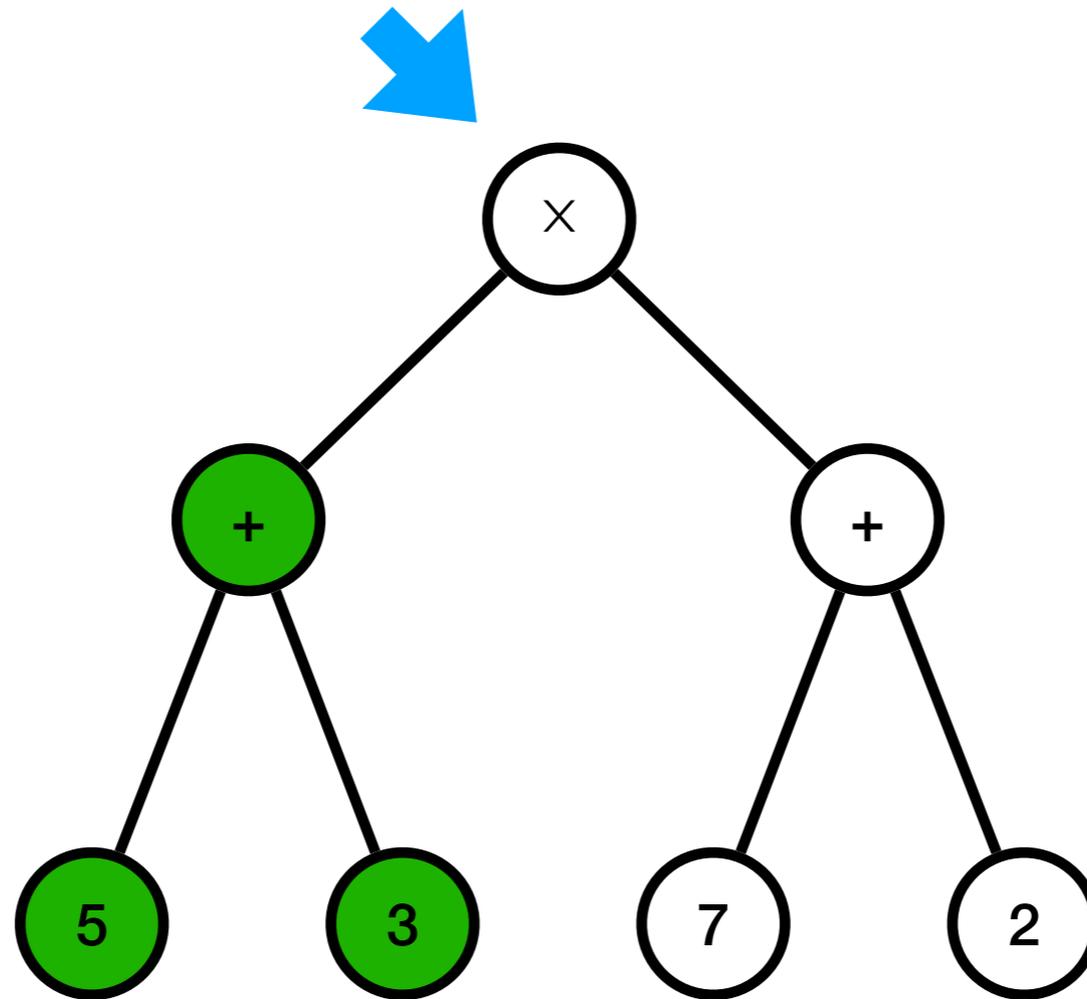
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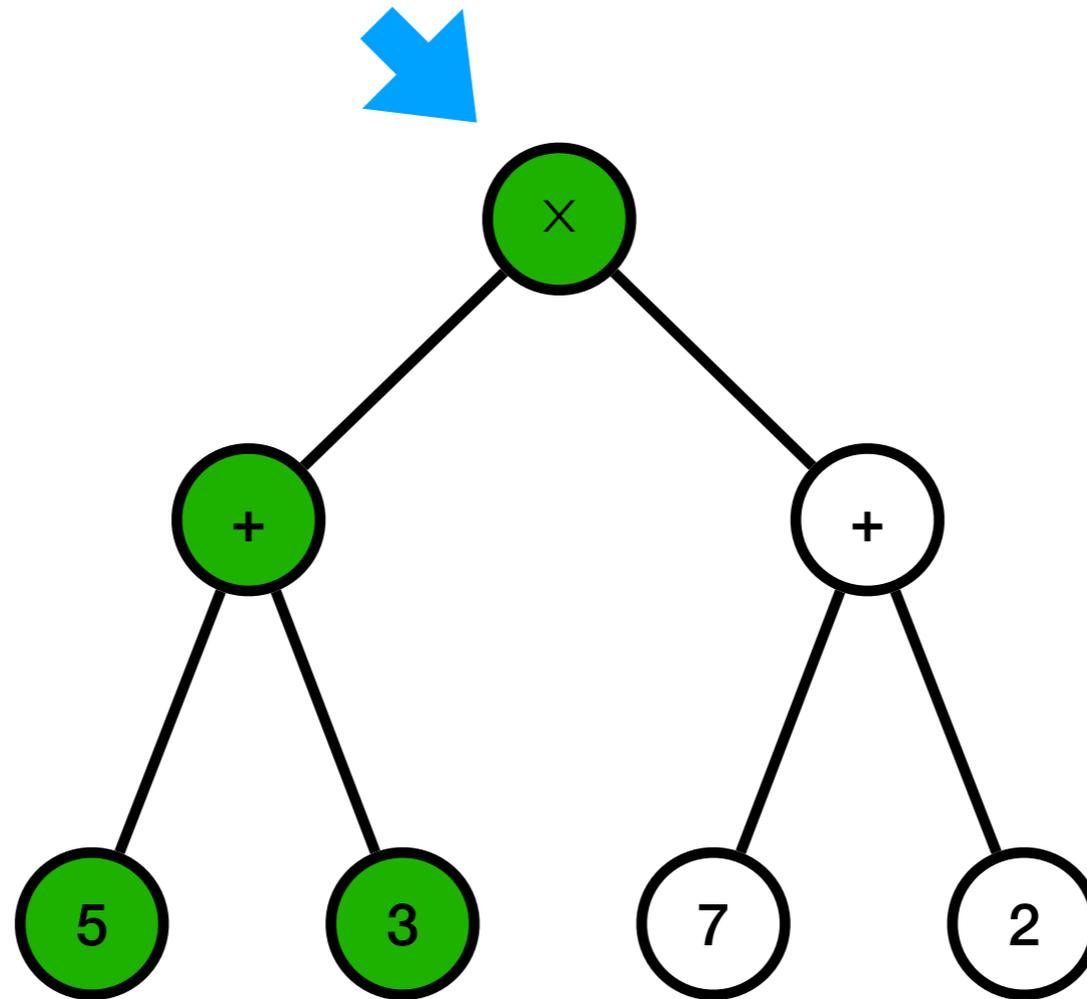
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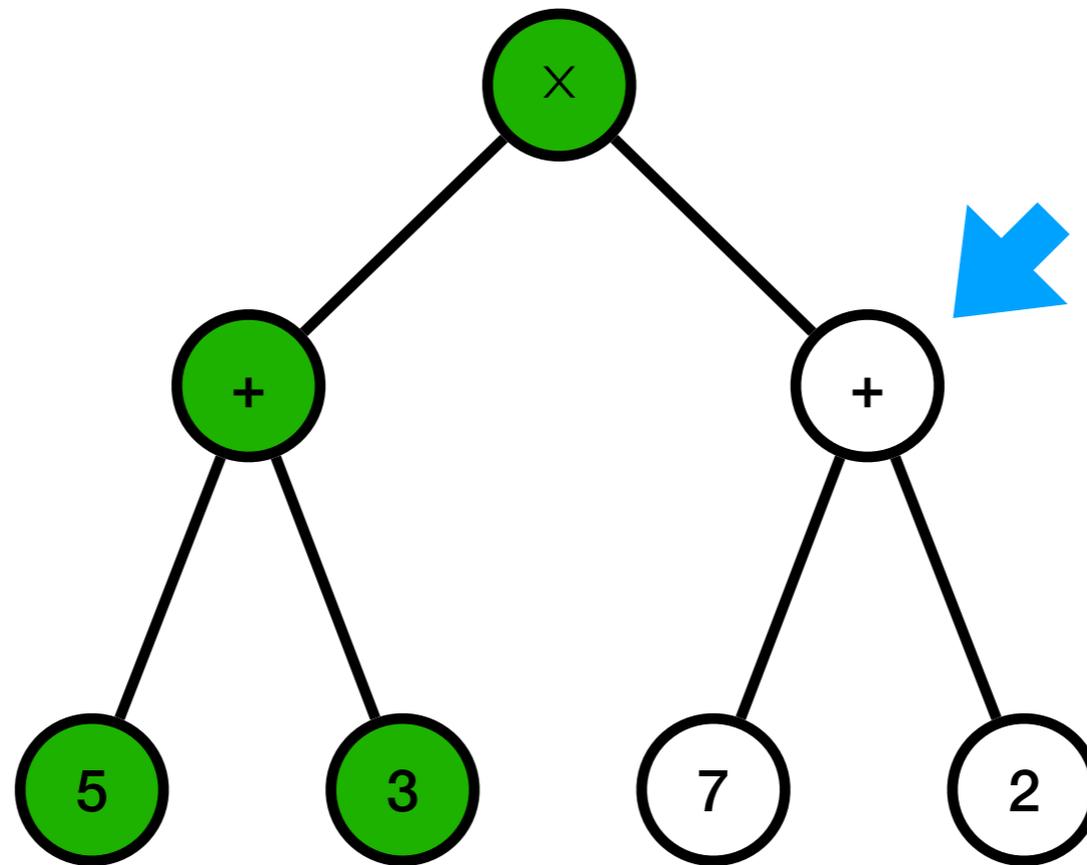
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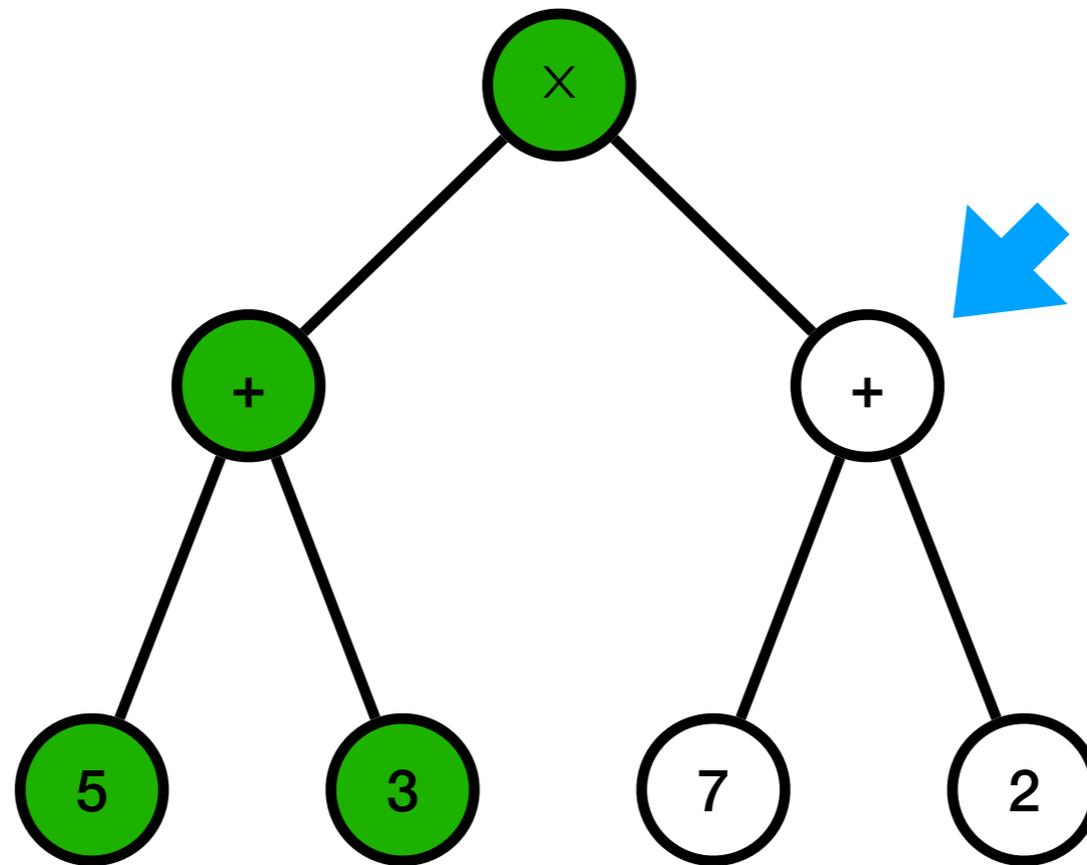
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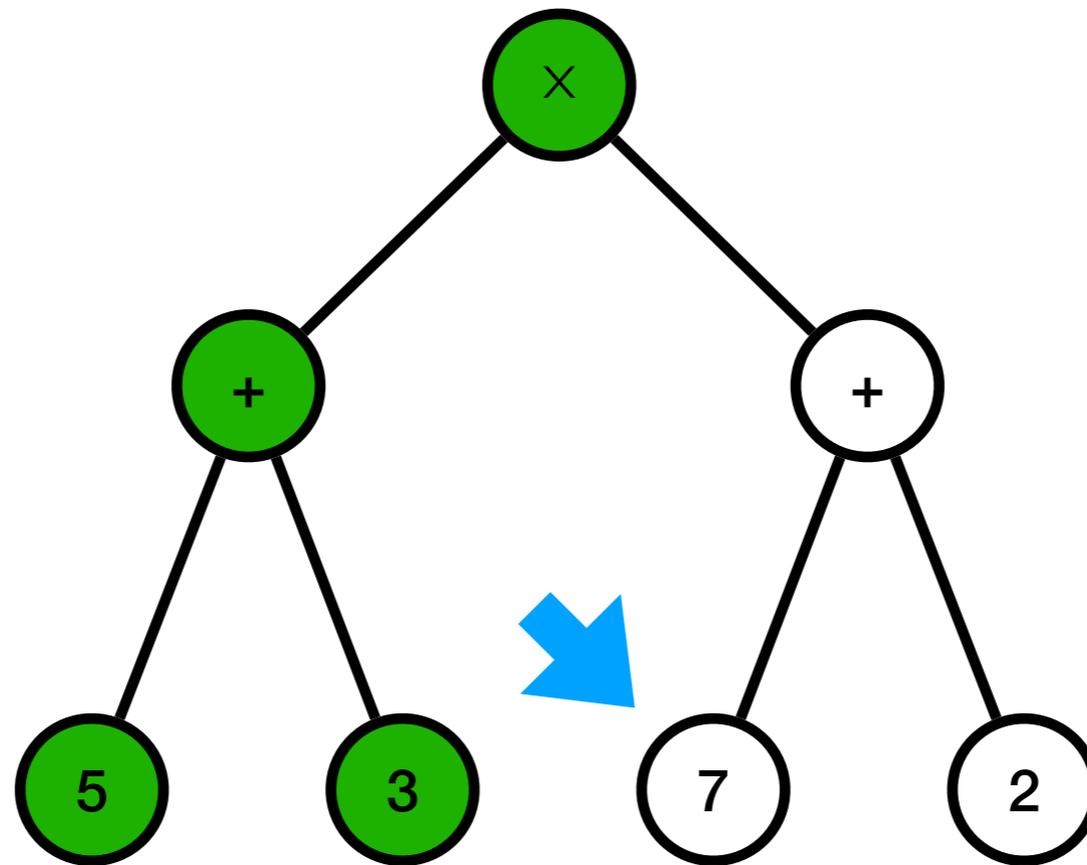
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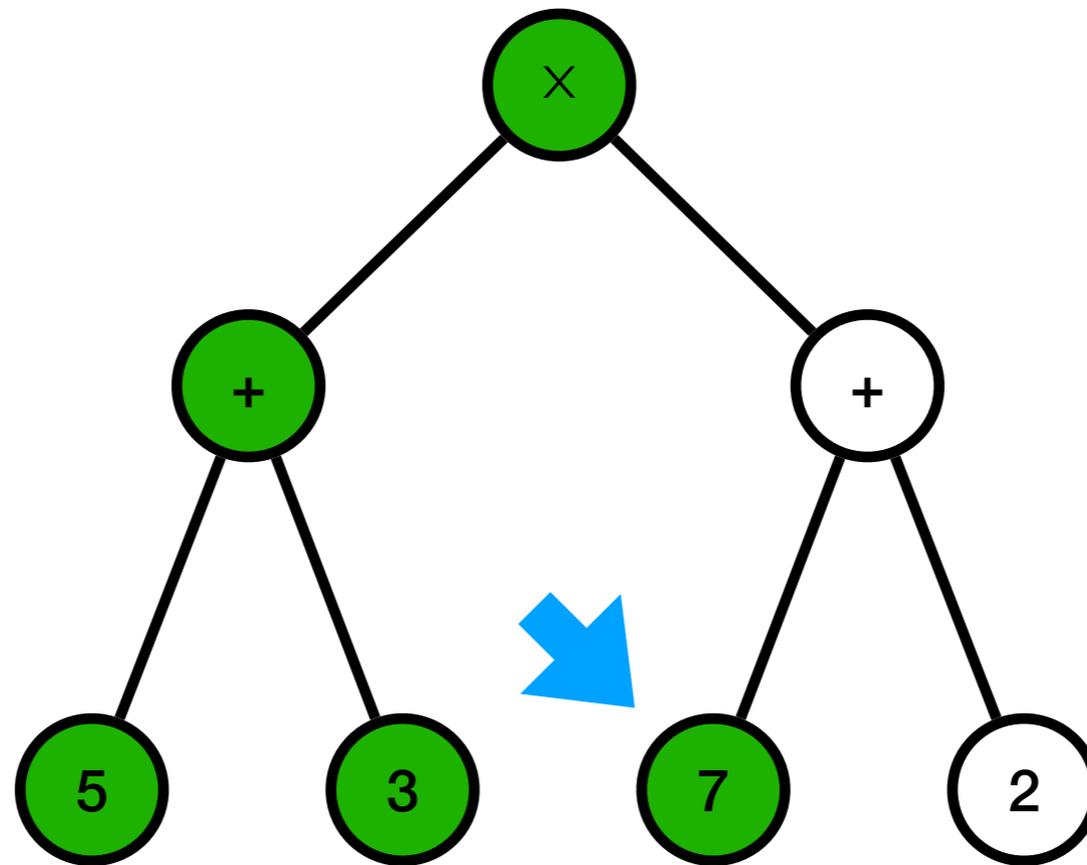
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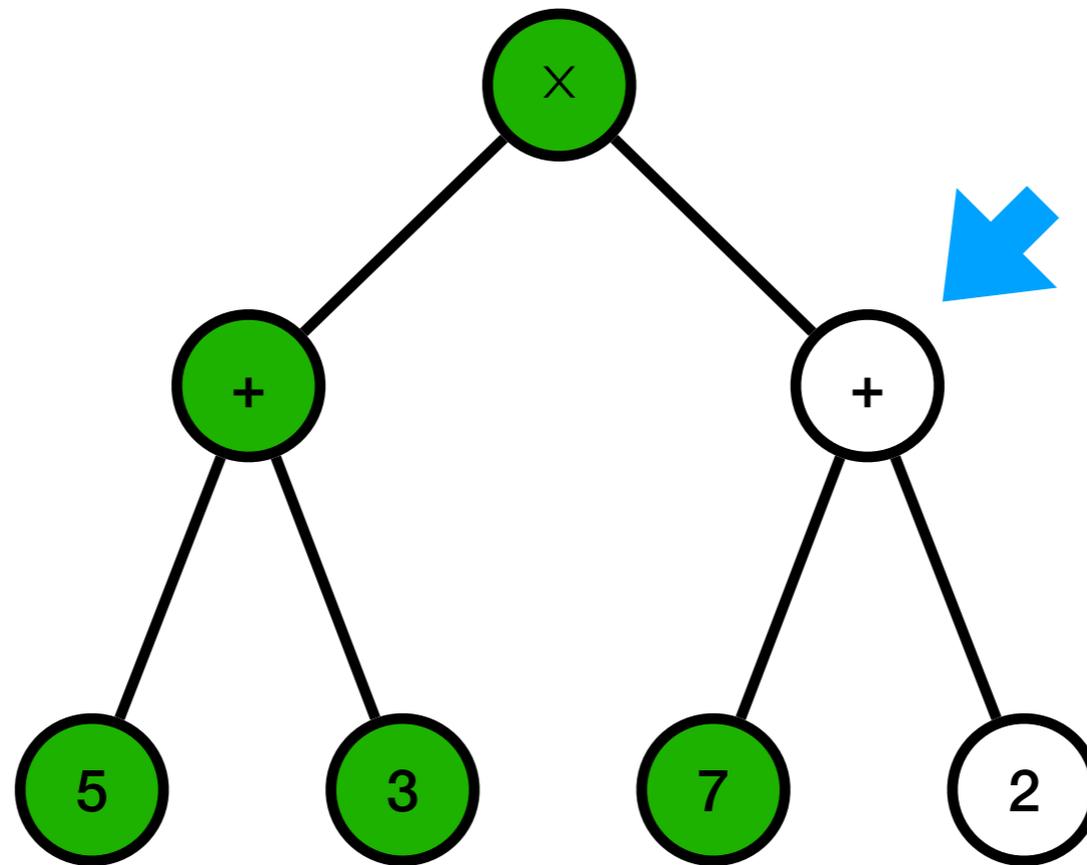
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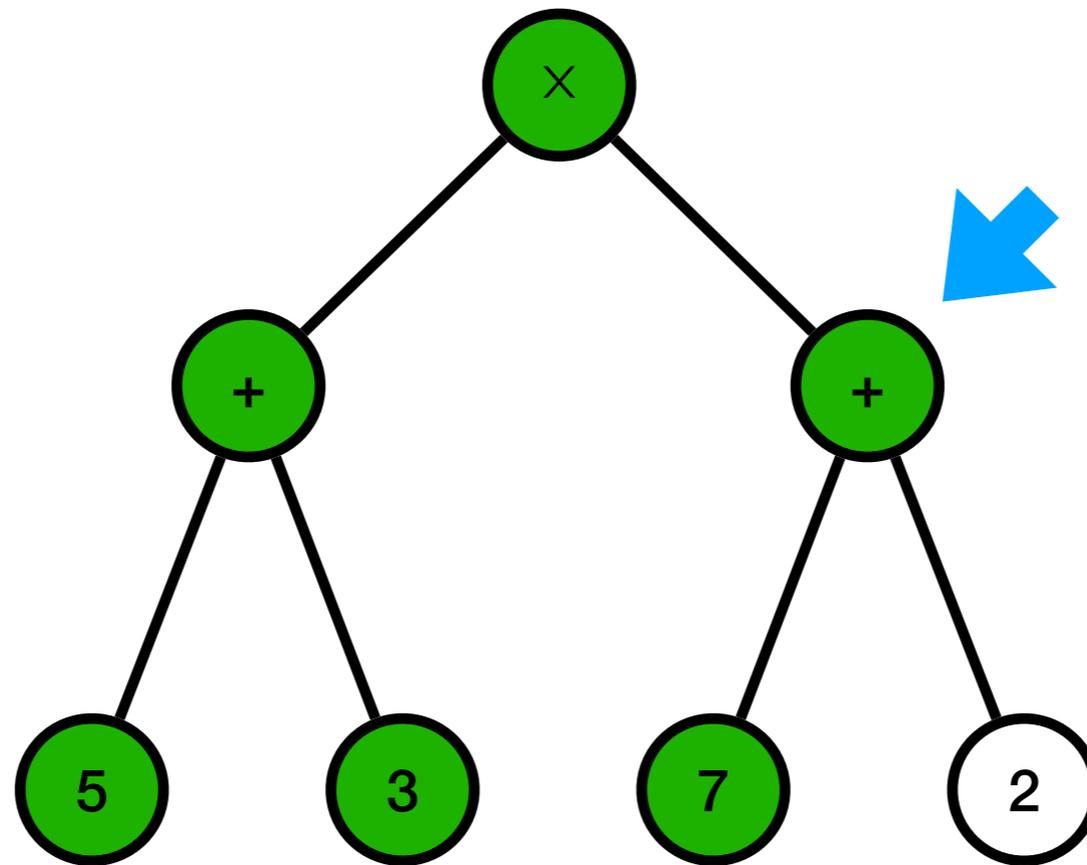
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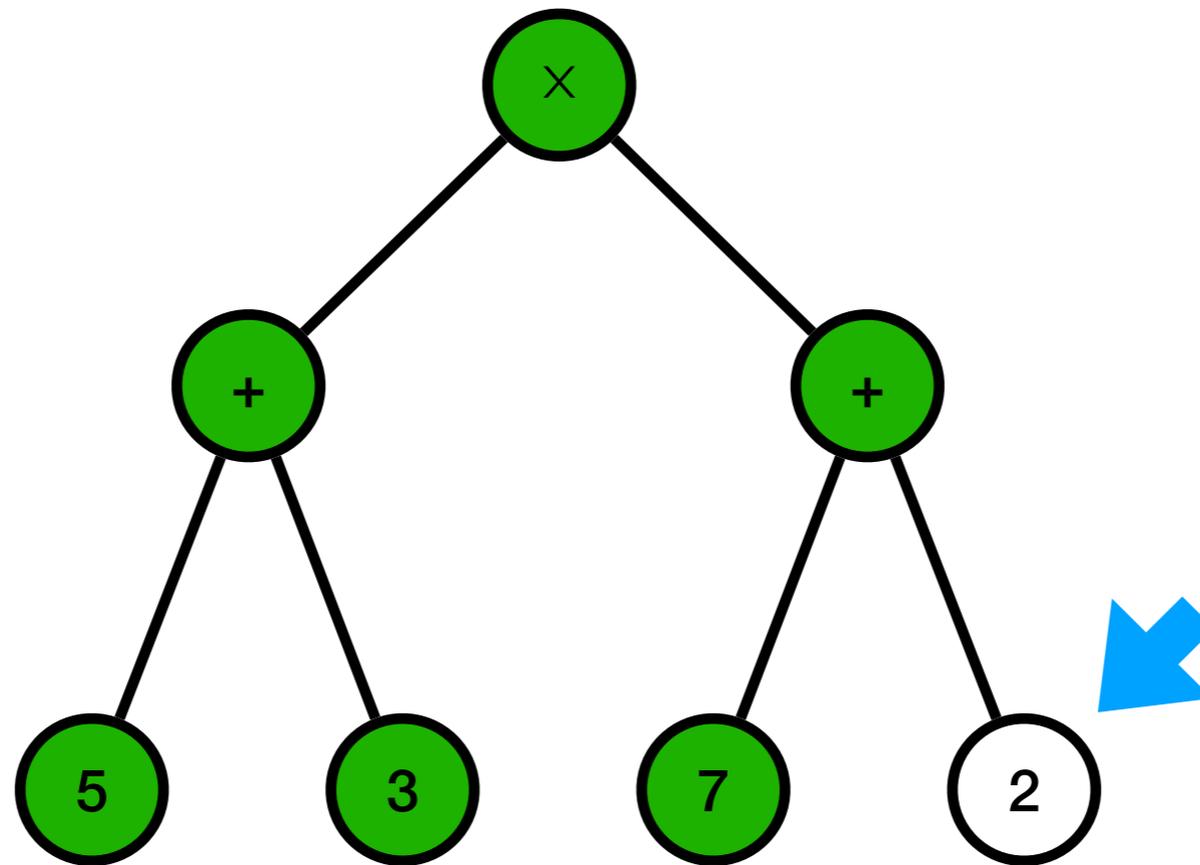
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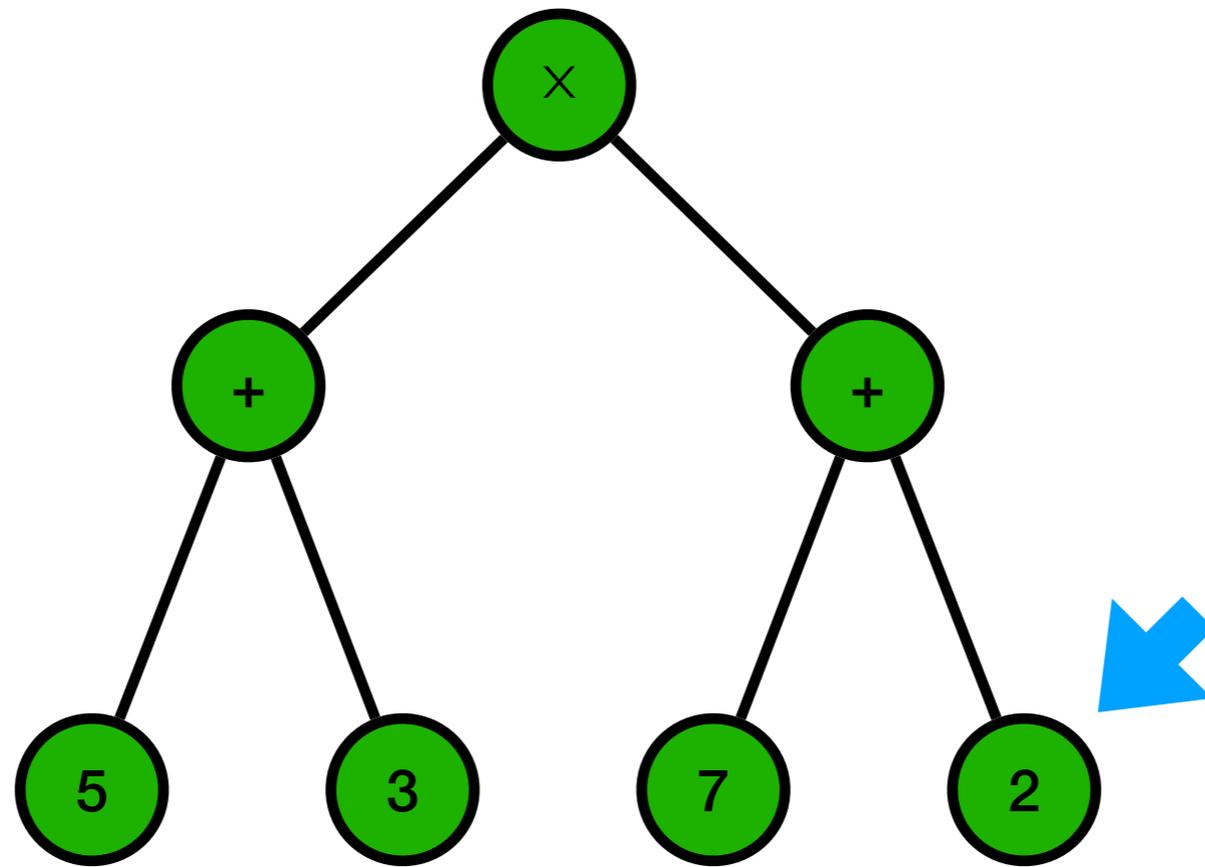
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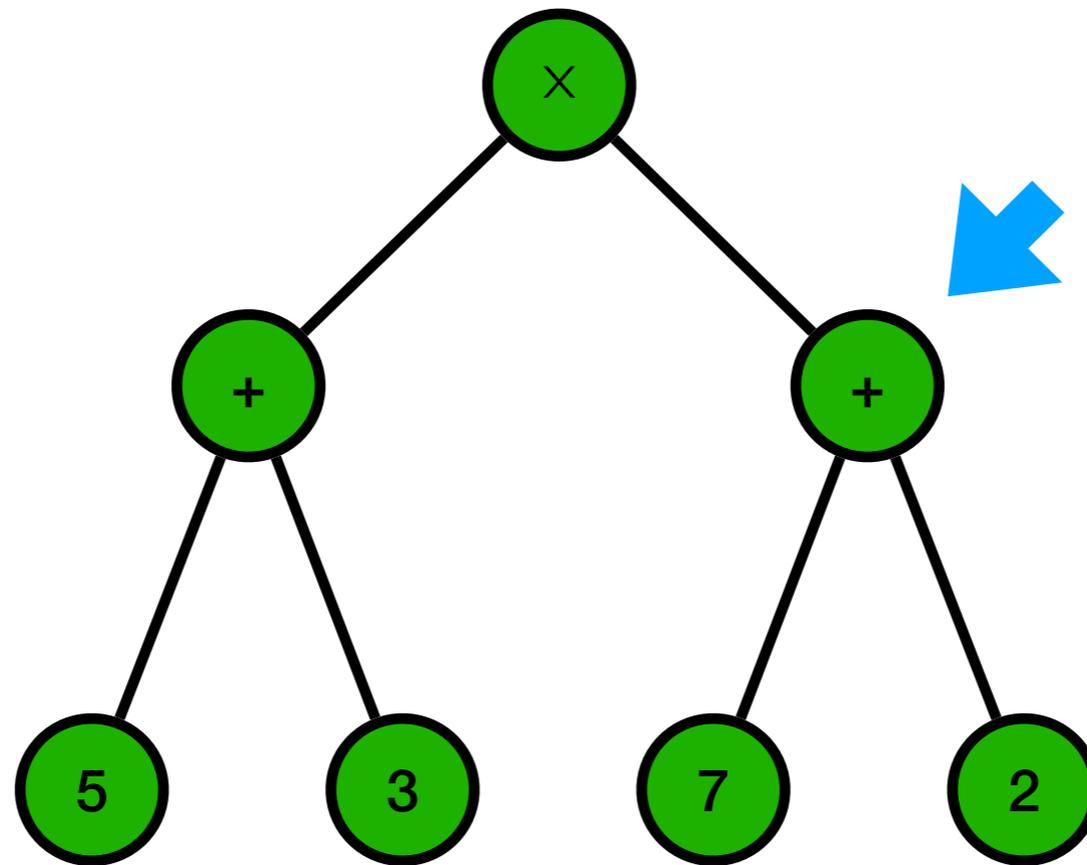
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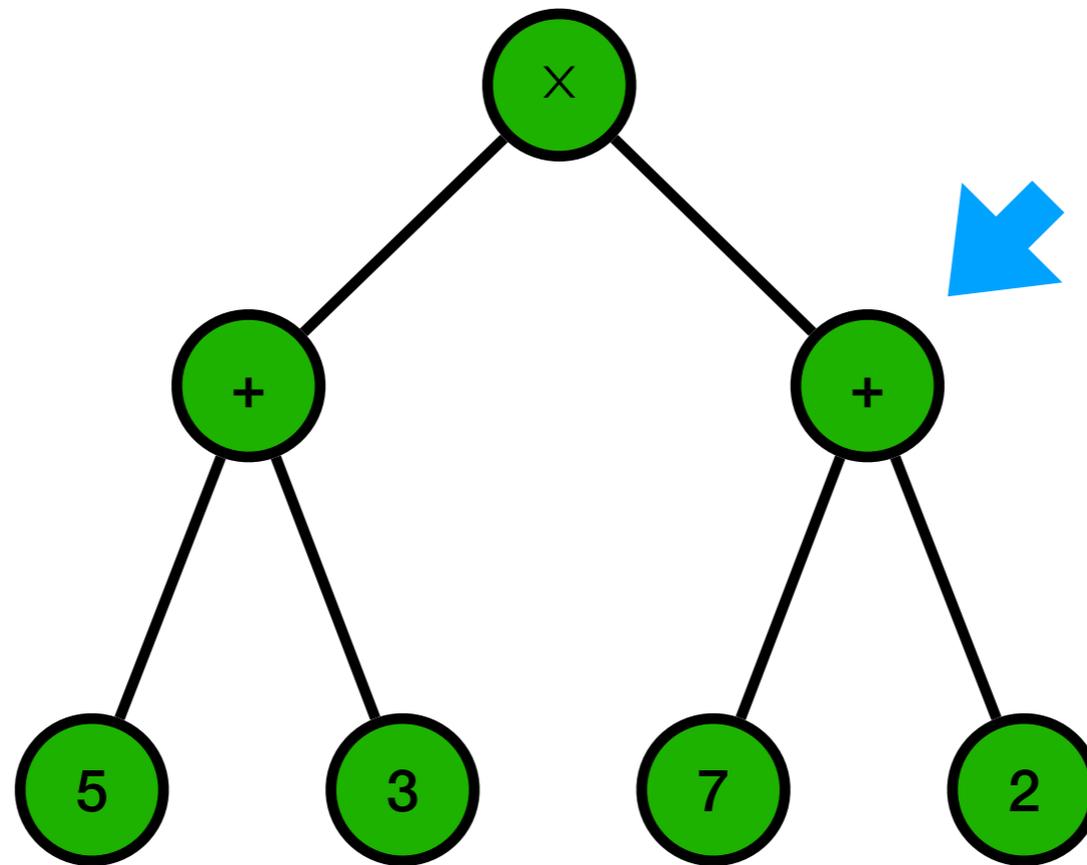
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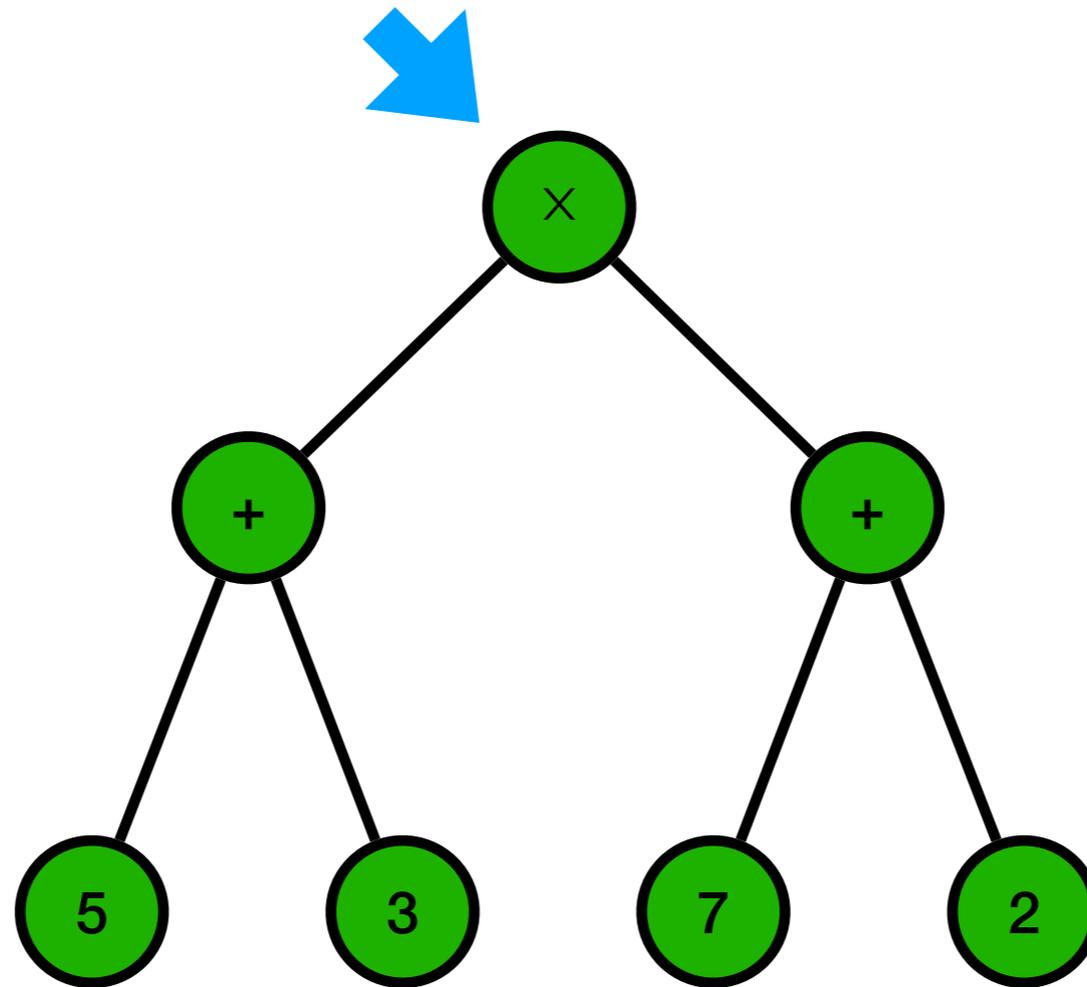
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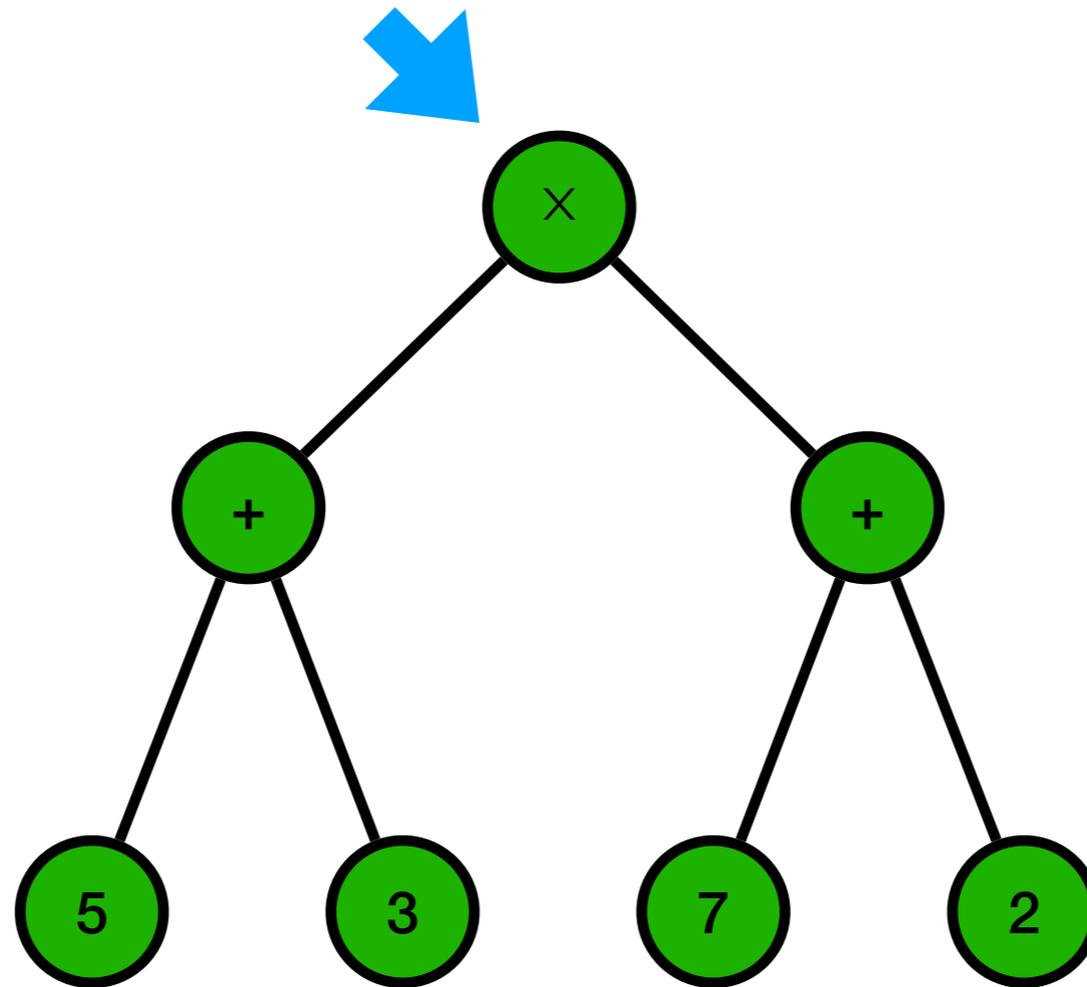
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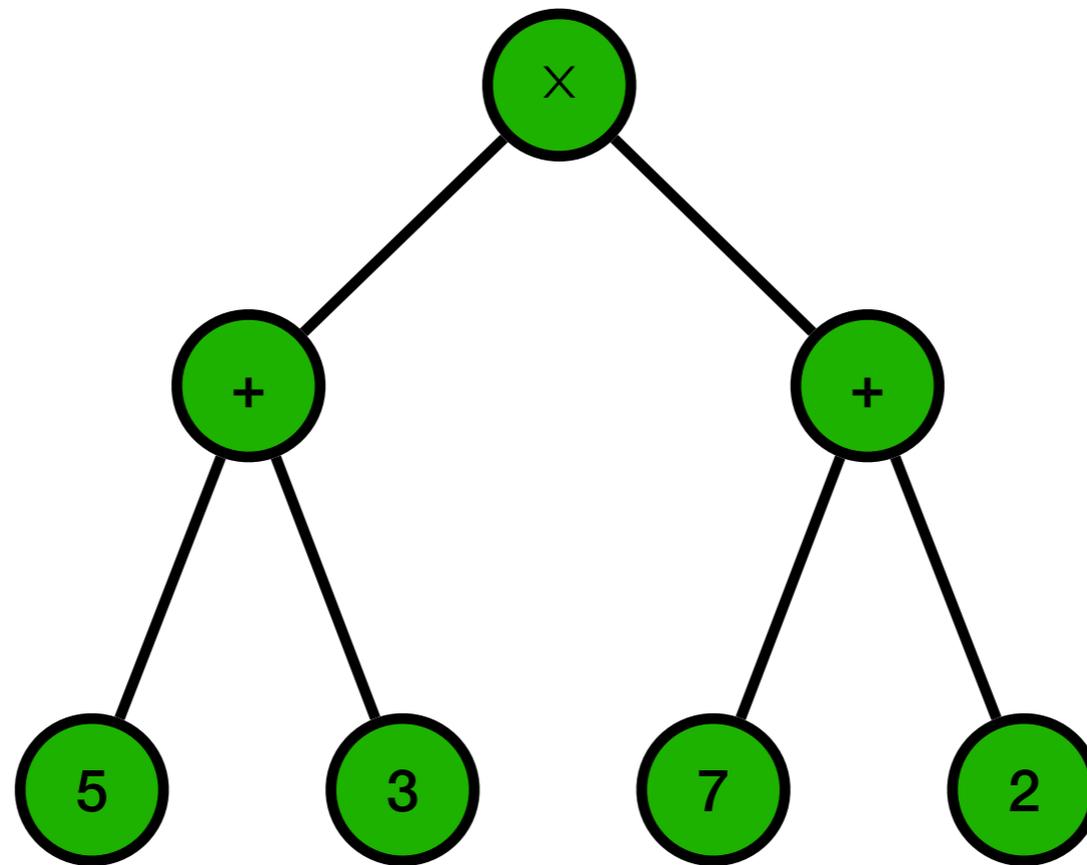
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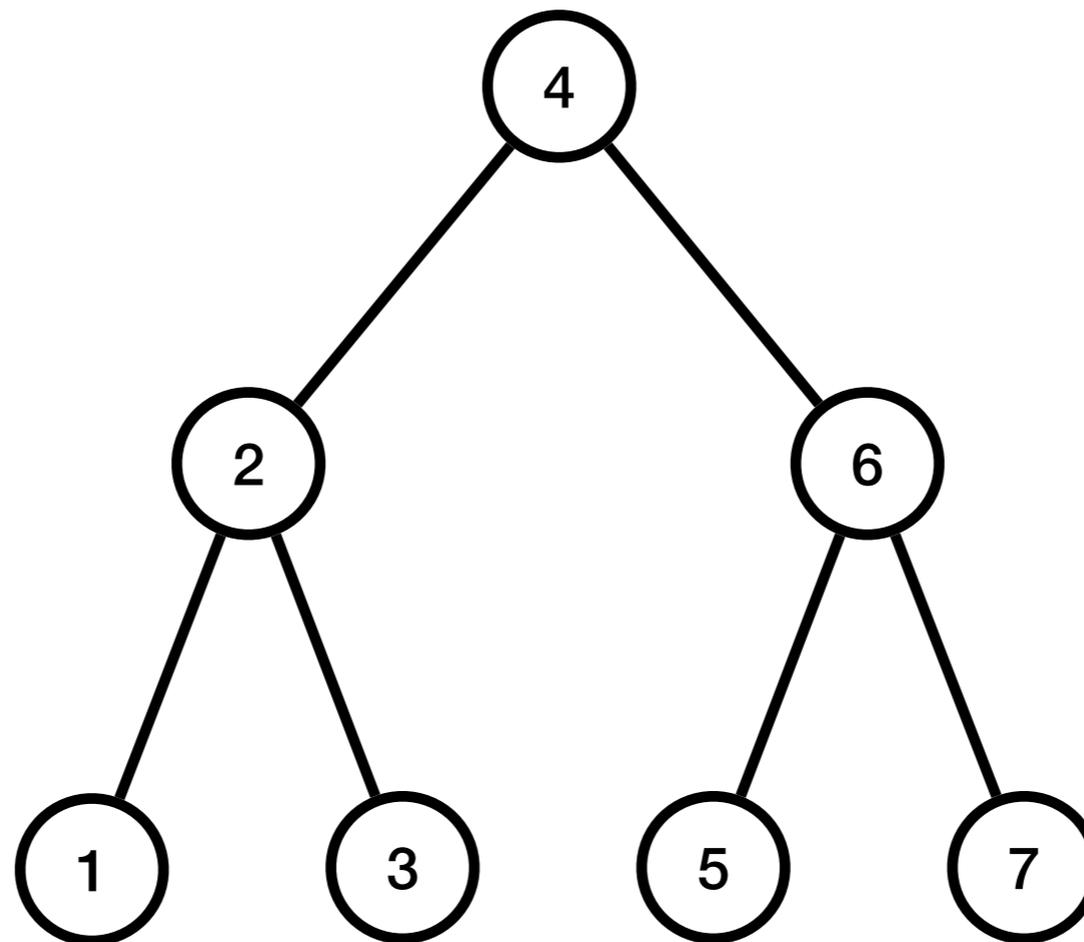
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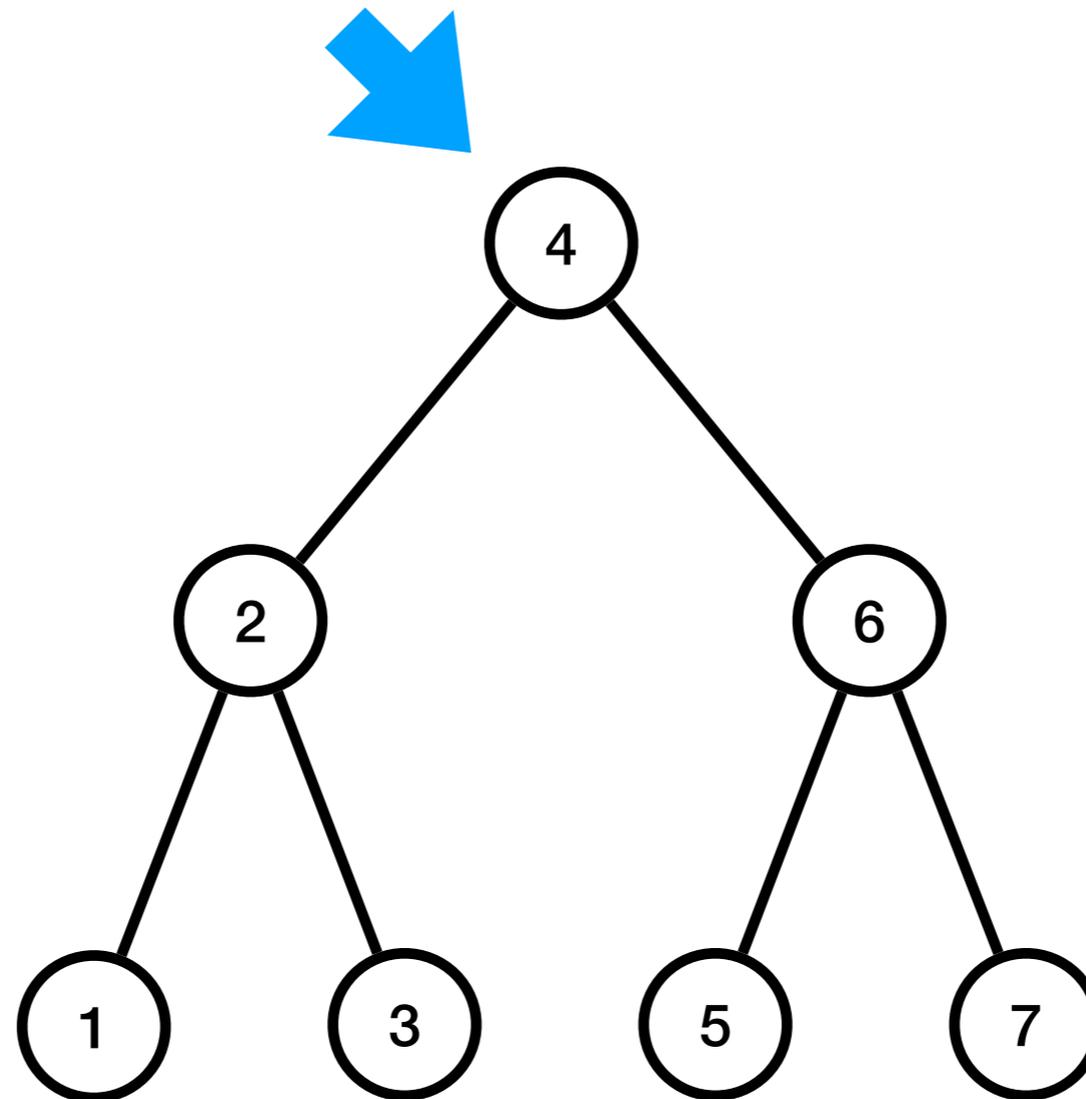


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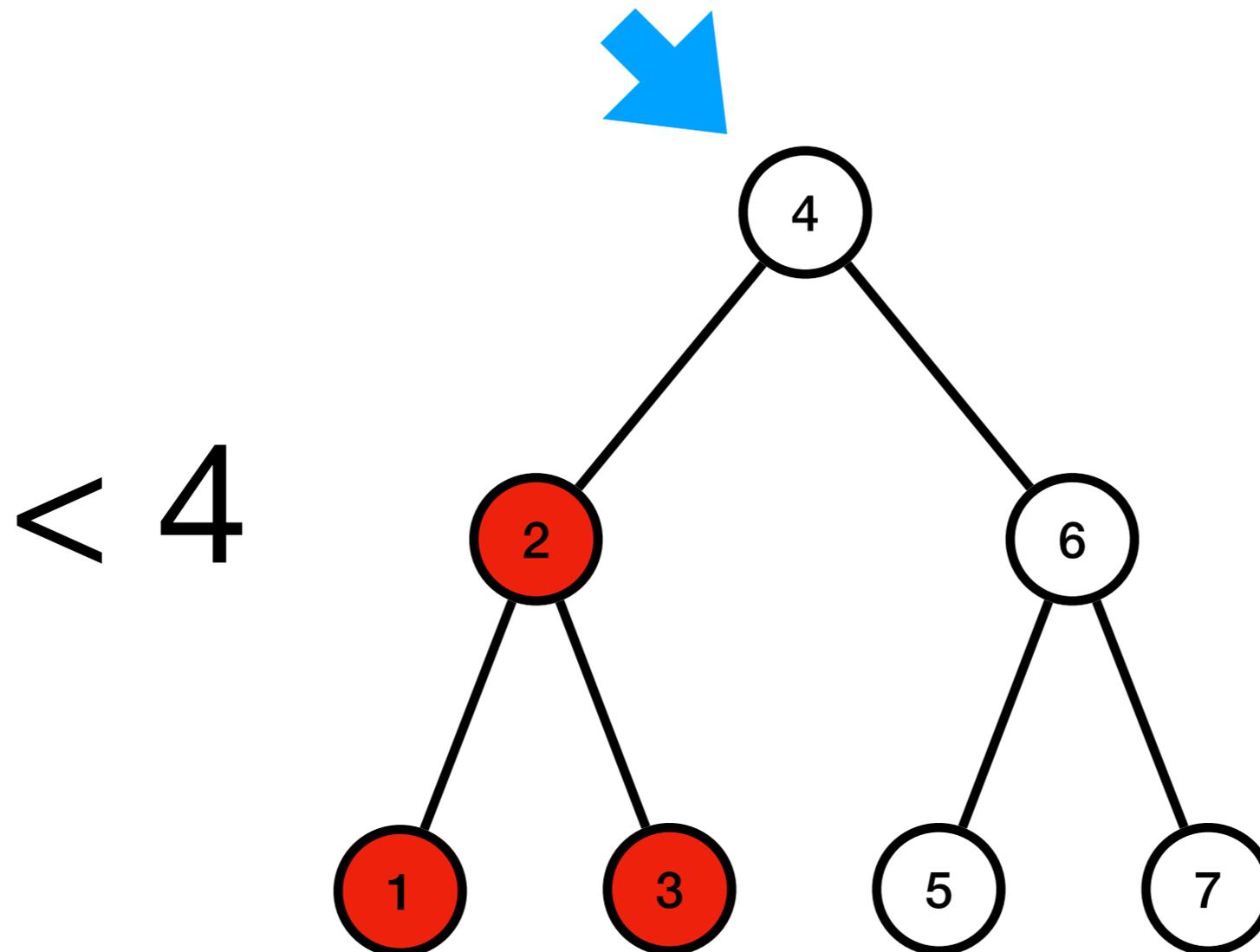
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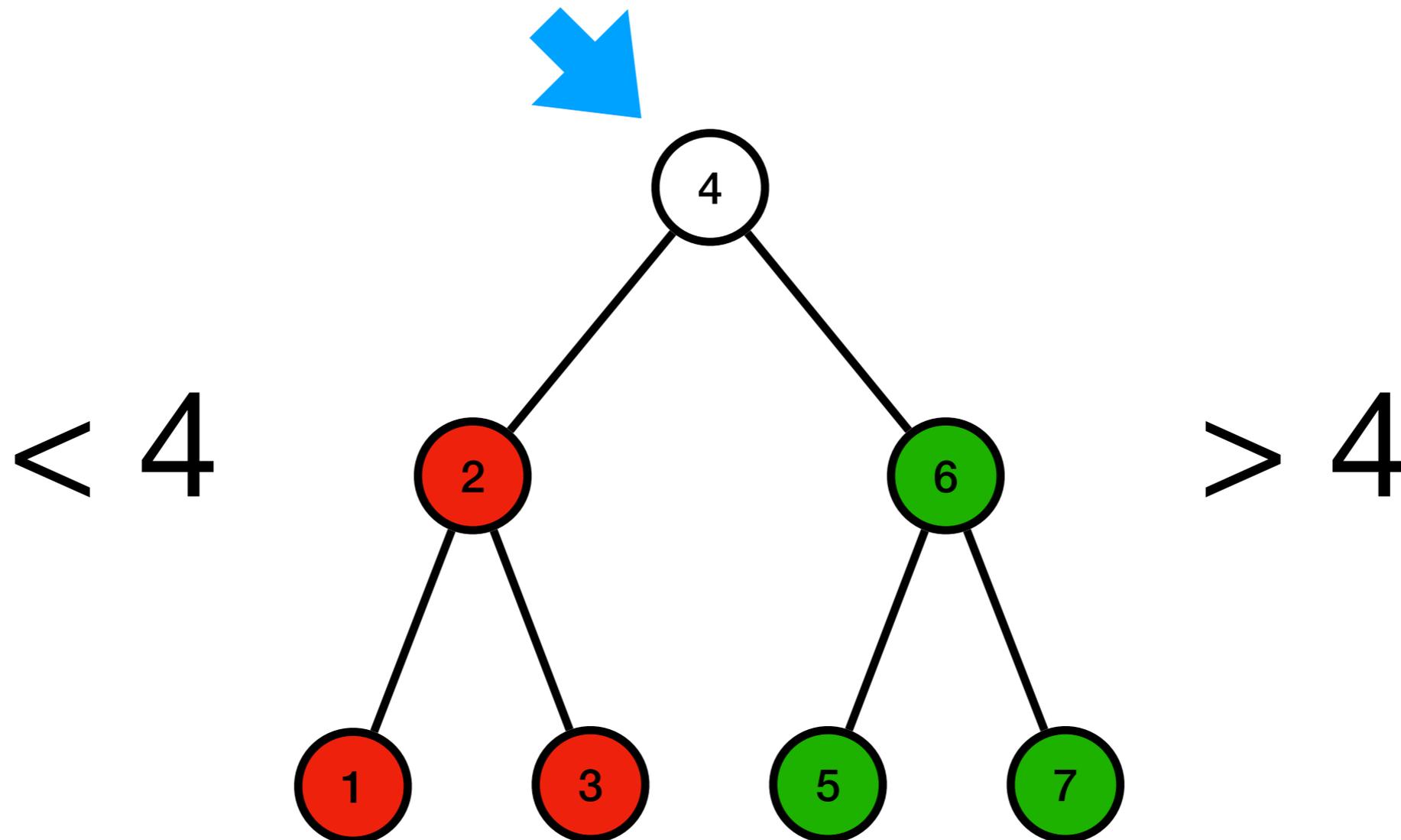
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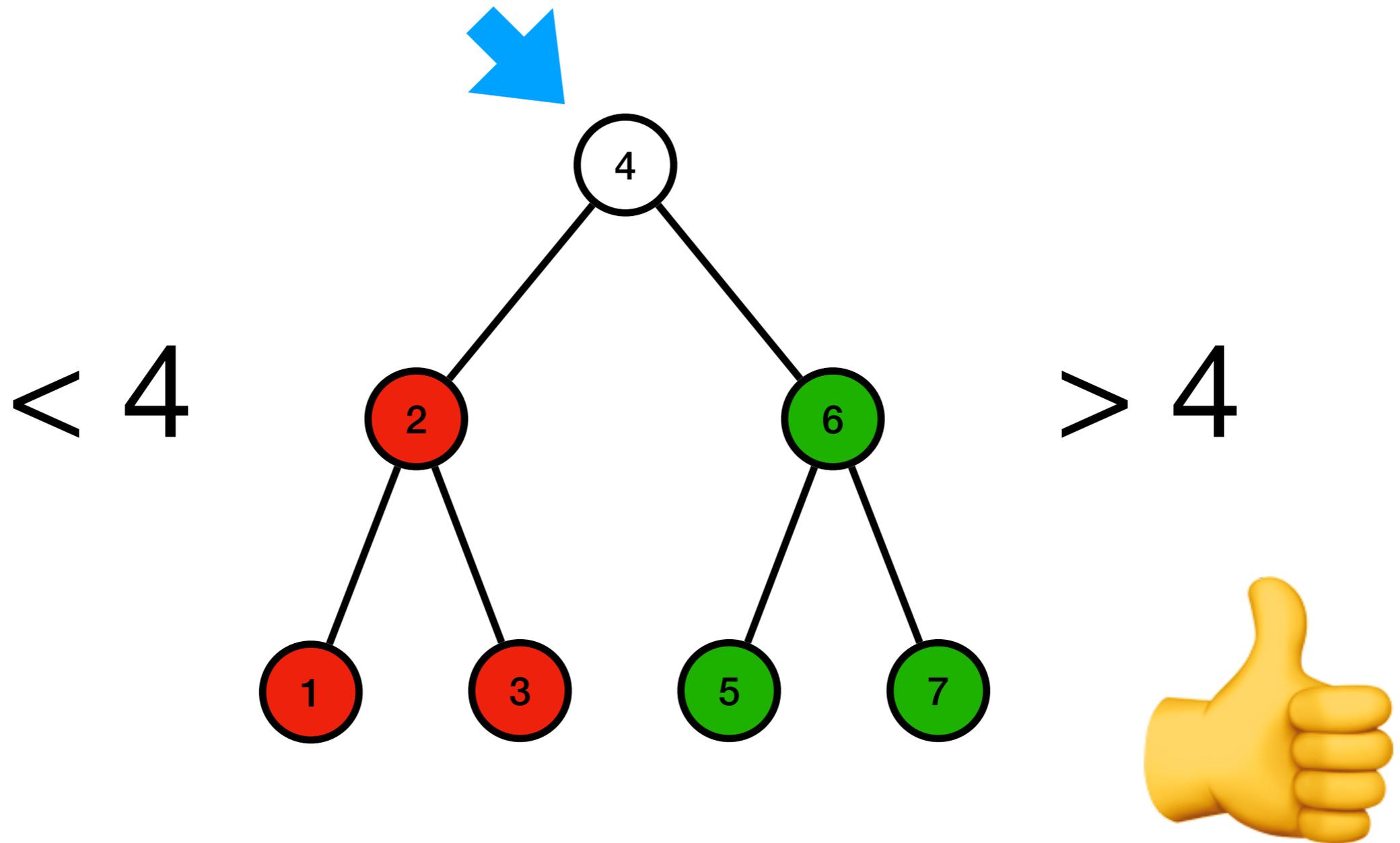
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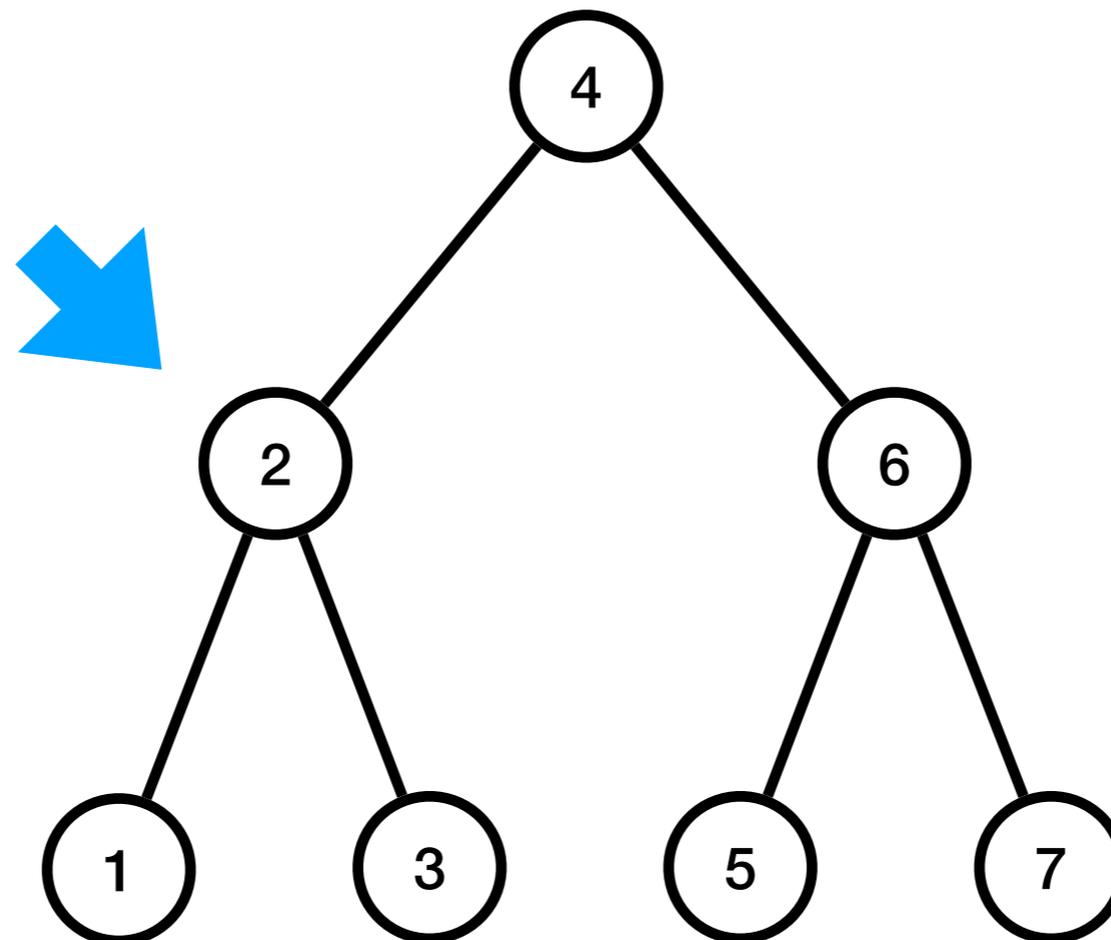
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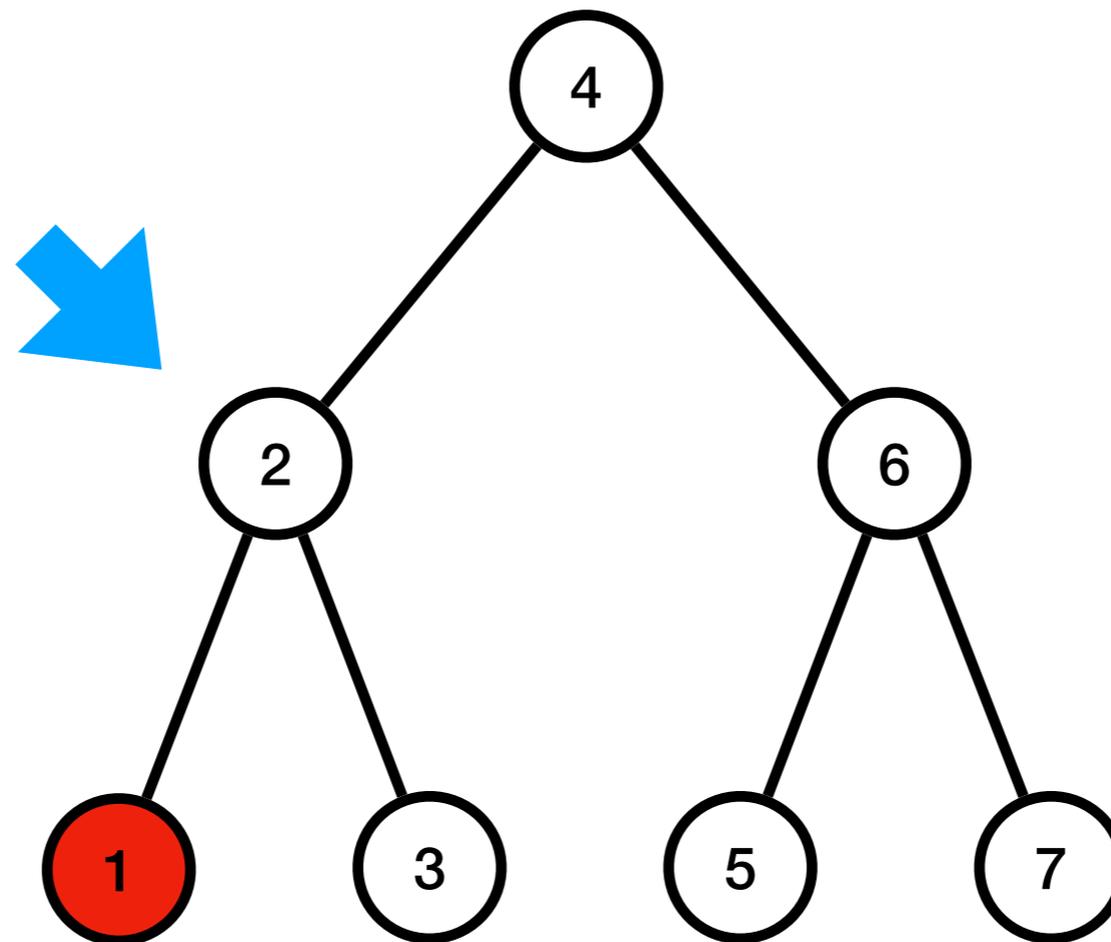
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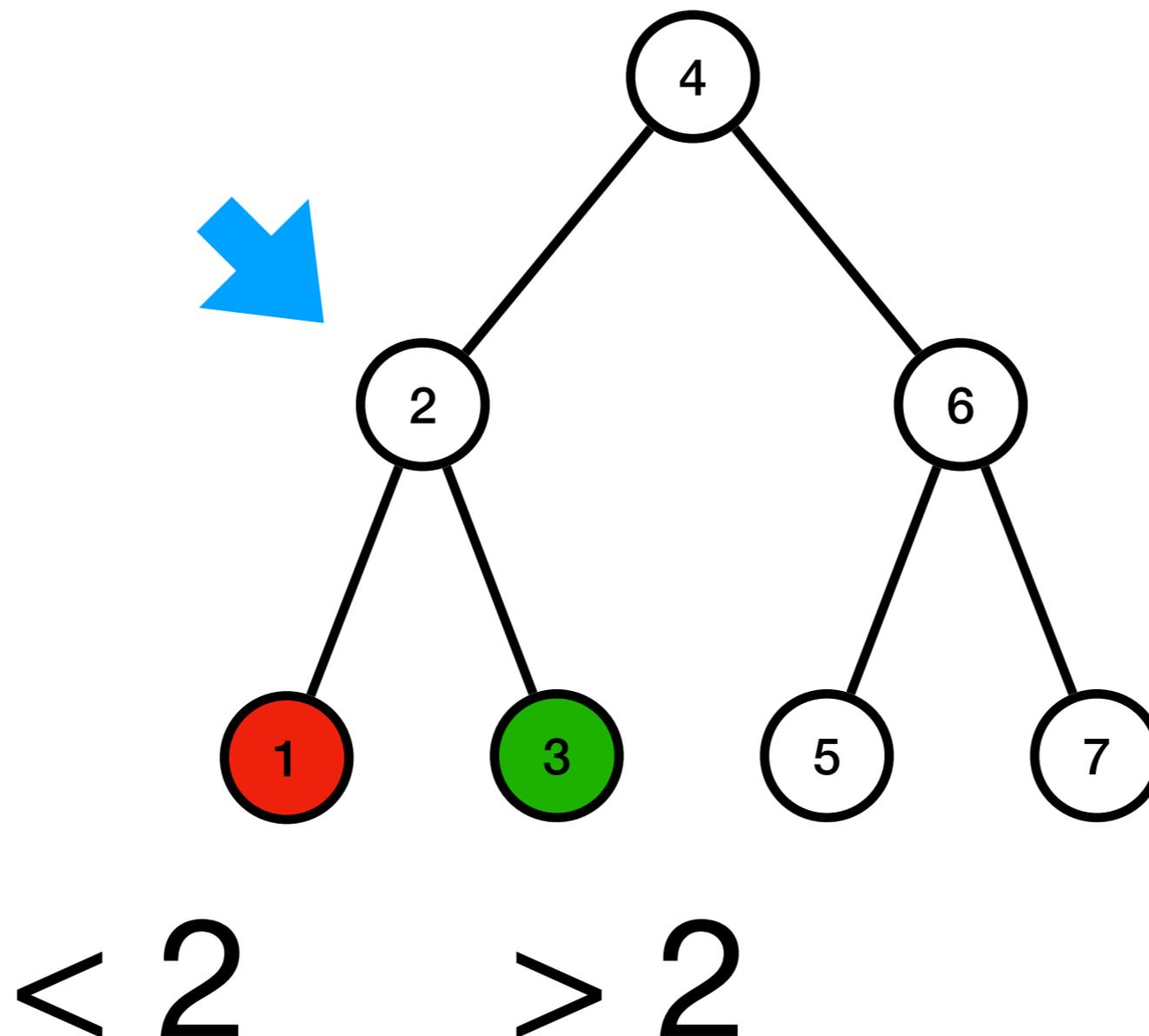


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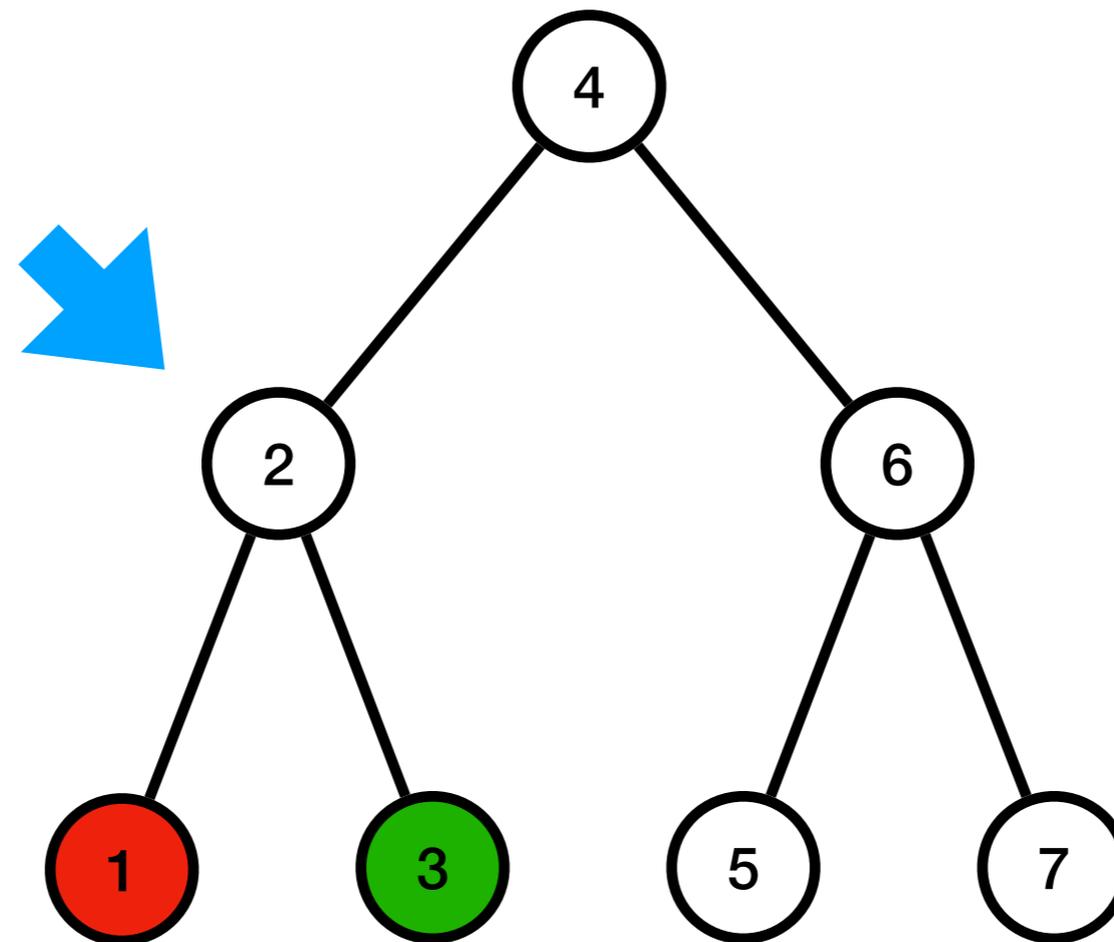


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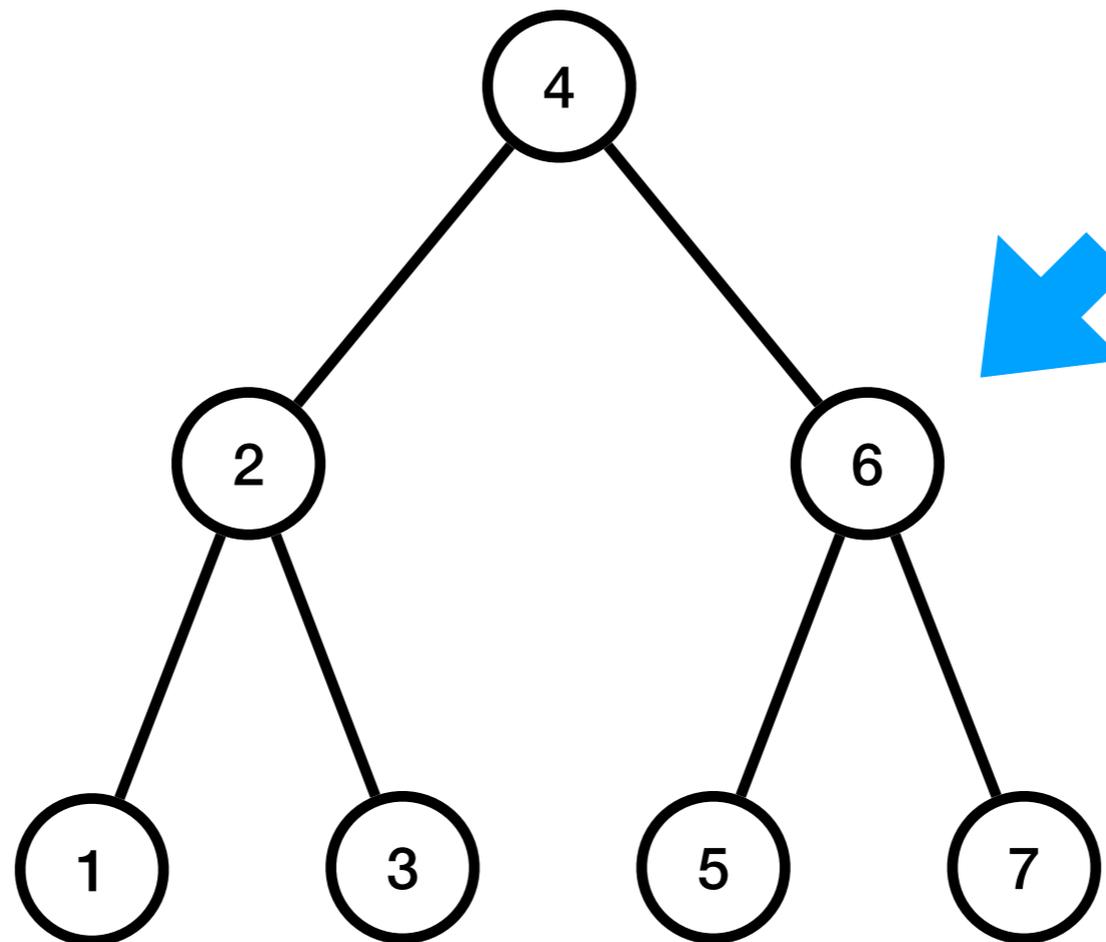
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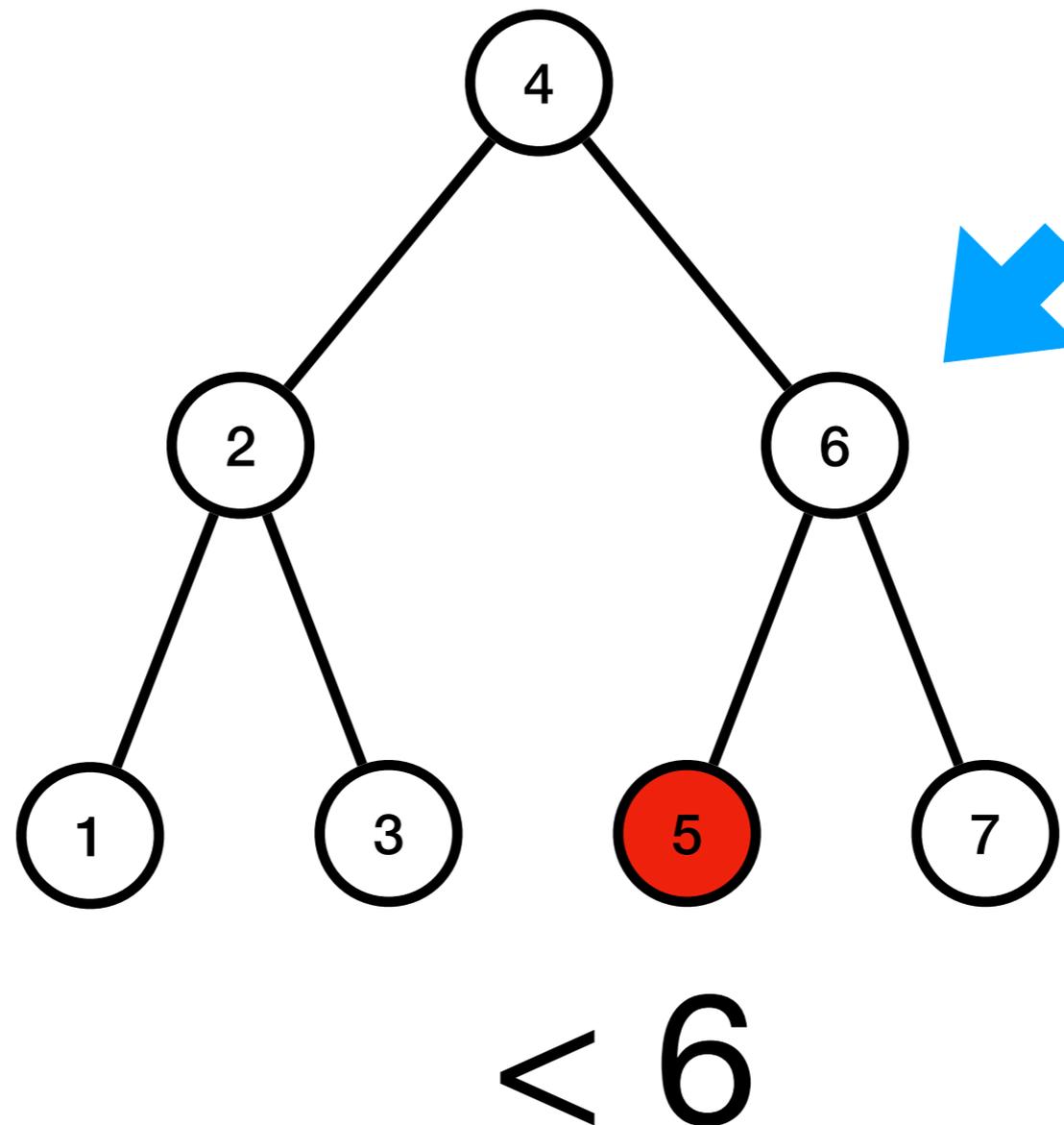
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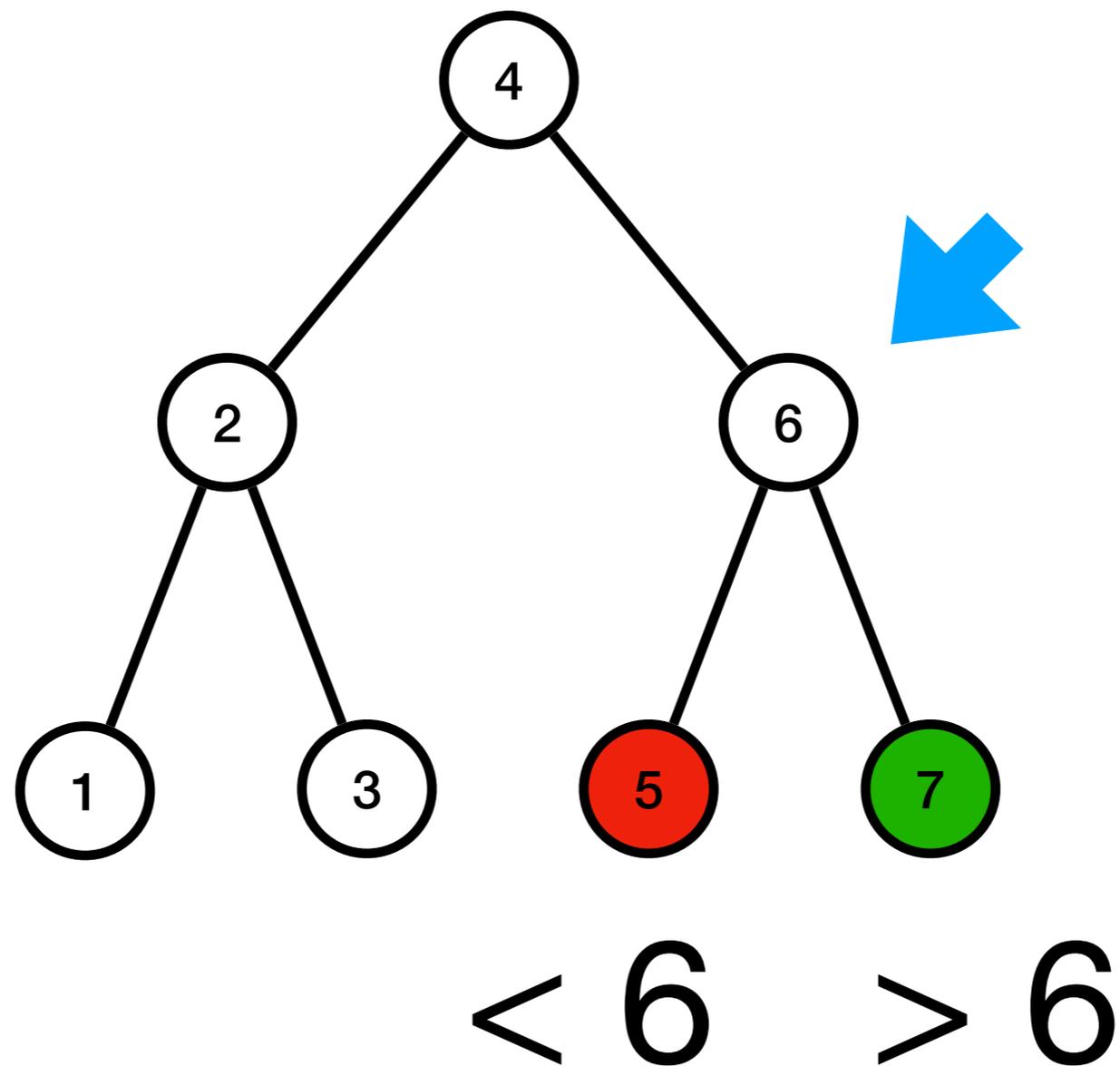
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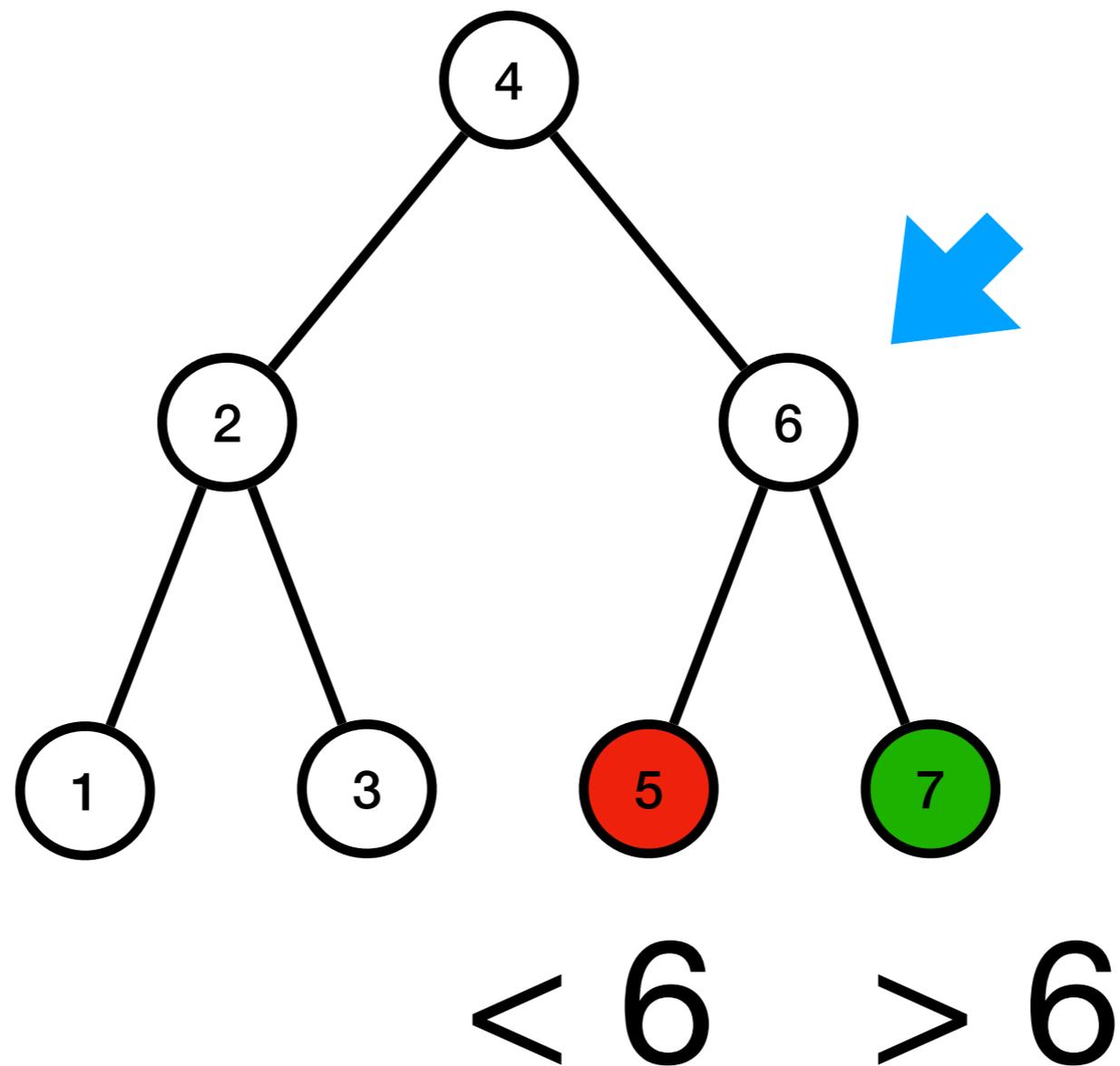
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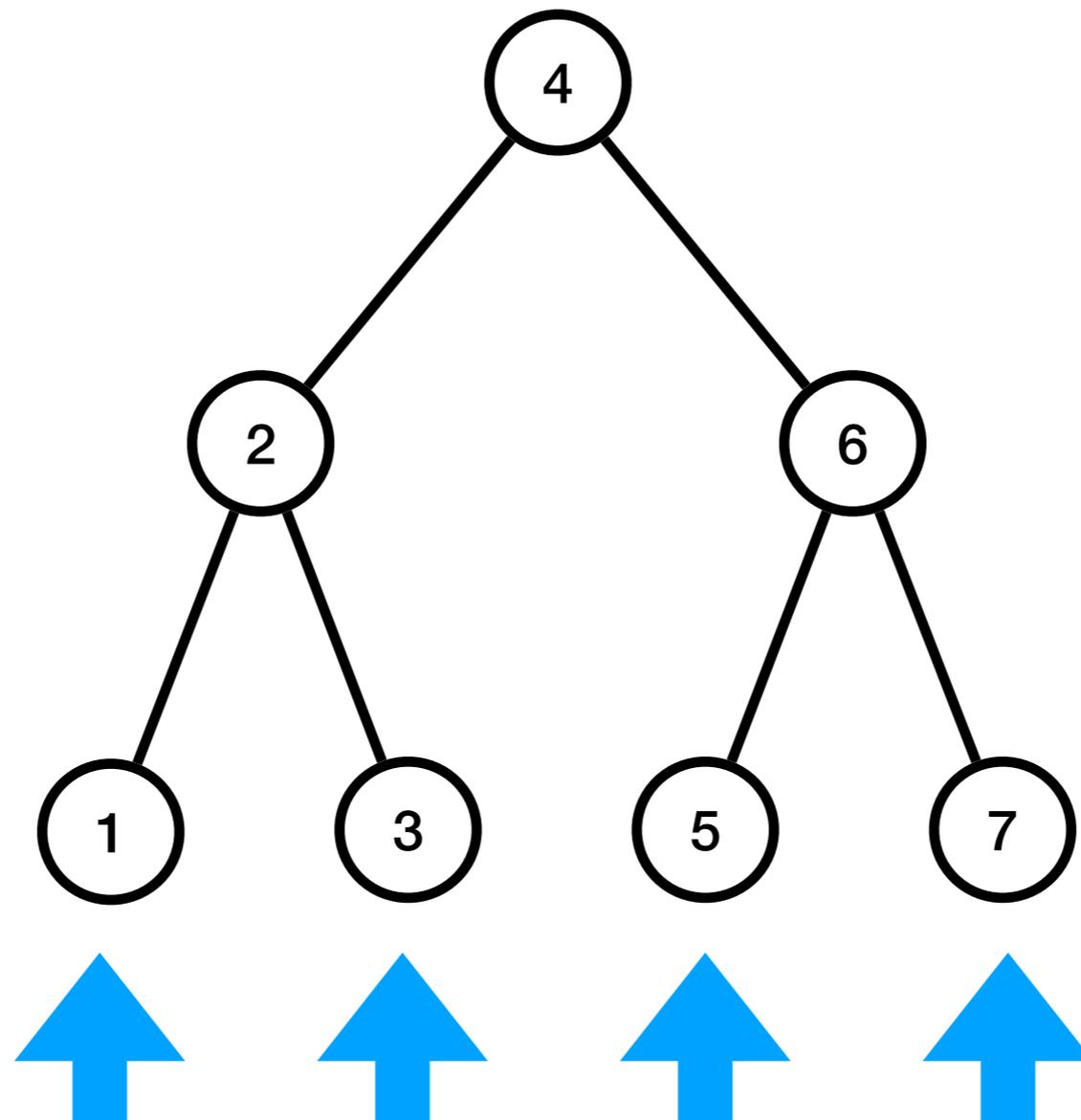
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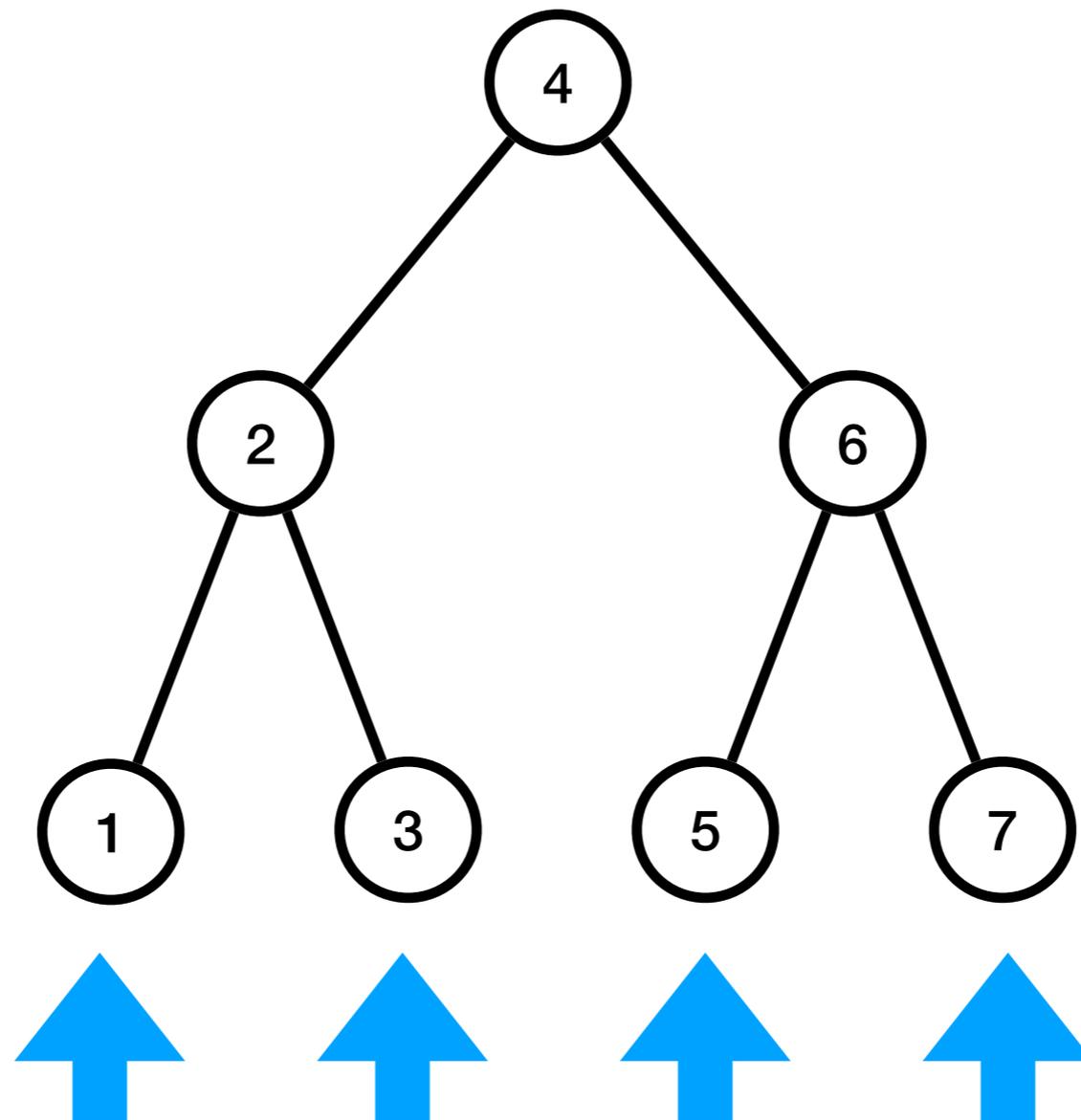
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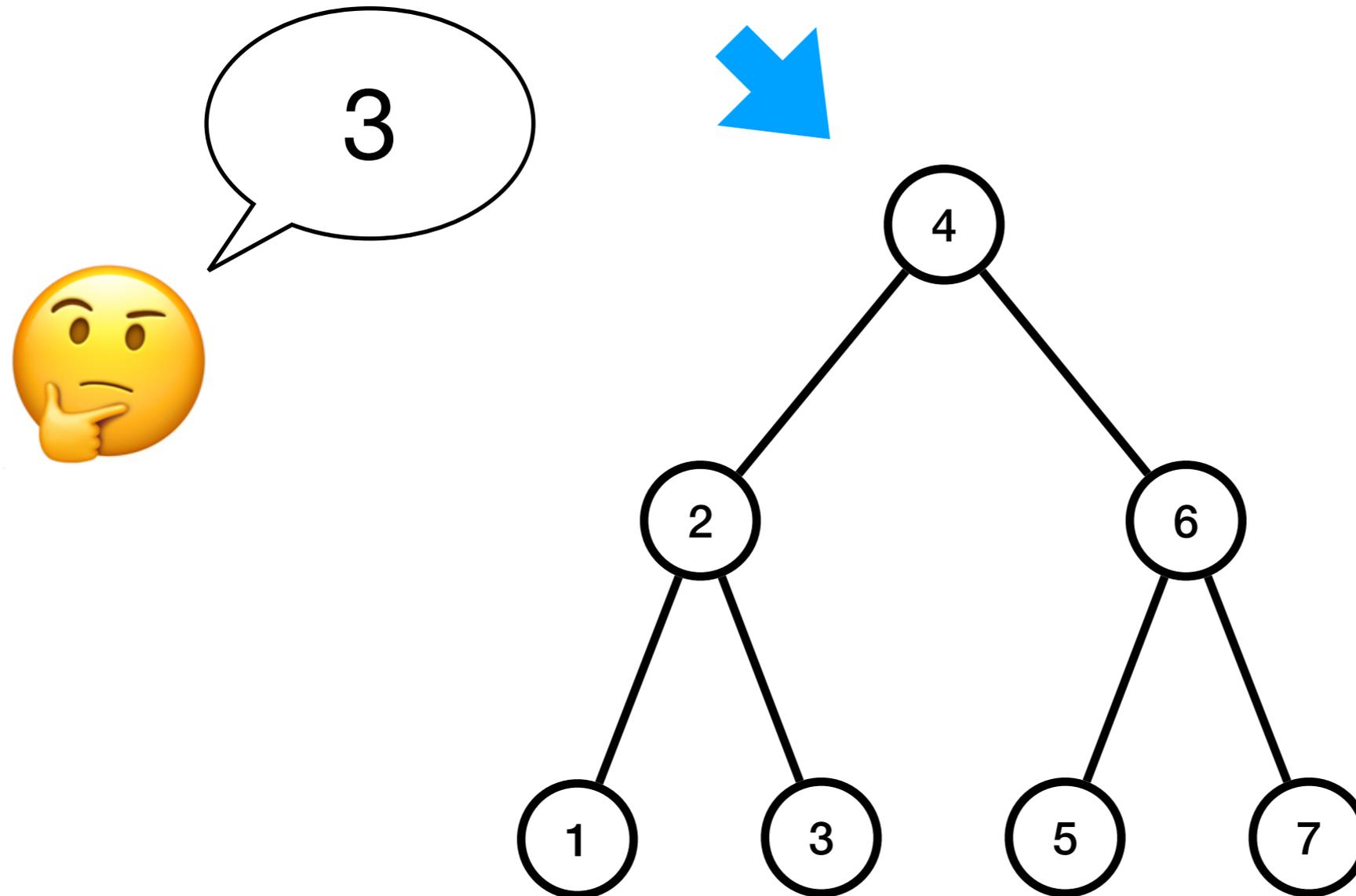
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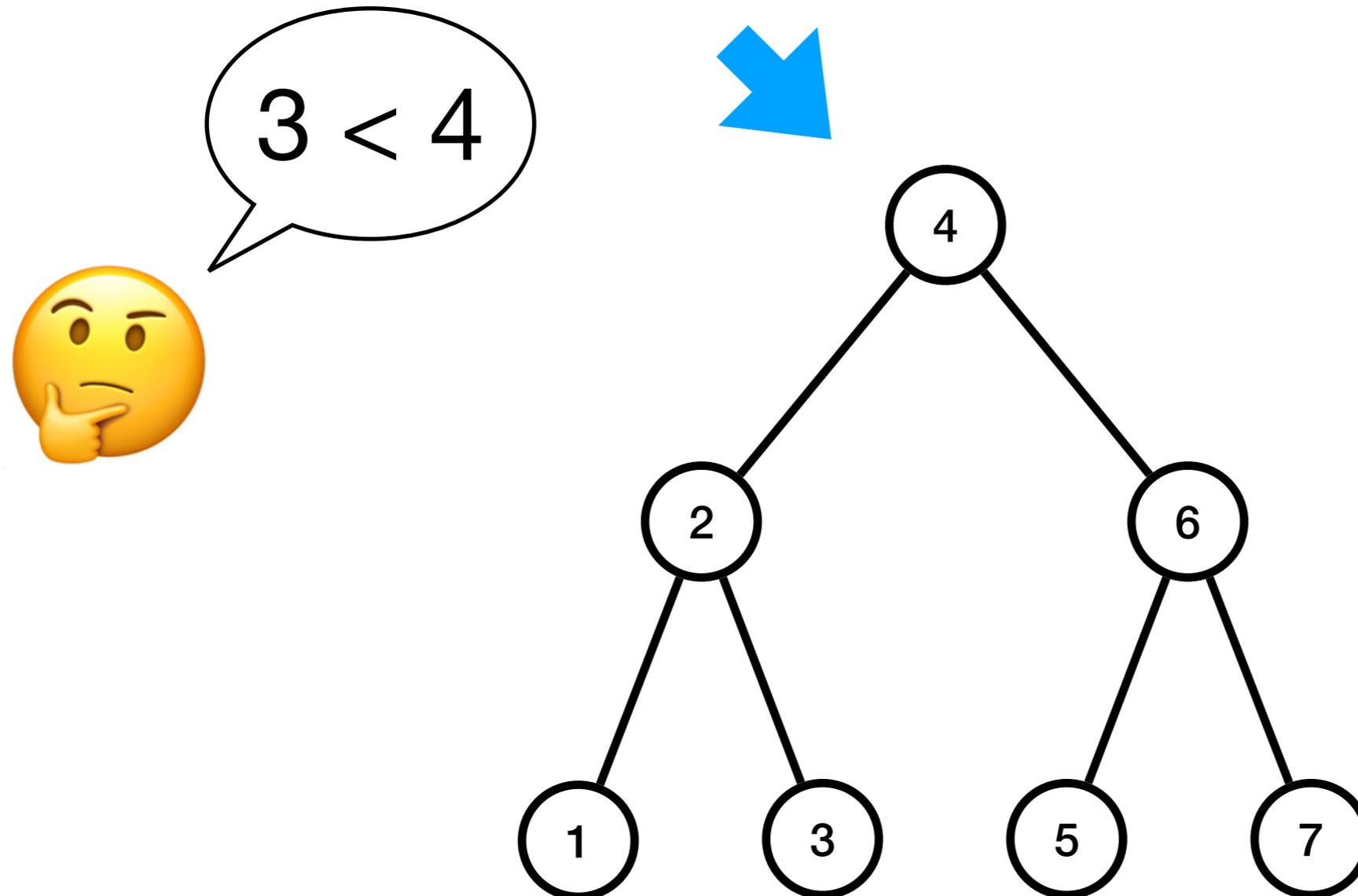
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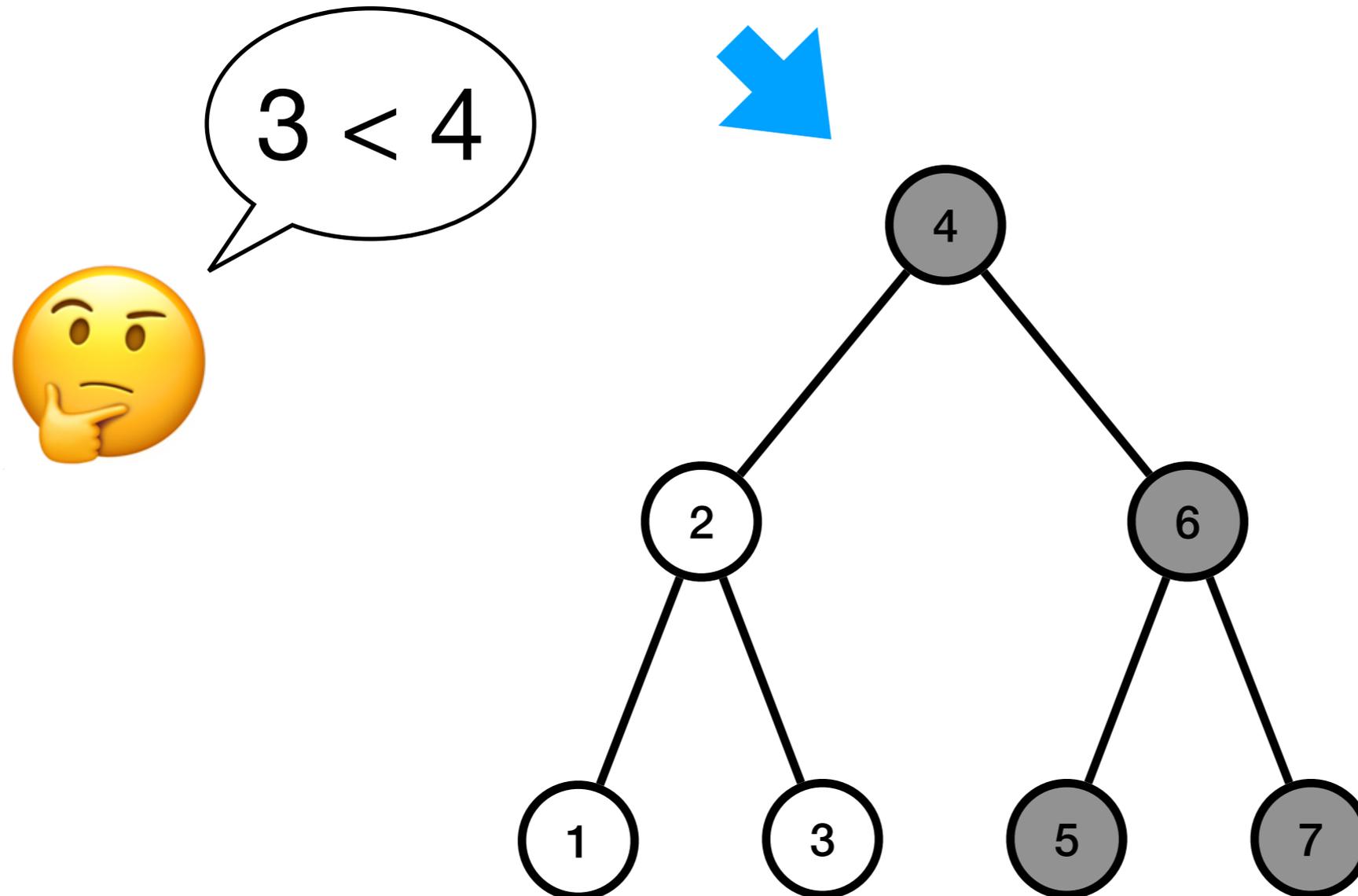
Recherche dans un ABR



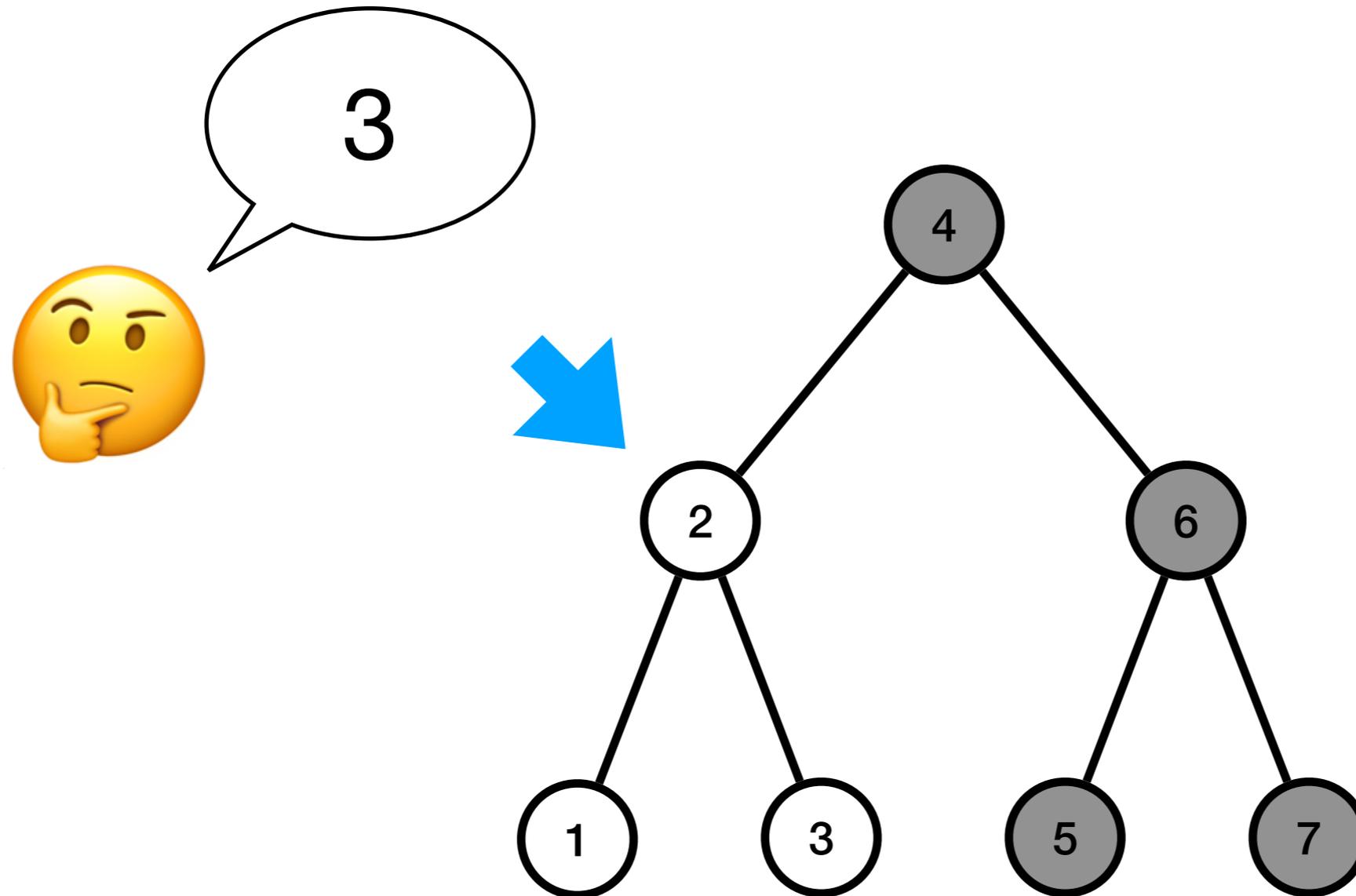
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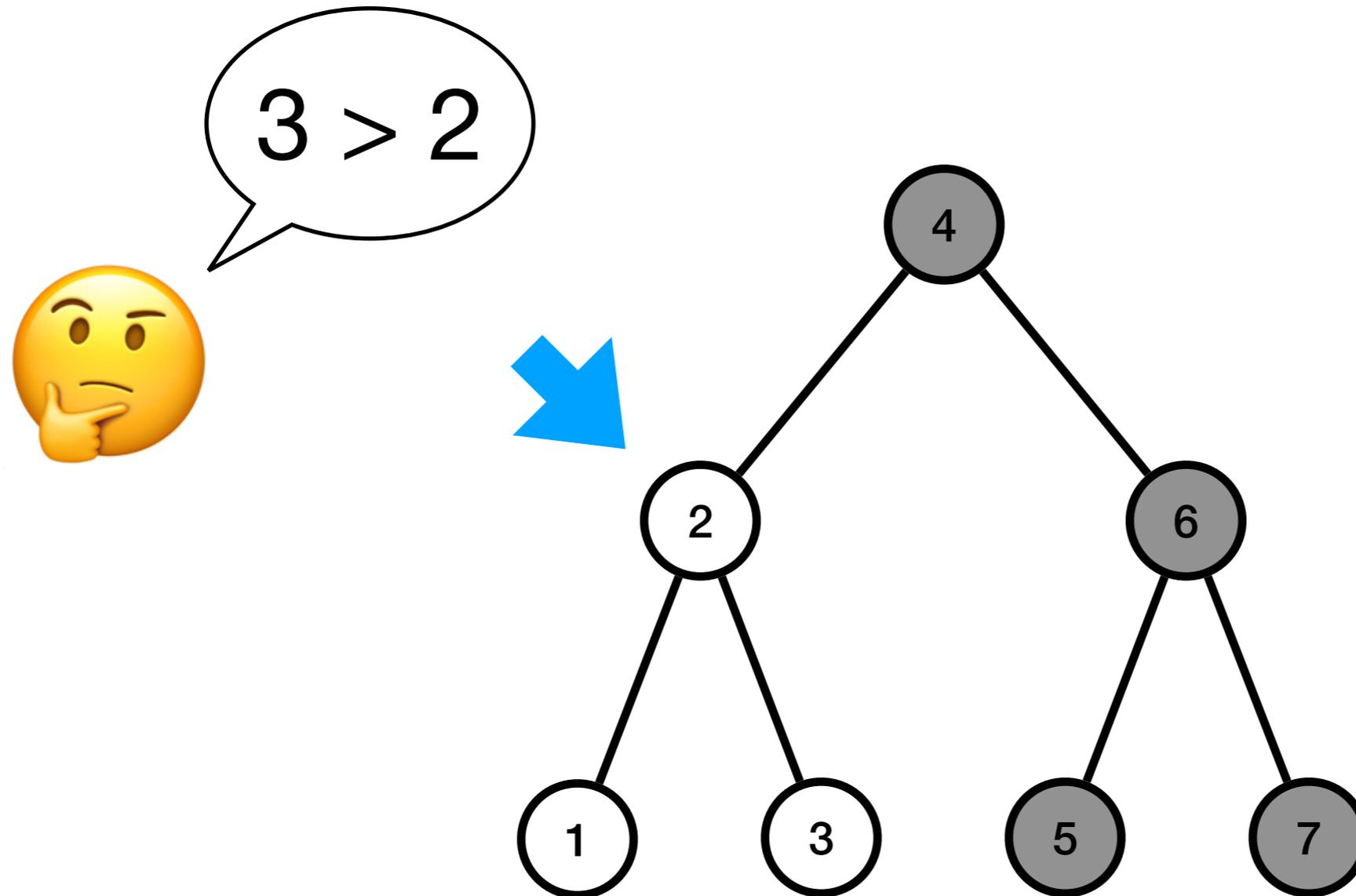
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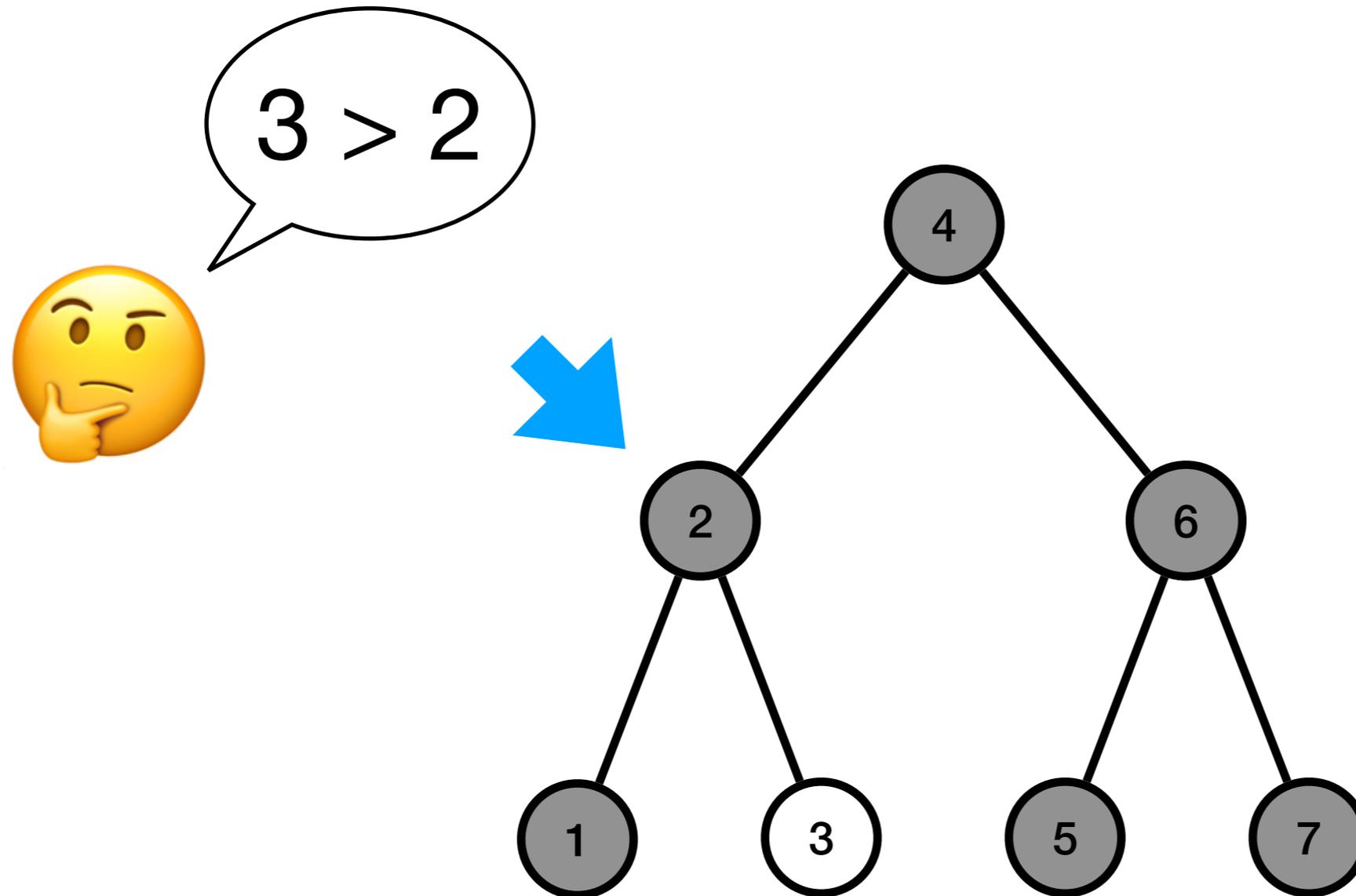
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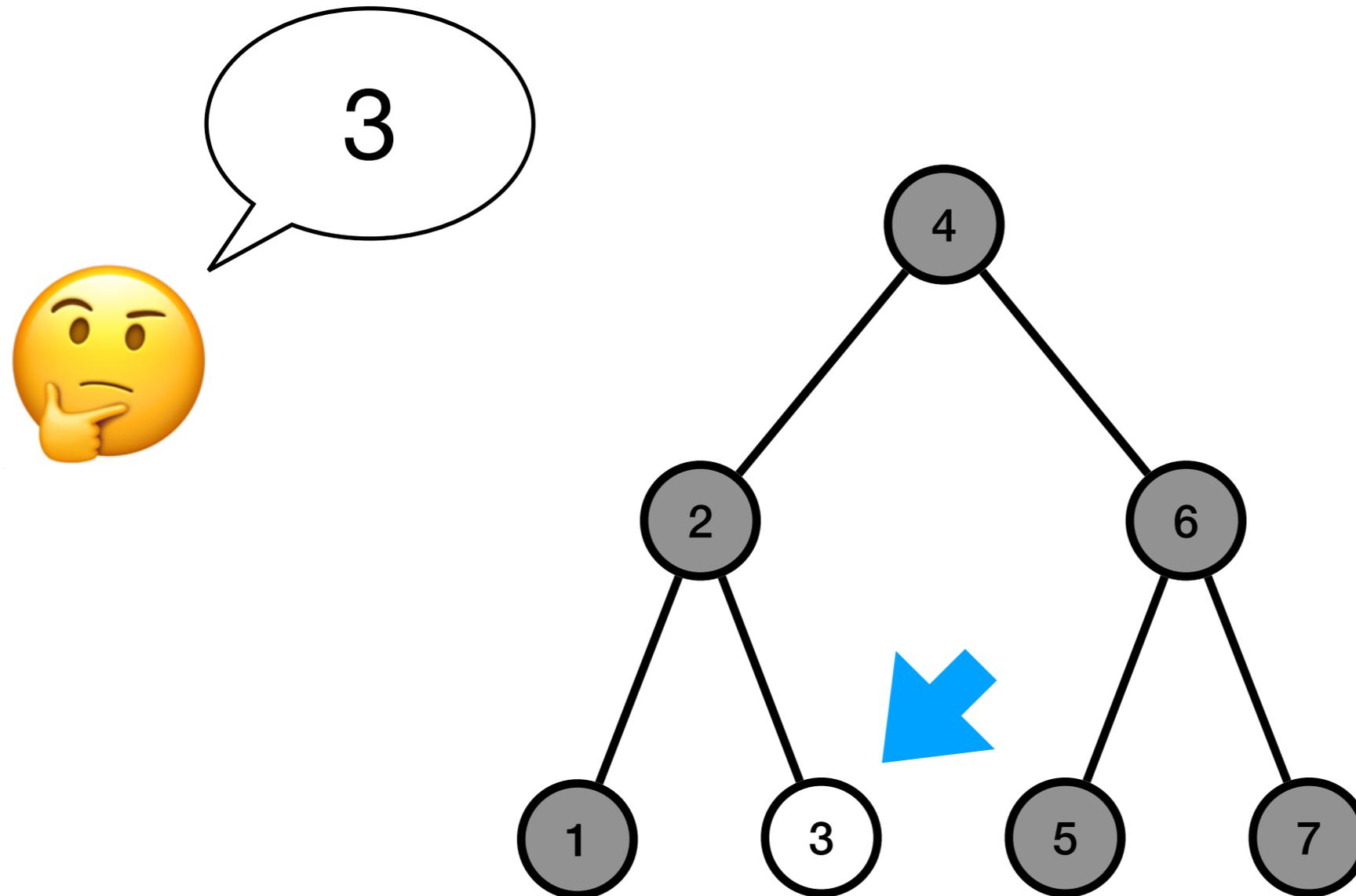
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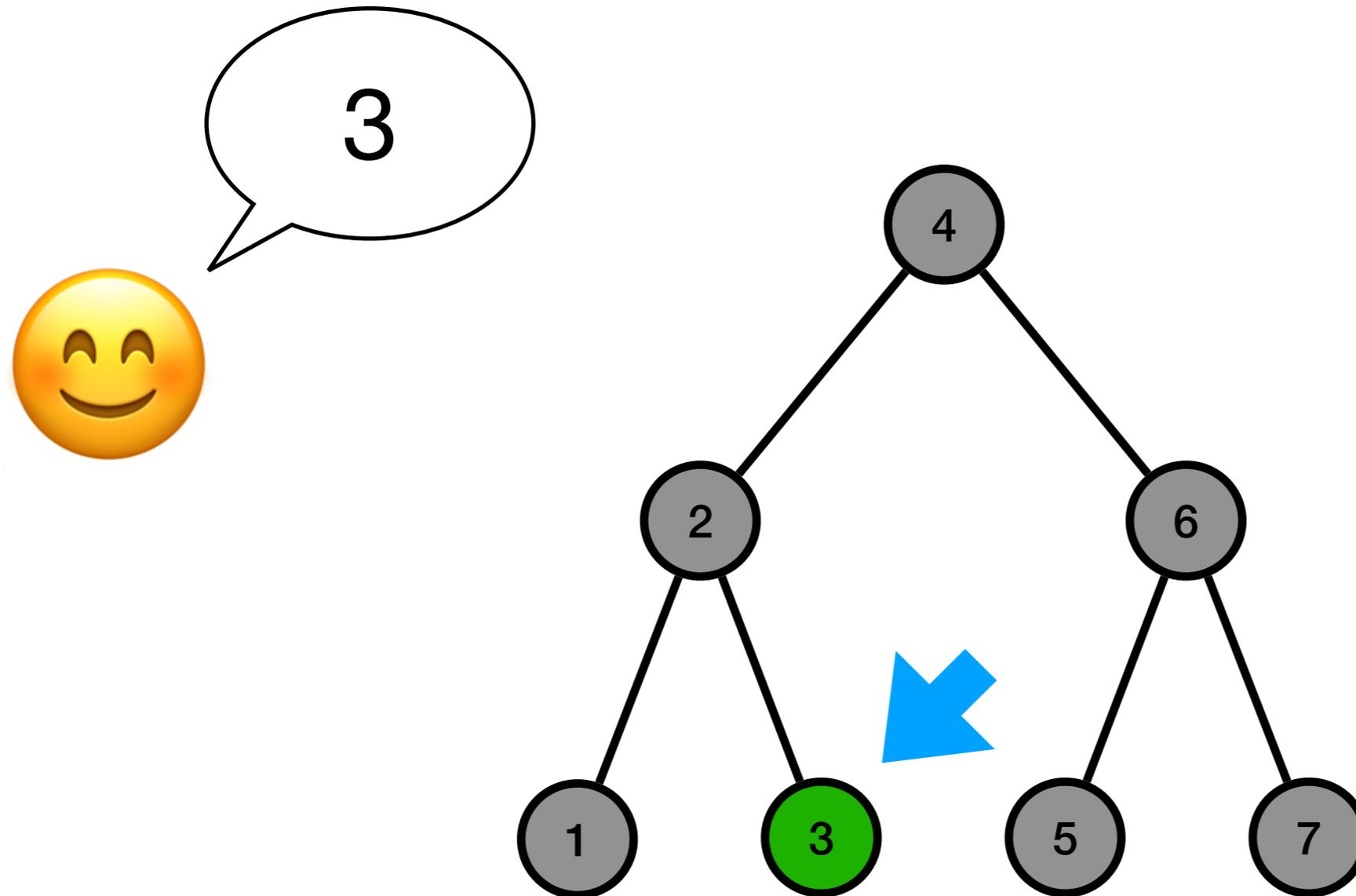
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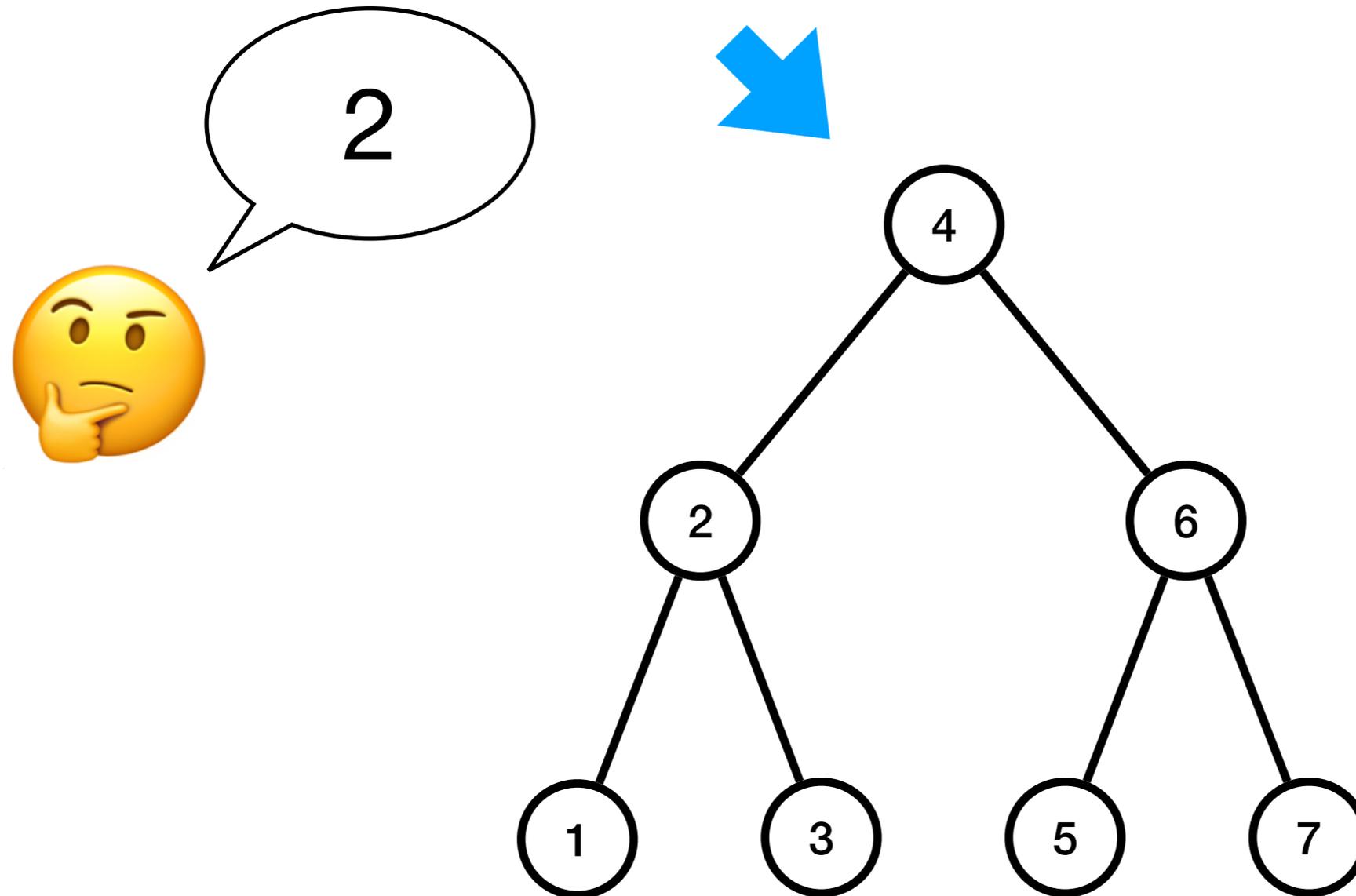
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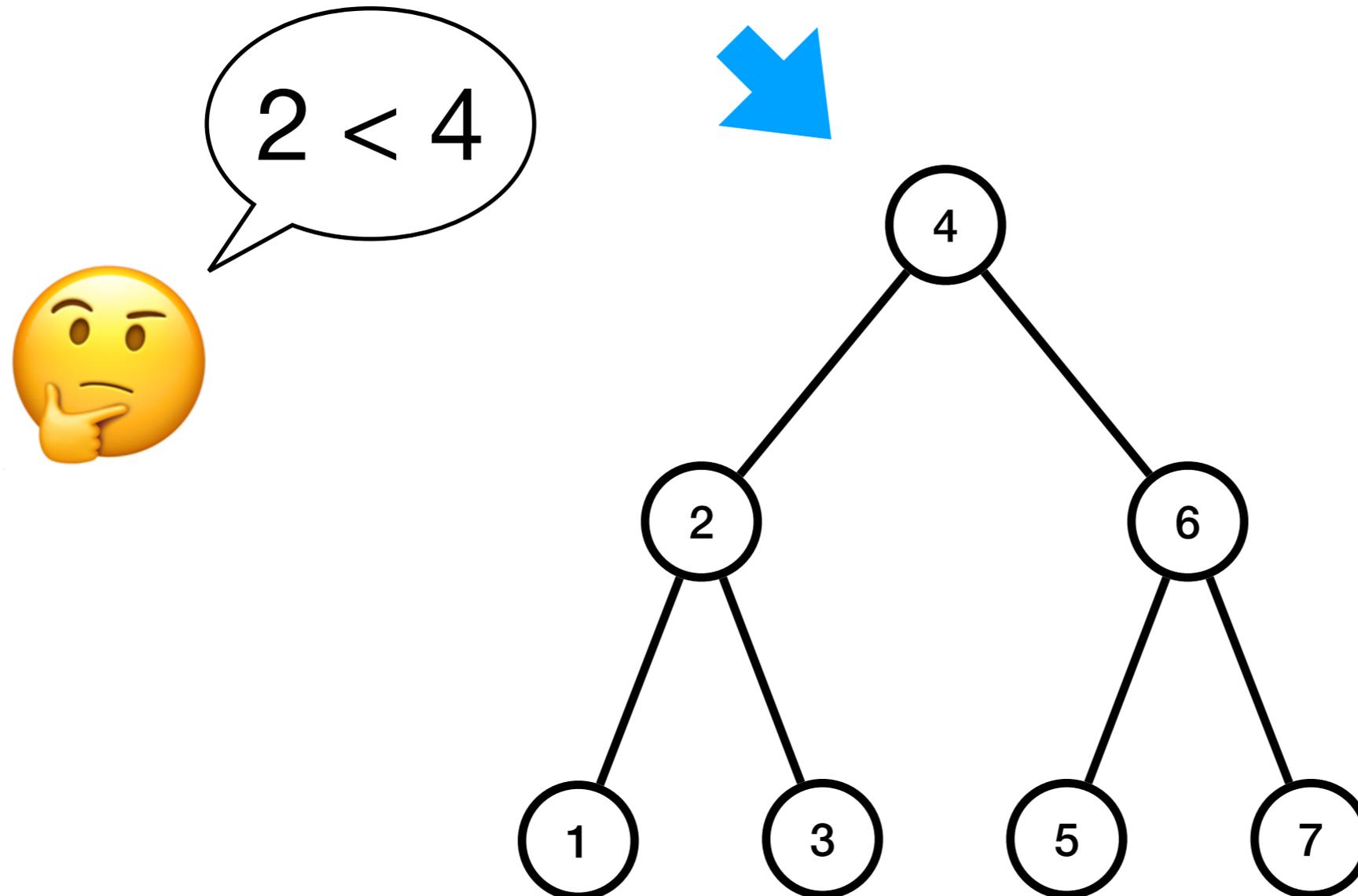
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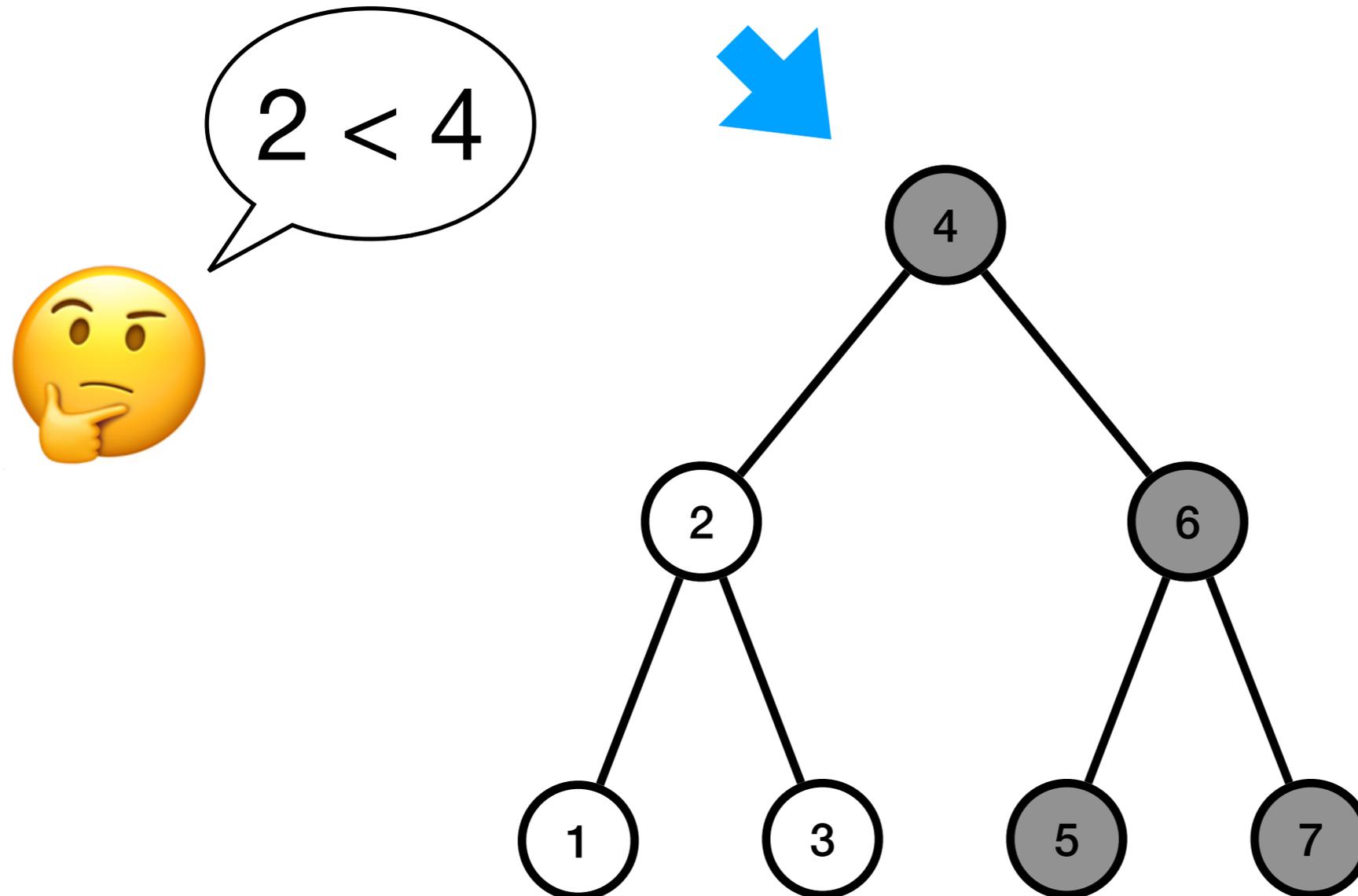
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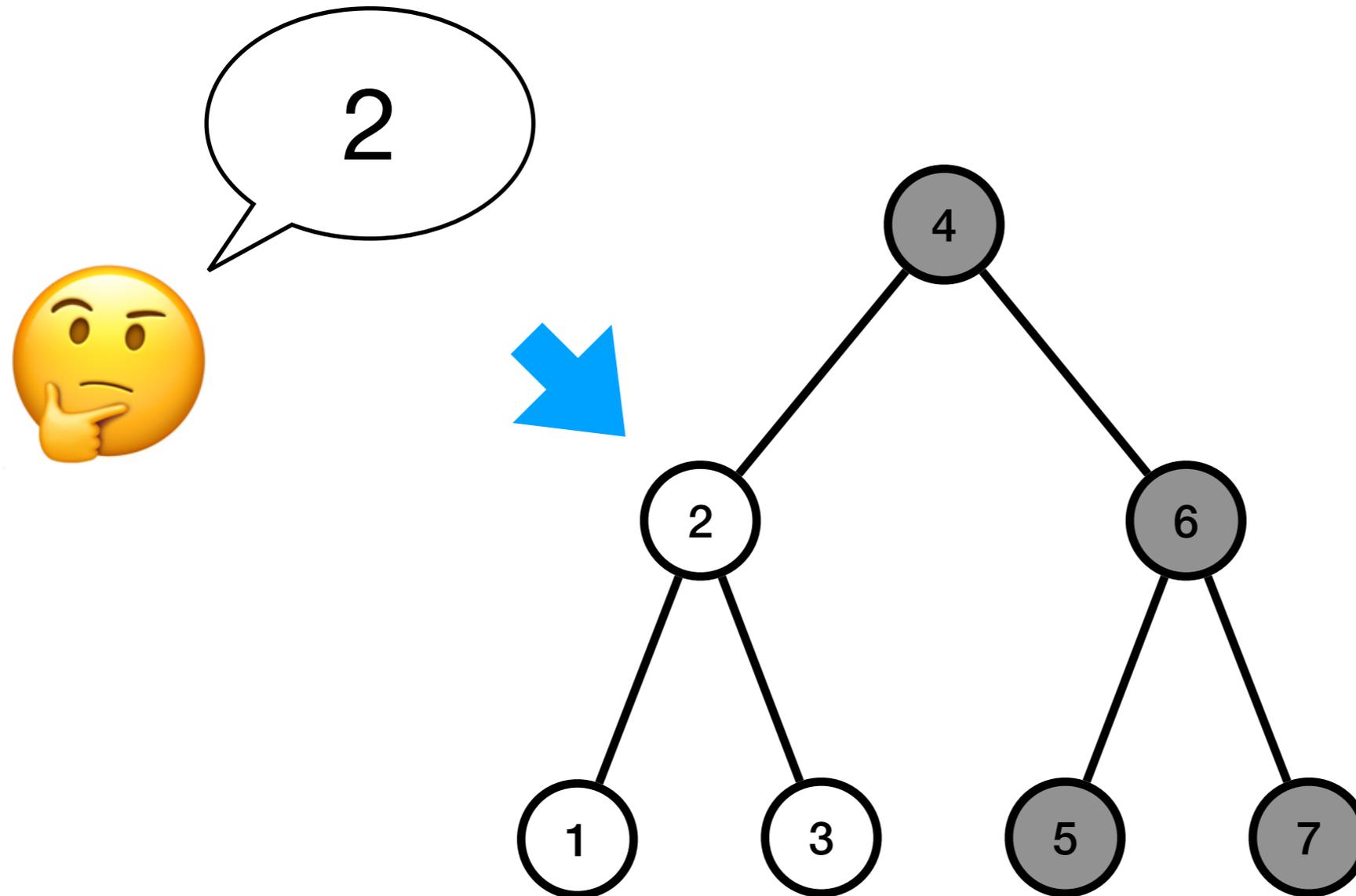
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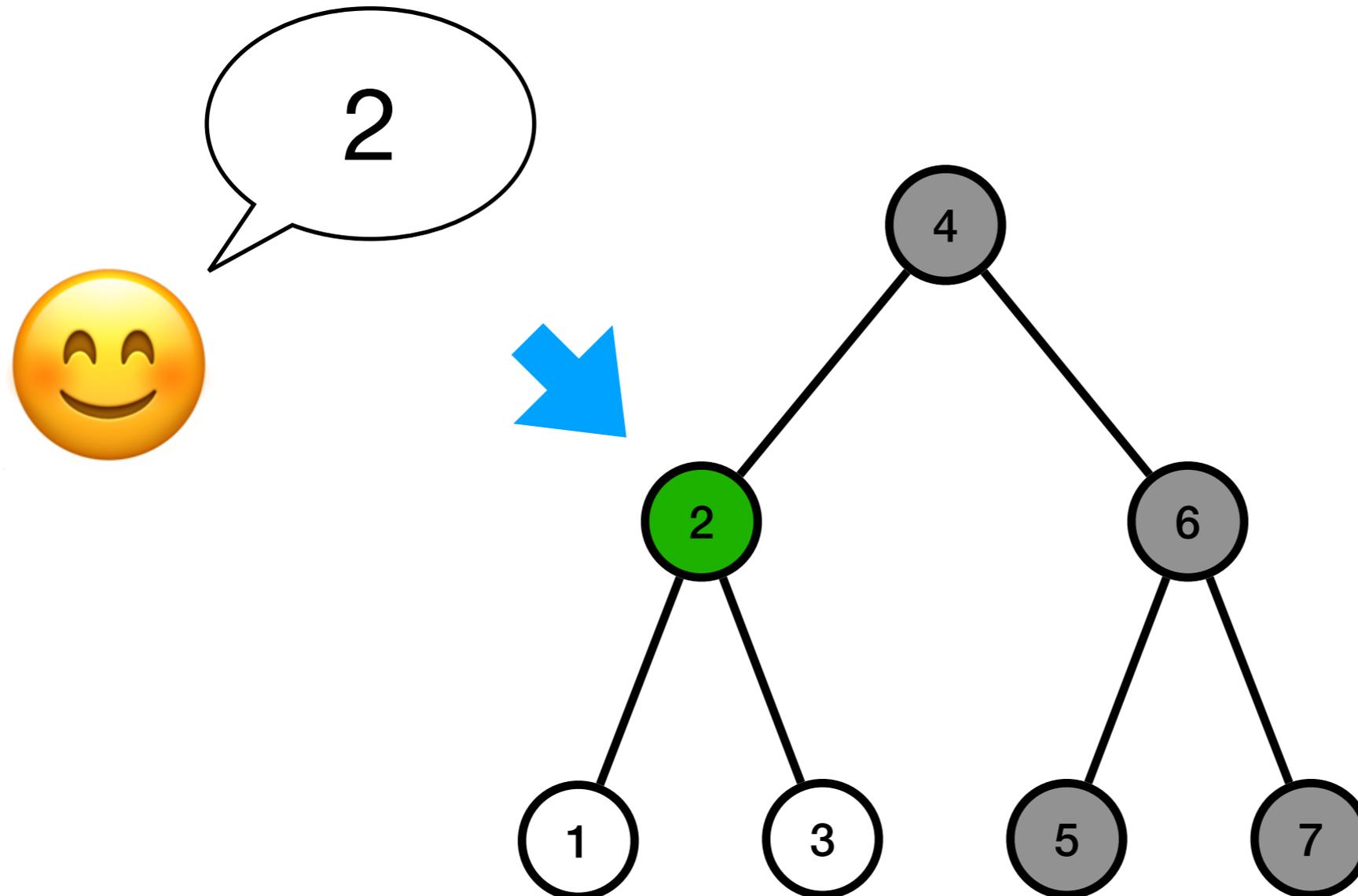
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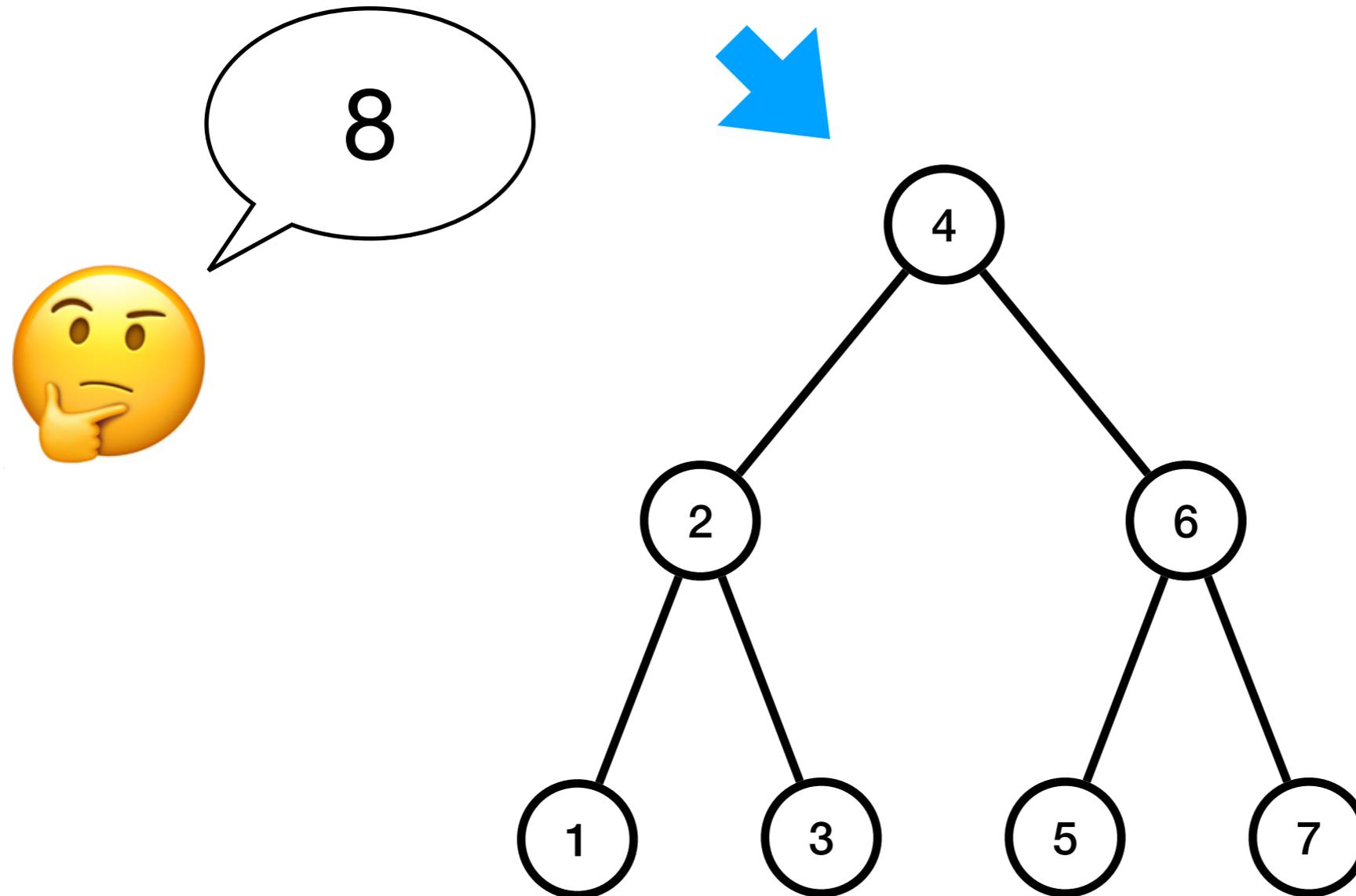
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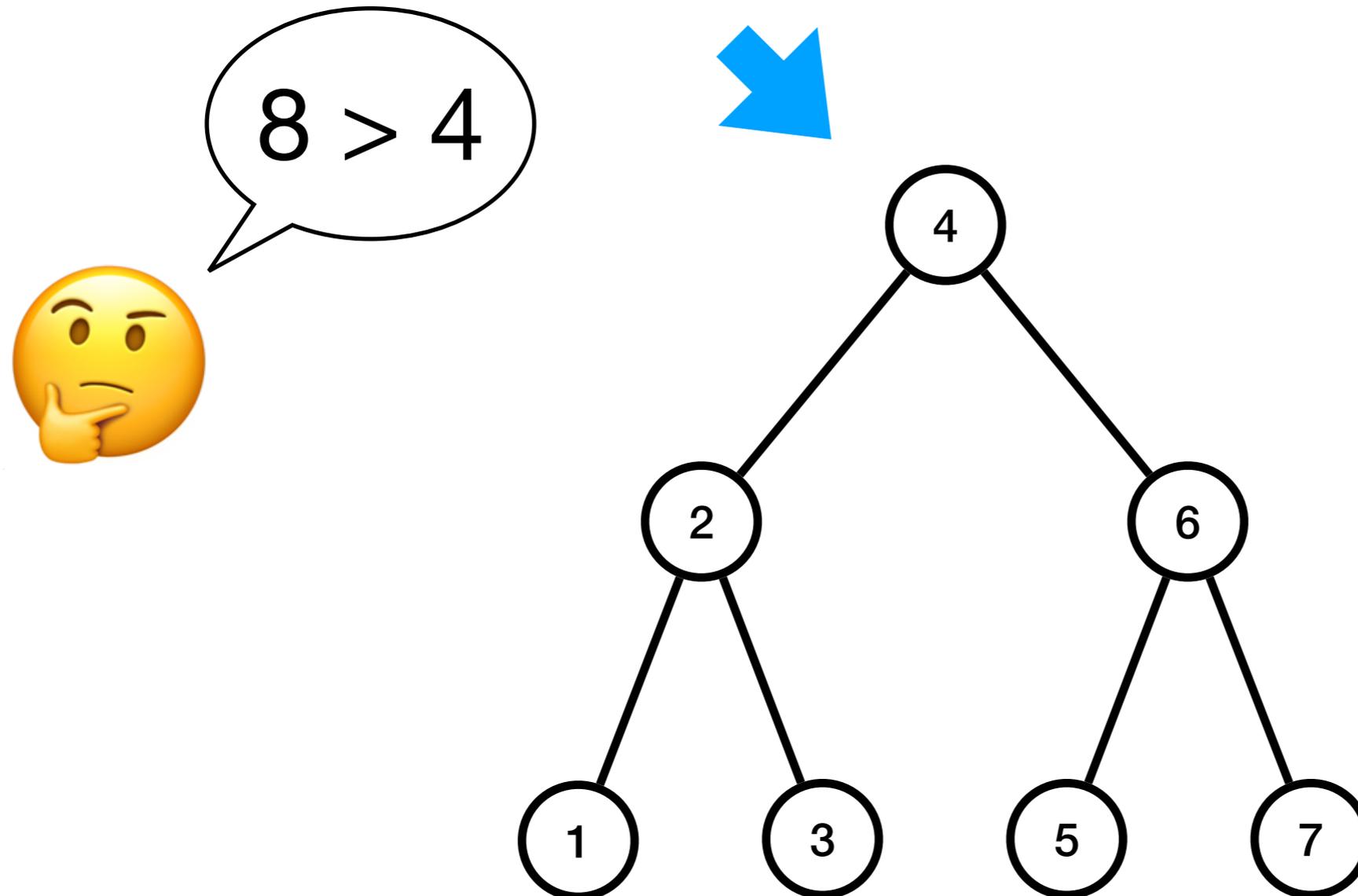
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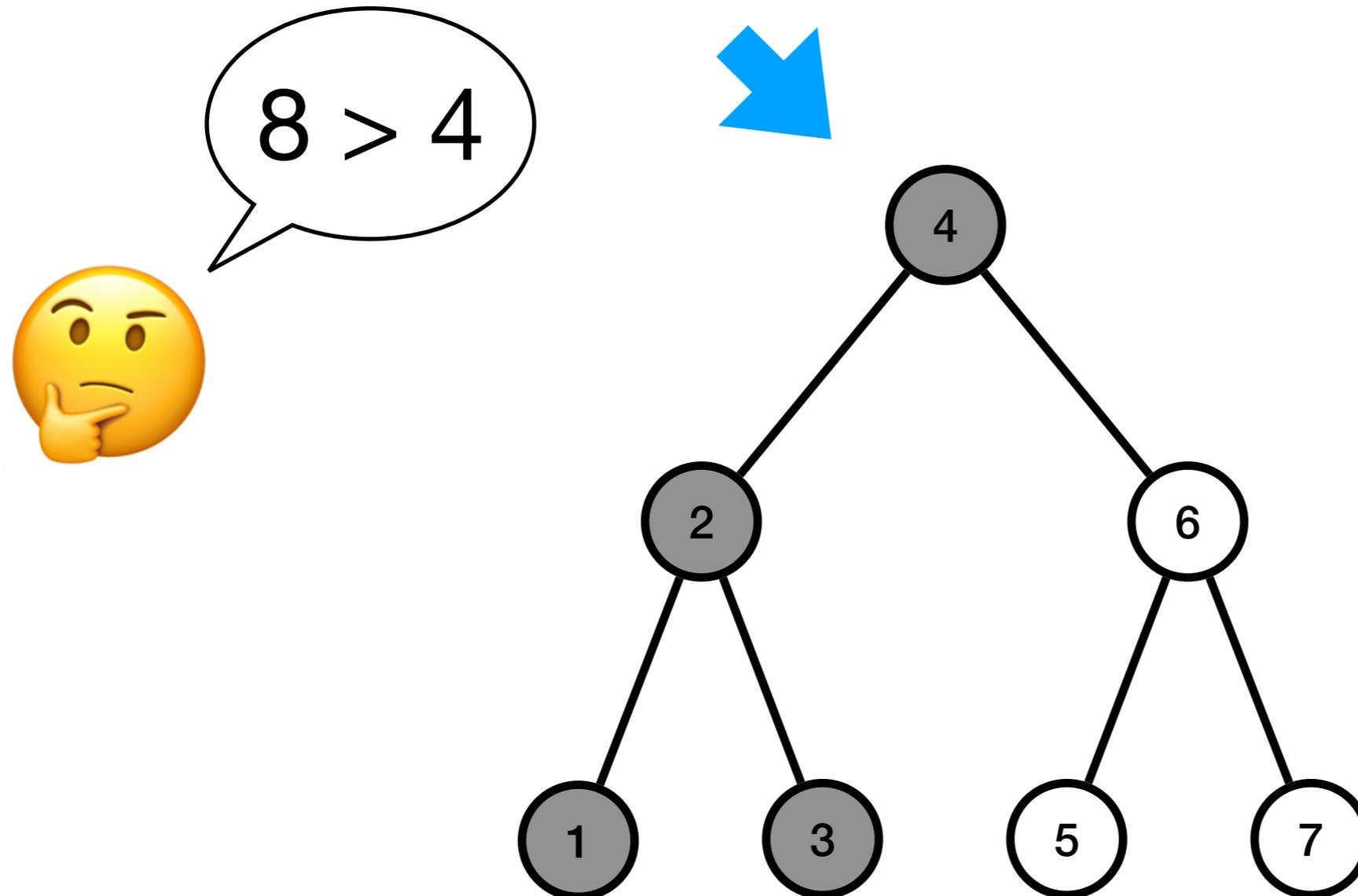
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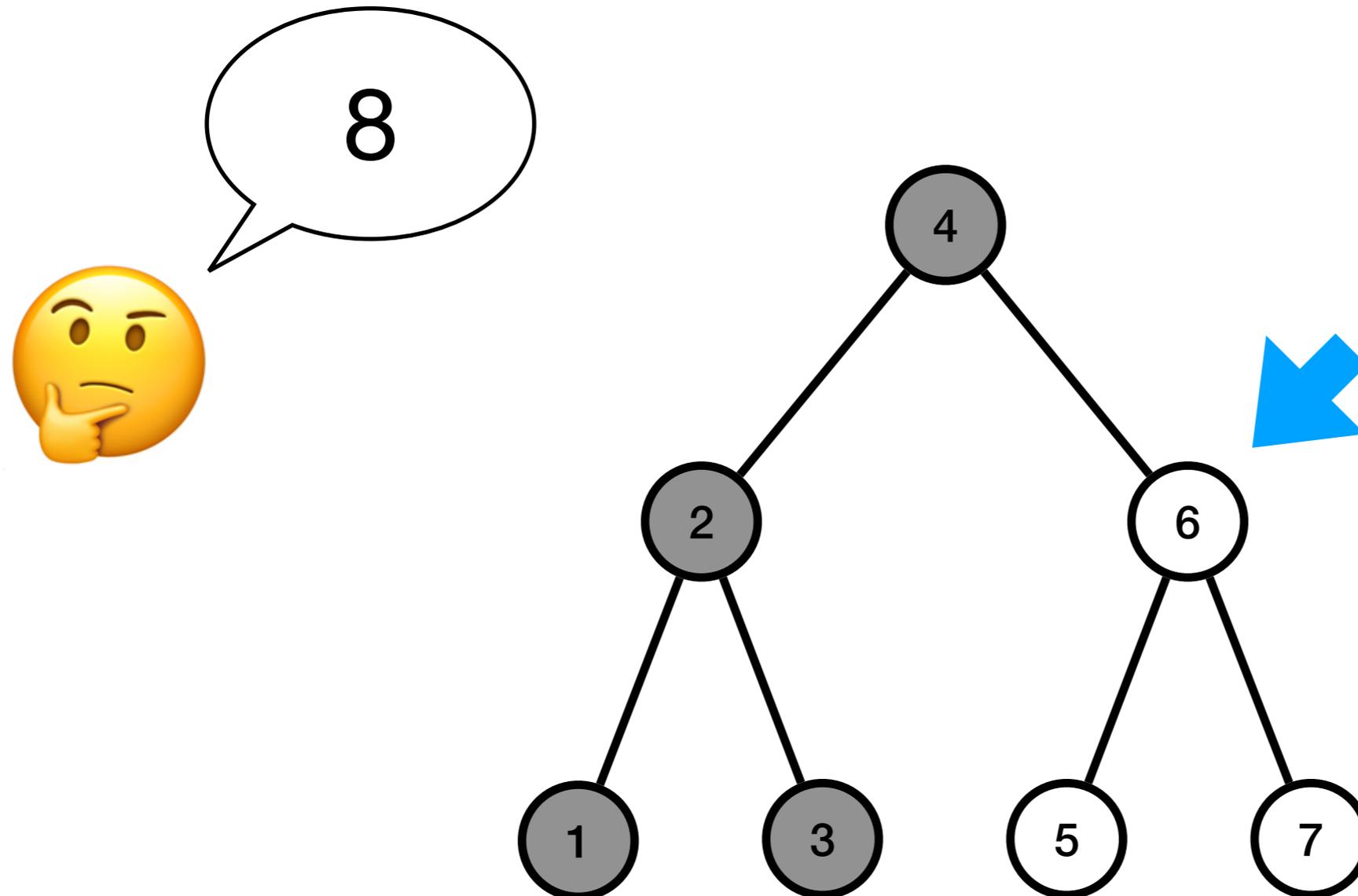
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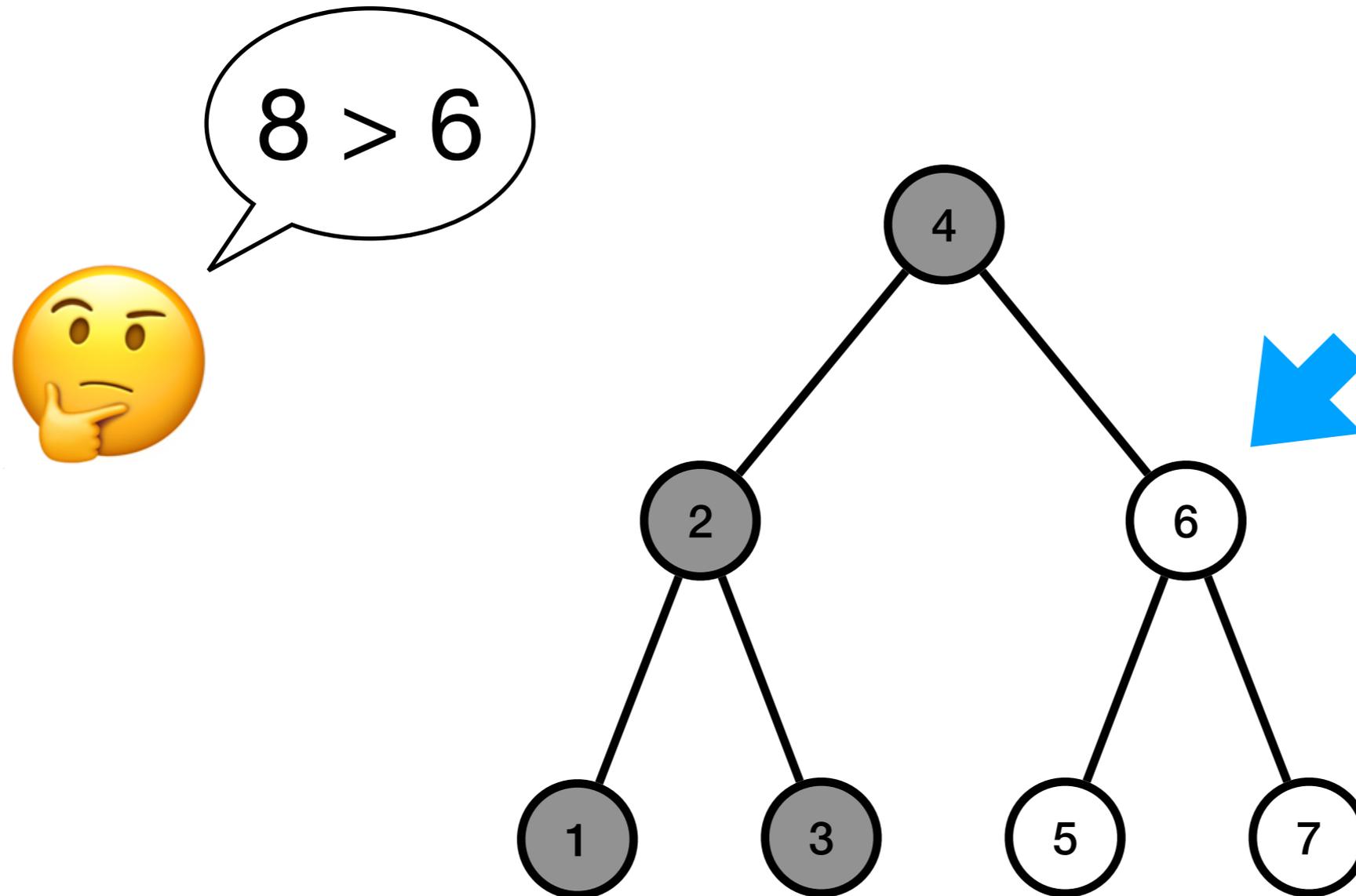
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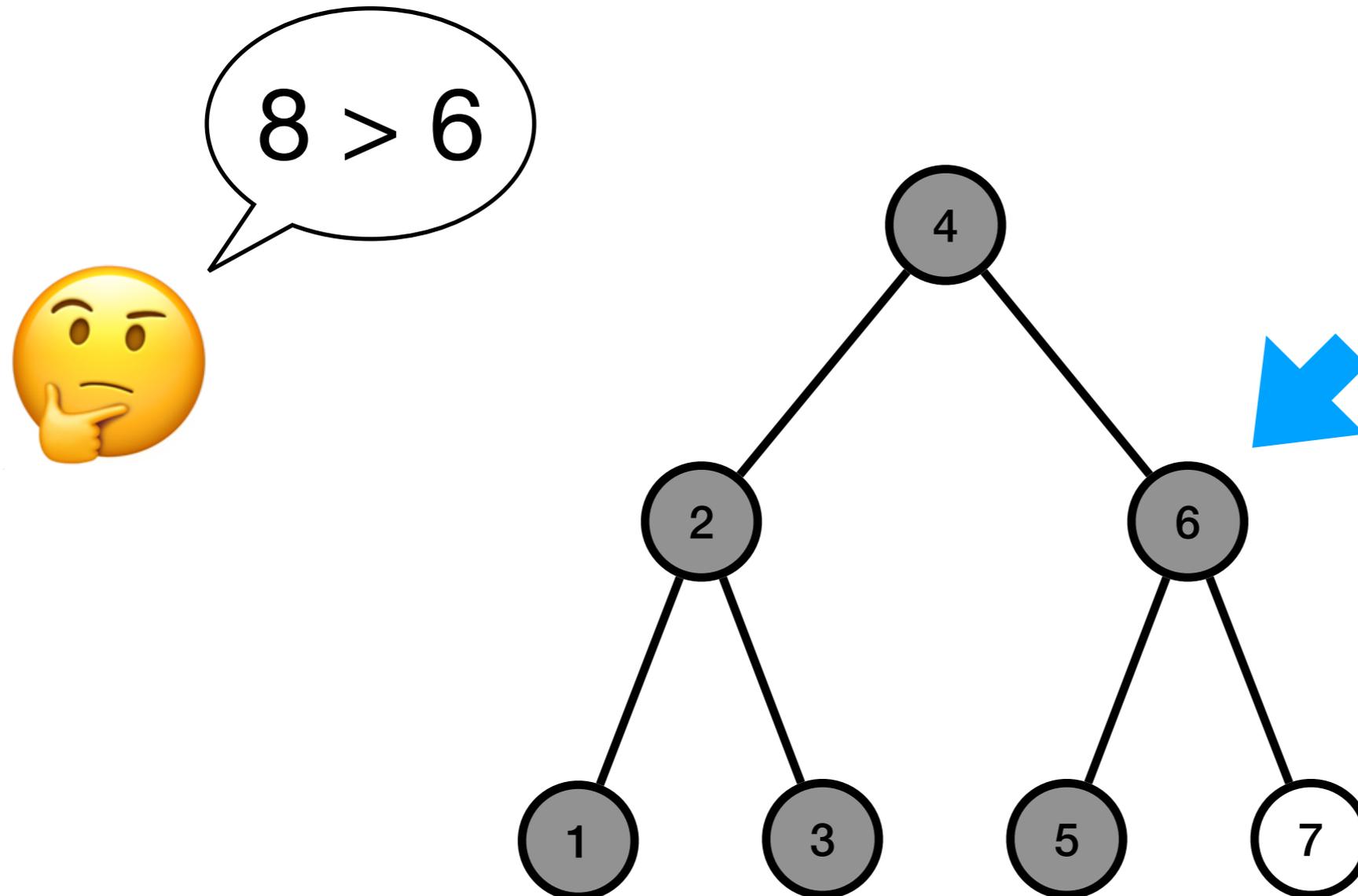
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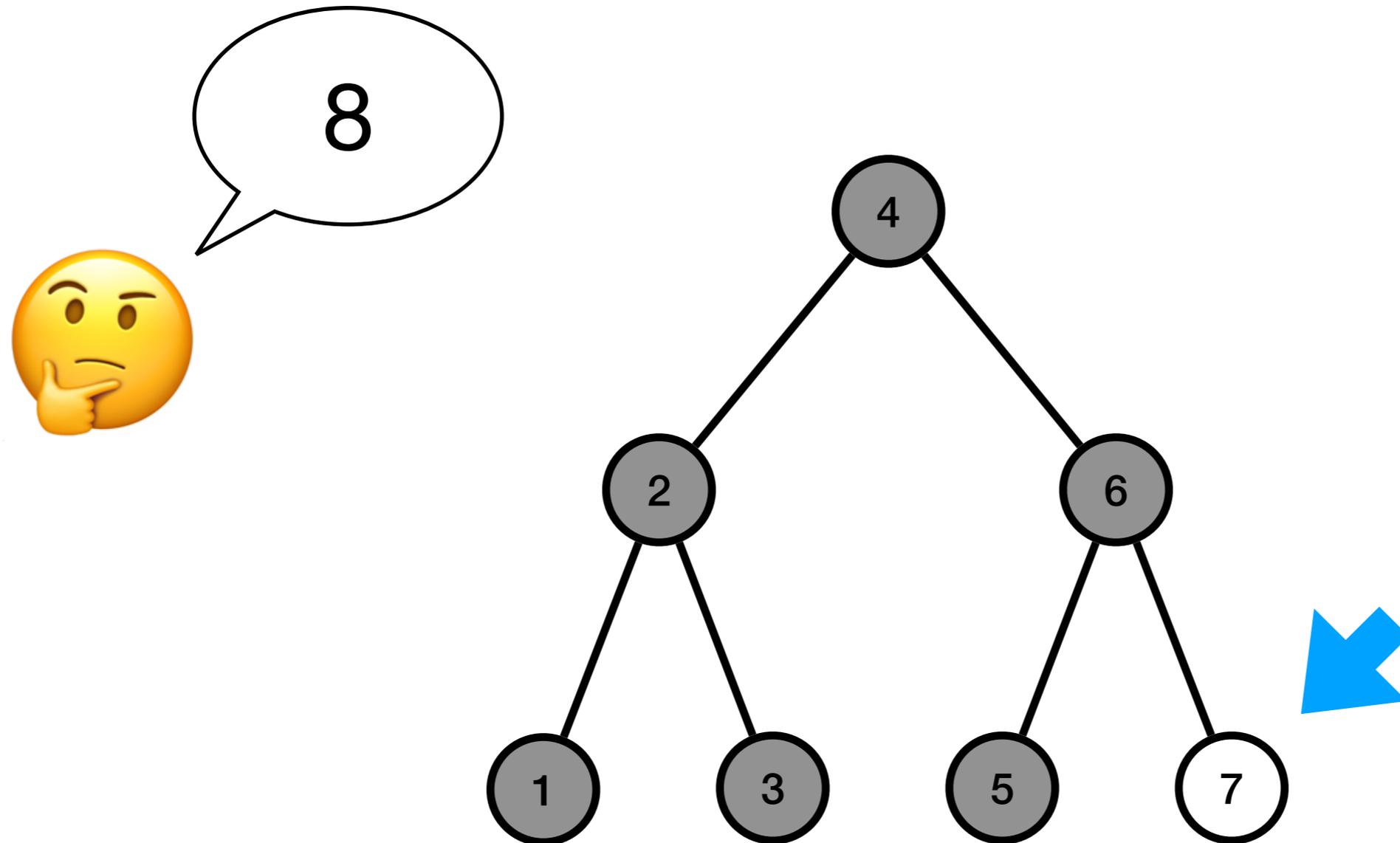
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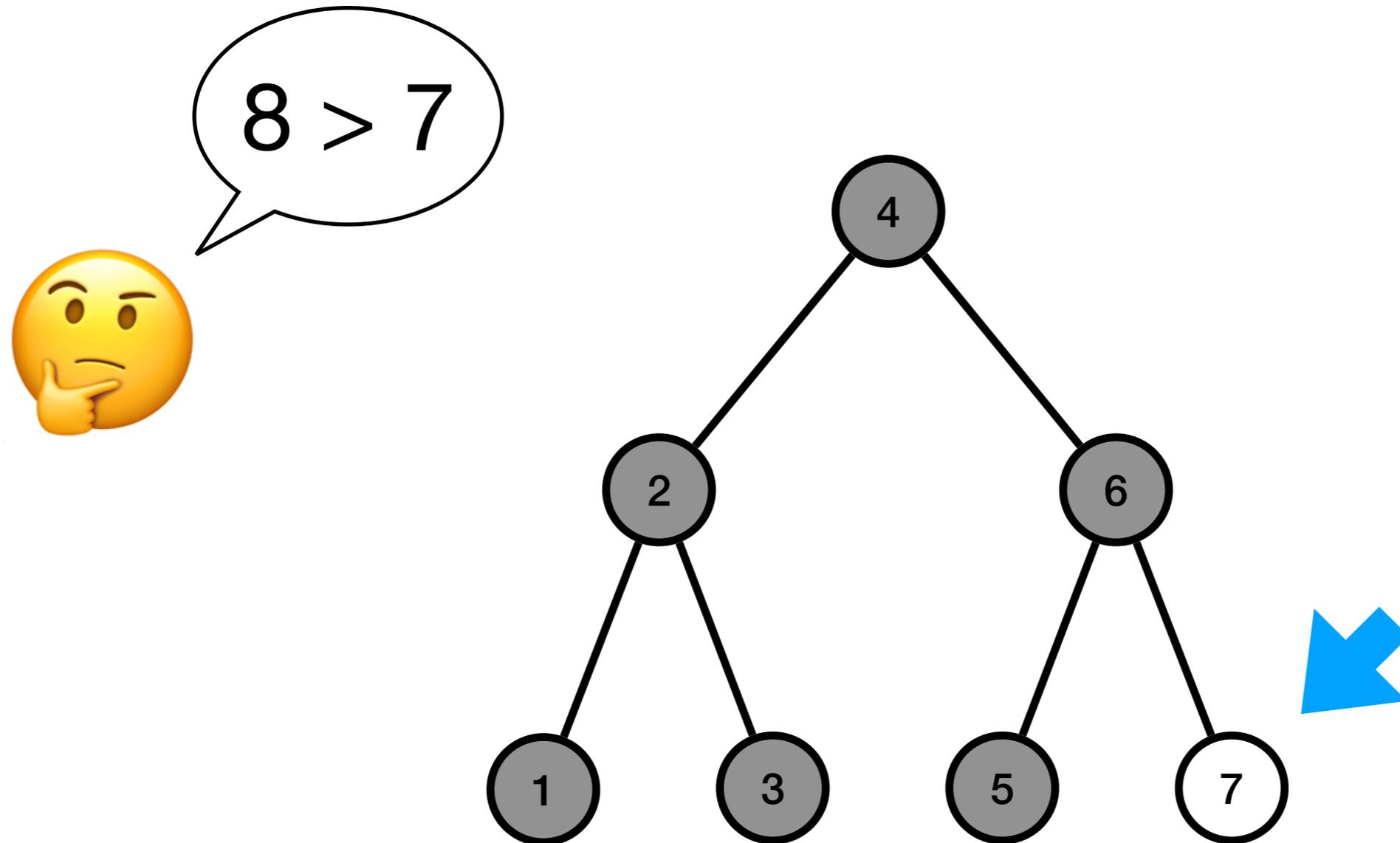
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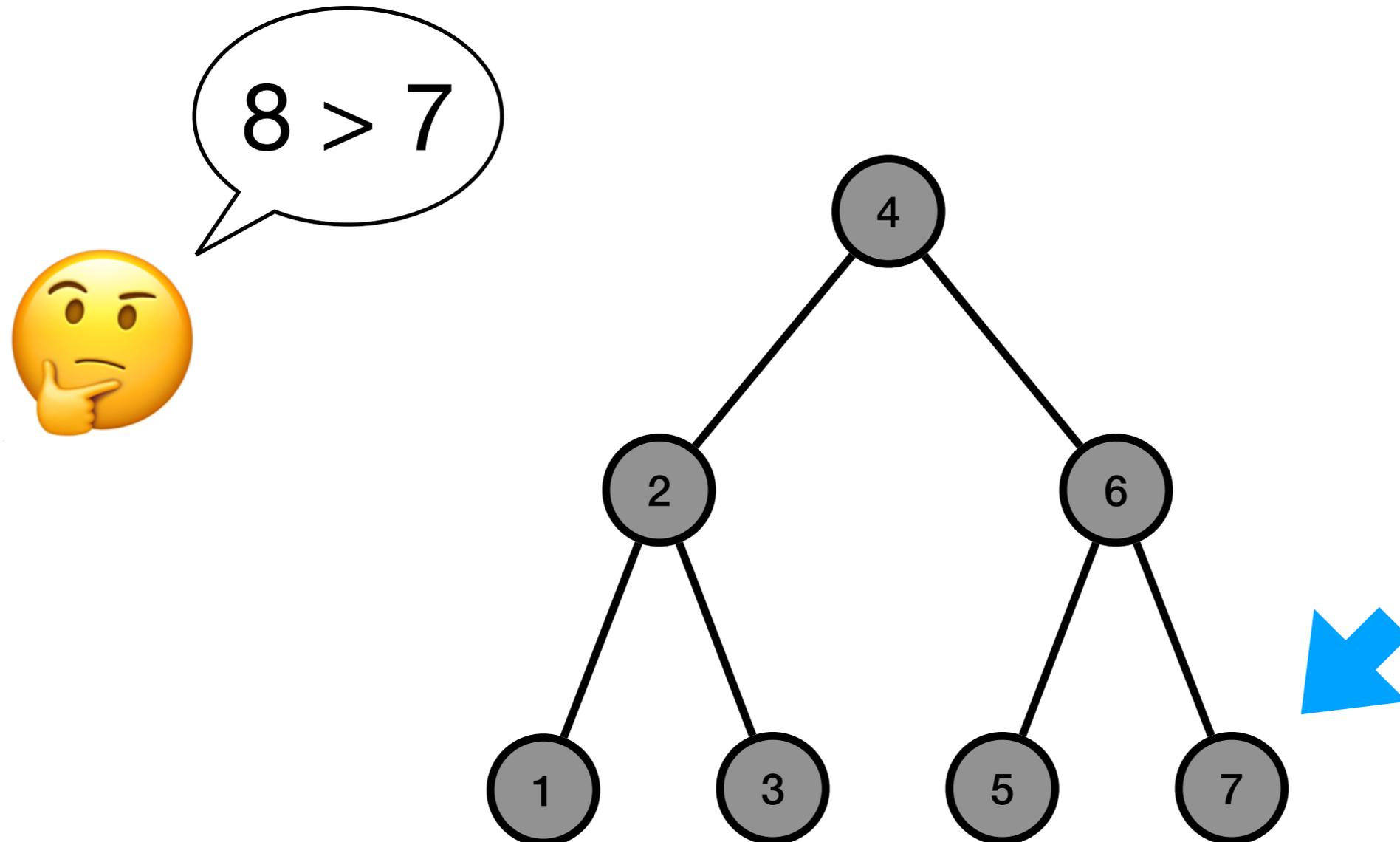
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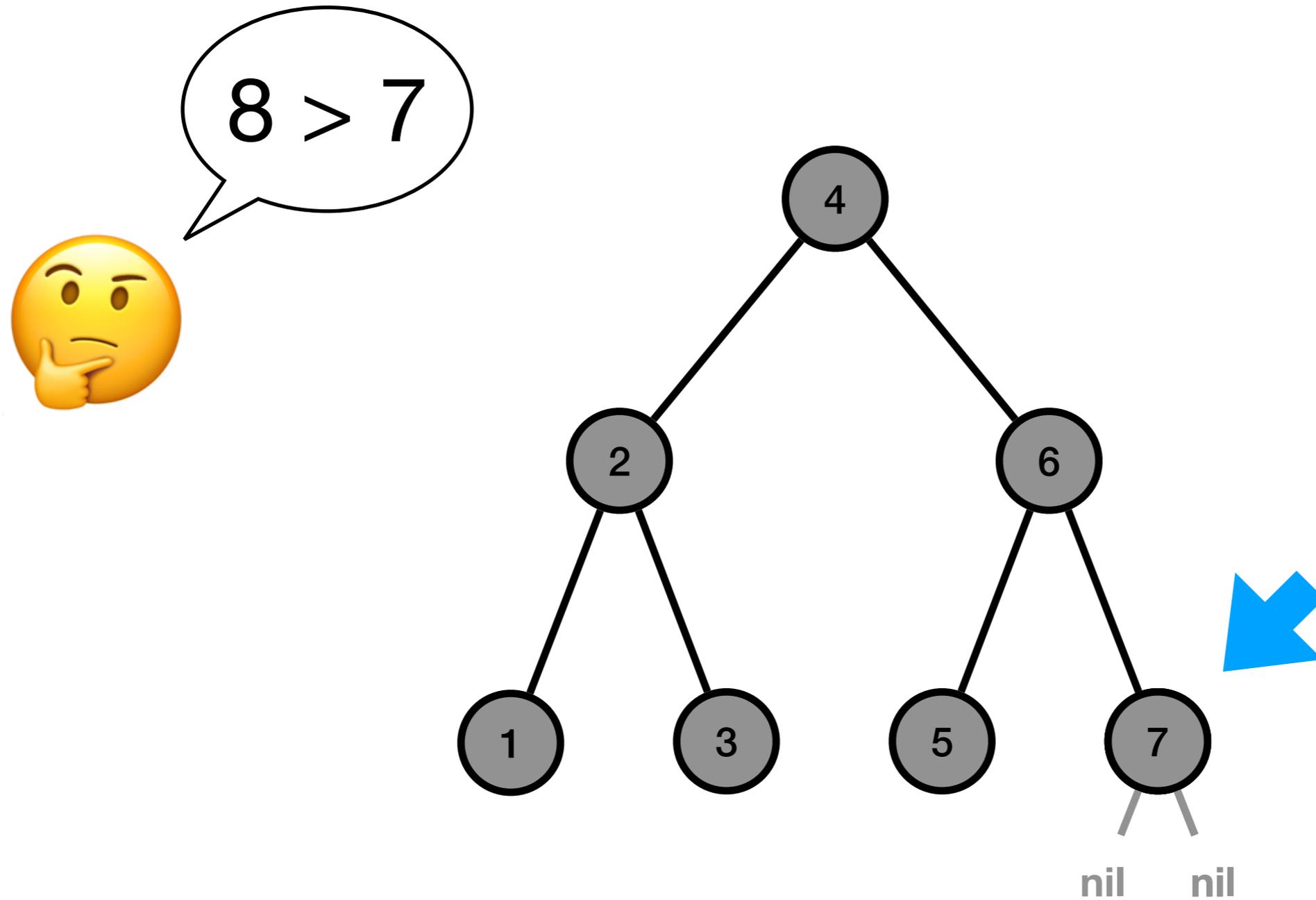
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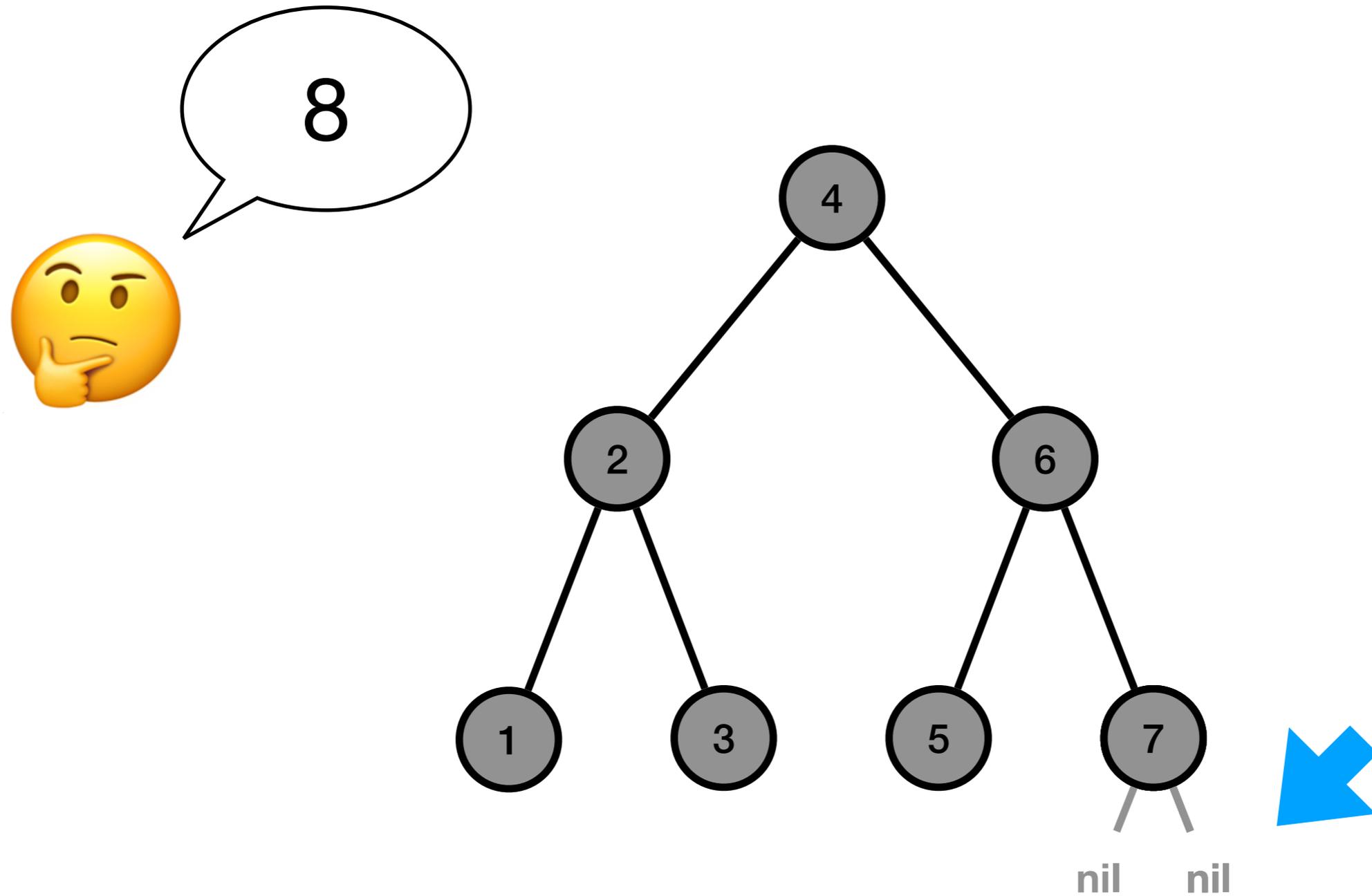
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Recherche dans un ABR



Recherche dans un ABR

